

# ST. PATRICK'S SCHOOL PRELIMINARY EXAMINATION 2021

SUBJECT

: Additional Mathematics

DATE

17 August 2021

Paper 1 (4049/01)

LEVEL

: Secondary 4 Express

DURATION:

2 hours 15 minutes

Candidates answer on the Question Paper.

## READ THESE INSTRUCTIONS FIRST

Write your Name, Class and Index No. in the spaces at the top of this page.

Write in dark blue or back pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

### Answer all the questions.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question. The use of an approved scientific calculator is expected, where appropriate.

You are reminded of the need for clear presentation in your answers.

The number of marks is given in brackets [] at the end of each question or part question. The total number of marks for this paper is 90.

For Exa	miner's Use	
Score		/90

#### Mathematical Formulae

# 1. ALGEBRA

# Quadratic Equation

For the equation 
$$ax^2 + bx + c = 0$$
,  
$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Binomial expansion

$$(a+b)^{n} = a^{n} + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^{2} + \dots + \binom{n}{r}a^{n-r}b^{r} + \dots + b^{n},$$

where *n* is a positive integer and  $\binom{n}{r} = \frac{n!}{(n-r)!r!} = \frac{n(n-1)...(n-r+1)}{r!}$ .

# 2. TRIGONOMETRY

## Identities

$$\sin^2 A + \cos^2 A = 1$$

$$\sec^2 A = 1 + \tan^2 A$$

$$\csc^2 A = 1 + \cot^2 A$$

$$\sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$$

$$\cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$$

$$\tan(A \pm B) = \frac{\tan A \pm \tan B}{1 \mp \tan A \tan B}$$

$$\sin 2A = 2\sin A \cos A$$

$$\cos 2A = \cos^2 A - \sin^2 A = 2\cos^2 A - 1 = 1 - 2\sin^2 A$$

$$\tan 2A = \frac{2\tan A}{1 - \tan^2 A}$$

Formulae for \( \Delta ABC \)

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$
$$a^2 = b^2 + c^2 - 2bc \cos A$$
$$Area of \Delta = \frac{1}{2}bc \sin A$$

- 1. Given that  $x^2 + 2x 3$  is a factor of f(x), where  $f(x) = x^4 + 4x^3 + 2x^2 + ax b$ .
  - (a) Find the values of a and b.

[4]

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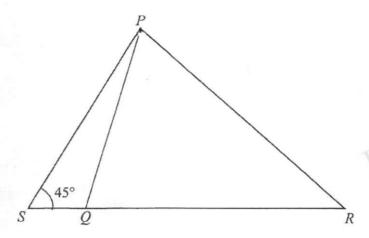
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(b) Hence, find the other quadratic factor of f(x).

[2]



2.



The diagram shows a triangle PQR with an area of 18 cm<sup>2</sup>. The base QR has a length of  $(4\sqrt{2} + 8)$  cm. The line RQ is extended to the point S where the angle  $PSR = 45^{\circ}$ .

(a) Find the perpendicular distance from P to QR, leaving your answer in the form  $a+b\sqrt{2}$ , where a and b are rational numbers,

[3]





(b) Find the exact length of PS, leaving your answer in the form  $m + n\sqrt{2}$ , where  $\underline{m}$  and n are integers.

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3. Given the curve  $y = \frac{1}{2}e^{2x} - \frac{1}{3}e^{-3x} + \frac{1}{3}$  and the normal to the curve at point  $P\left(\ln 2, \frac{55}{24}\right)$  crosses the y – axis at Q.

(a) Show that 
$$\frac{dy}{dx} = \frac{e^{5x} + 1}{e^{3x}}$$
.

[2]

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(b) Find the equation of the normal at  $P\left(\ln 2, \frac{55}{24}\right)$ , leaving your answer in exact form. [3]

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(c) Hence, find the coordinates of Q.

4. (a) Find the coordinates of the stationary points on the graph of  $y = 2x^3 - 9x^2 + 13$ . [4]



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(b) Hence, determine the nature of the stationary point(s).

<sup>L</sup>[3]





5. (a) Differentiate  $2x\cos 2x$  with respect to x.

[2]

(b) Hence, evaluate  $\int_0^{\frac{\pi}{2}} (1 - 4x \sin 2x) dx$ .

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- 6. It is given that  $y = (x-2)(2x-5)^3$ .
  - (a) Obtain an expression for  $\frac{dy}{dx}$  in the form  $(ax+b)(2x-5)^2$ , where a and b are integers.

[2]

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(b) Determine the values of x for which y is a decreasing function.

[2]



The variables x and y are such that, when x = 3, y is increasing at a rate of 0.35 units per second.

(c) Find the rate of change of x when x = 3.



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It is given further that the variable z is such that  $z = y^2$ .

(d) Show that, when 
$$x = 3$$
, z is increasing at twice the rate of y.

[2]





7. (a) Given that 
$$\sqrt{125^x} = \frac{5^{1-x}}{25}$$
, find the value of  $\sqrt{125^x}$ .

[4]

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(b) Show that 
$$\log_2 x - \log_{16} x = \frac{3 \lg x}{4 \lg 2}$$
.

[4]

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8. (a) Write down the general term,  $T_{r+1}$ , for the binomial expansion of  $\left(2x + \frac{1}{2x^3}\right)^{12}$ . [1]

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(b) Find the term independent of x in the expansion of  $\left(\frac{1}{x^4} - 1\right) \left(2x + \frac{1}{2x^3}\right)^{12}$ . [5]

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(c) Explain whether there are any terms containing  $x^n$ , where n is odd in the expansion of

$$\left(2x+\frac{1}{2x^3}\right)^{12}.$$

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9. (a) Prove that 
$$\frac{\sec^2 x}{1+\sec^2 x} = \frac{2}{\cos 2x + 3}$$
.

[3]

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(b) Hence, solve the equation 
$$\frac{\sec^2 2x}{1+\sec^2 2x} = \frac{4}{7}$$
 for  $0 \le x \le 3$ .

[4]

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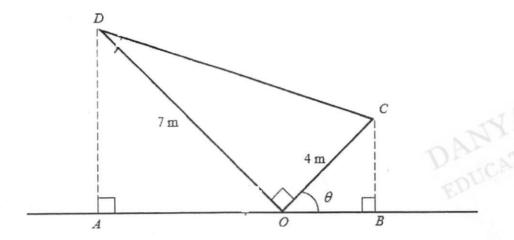
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(c) State the number of solutions for  $-2\pi \le x \le 2\pi$ .

[1]



10.



In the diagram, OC = 4 m, OD = 7 m and angle CBO = angle DOC = angle  $DAO = 90^{\circ}$ . It is also given that angle  $COB = \theta$  such that  $0^{\circ} \le \theta \le 90^{\circ}$ .

(a) Express AB in the form  $p \sin \theta + q \cos \theta$  where p and q are integers. [2]



(b) Hence, express AB in the form  $R \sin (\theta + a)$  where R is positive and a is acute. [3]



(c) State the maximum length of AB and its corresponding value of  $\theta$ .

[3]

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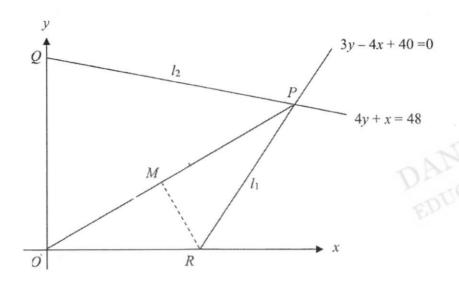
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(d) Find the value of  $\theta$  when  $AB = \sqrt{55}$  m.

[3]



11.



The diagram shows lines  $l_1$  and  $l_2$  intersecting at P. Line  $l_1$  has equation 3v - 4x + 40 = 0and  $l_2$  has equation 4y + x = 48. The point M is the midpoint of OP. The line  $l_2$  intersects the y-axis at Q and the line  $l_1$  intersects the x-axis at R. DANYAL DANYAL EDUCATION

(a) Show that OP is perpendicular to MR.

[5]



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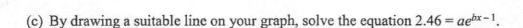
12. The table shows experimental values of two variable, x and y, which are connected by the equation  $y = ae^{bx-1}$ , where a and b are constants.

X	1	2	3	4	5
У	1.89 ,	2.3	2.82	3.44	4.20

(a) On the grid given on page 23, using a scale of 2 cm to represent 1 unit on the horizontal axis and 2 cm to represent 0.2 units on the vertical axis, plot a straight line graph of ln y against x. [3]

(b) Use your graph to estimate the value of a and of b.

[3]



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# ST. PATRICK'S SCHOOL PRELIMINARY EXAMINATION 2021

SUBJECT

: Additional Mathematics

DATE

23 August 2021

Paper 2 (4049/02)

LEVEL

: Secondary 4 Express

DURATION:

2 hours 15 minutes

Candidates answer on the Question Paper.

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where *n* is a positive integer and  $\binom{n}{r} = \frac{n!}{(n-r)!r!} = \frac{n(n-1)...(n-r+1)}{r!}$ .

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Formulae for AABC

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$Area \text{ of } \Delta = \frac{1}{2}bc \sin A$$

1. (a) Express  $y = 2x^2 - 4x + 7$  in the form  $a(x - b)^2 + c$ , where a, b and c are constants. [3]



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(b) Hence, explain why the curve lies completely above the x-axis.

[2]





2. A virus is spreading in a country. The number of infected cases, I, after t days, can be modelled by  $I = \frac{a}{b+2^{20-t}}$ , where a and b are constants. The number of infected cases was 3600 after 16 days. Four days later, the number of infected cases increased to 9000.

(a) Show that a = 90000 and b = 9.

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(b) Given that the number of infected cases first exceeds 100 after n days, where n is an integer, find the value of n. [3]

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(c) Describe what happens to the number of infected cases in the long run.

[1]



3. (a) Without the use of calculator, show that  $\sin 75 = \frac{\sqrt{2} + \sqrt{6}}{4}$ . [3]

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- (b) In a city in the United Kingdom, the number of daylight hours is given by  $h(t) = -4\cos(bt) + 12$ , where t is an integer ranging from 1 to 12 inclusive that represents the month of January to December. It takes 12 months before the number of daylight hours reaches its lowest point again.
  - (i) Explain, with workings clearly shown, why  $b = \frac{\pi}{6}$ . [2]

(ii) Sketch the graph of h(t), where  $0 \le t \le 18$ .

[3]



4. (a) Show that 
$$\frac{d}{dx} \left( \frac{\ln x}{x^4} \right) = \frac{1}{x^5} - \frac{4 \ln x}{x^5}.$$

[3]

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(c) Given that the curve y = f(x) passes through the point  $\left(1, \frac{3}{4}\right)$  and is such that

$$f'(x) = \frac{\ln x}{x^5}$$
, find  $f(x)$ .

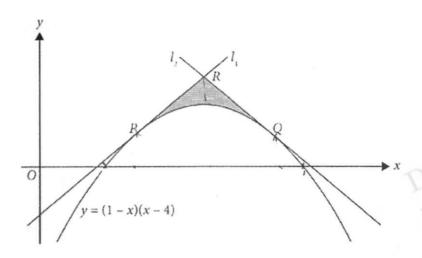
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5.



The diagram shows part of the curve y = (1-x)(x-4) and two lines  $l_1$  and  $l_2$ . The lines  $l_1$  and  $l_2$  are tangents to the curve at points P and Q and have gradients 2 and -2 respectively.

(a) Show that coordinates 
$$P$$
 and  $Q$  are  $\left(\frac{3}{2}, \frac{5}{4}\right)$  and  $\left(\frac{7}{2}, \frac{5}{4}\right)$  respectively. [3]



The lines  $l_1$  and  $l_2$  intersect at point R.

(b) Find the coordinate of point R.

[2]



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(c) Hence, find the shaded area PQR.

[4]





6. (a) Find the set of values of x for which  $5x^2 + 12x > 3x + 2$ .

[3]

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(b) The line y = mx + c does not intersect the curve  $x^2 + y^2 = 8$ .

(i) Prove that  $8m^2 + 8 < c^2$ .

[4]



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(ii) Hence, determine whether the line y = 2x + 5 intersects the curve  $x^2 + y^2 = 8$ . [2]



- 7. The equation of a circle is  $x^2 + y^2 + 2x 8y 8 = 0$ .
  - (a) Find the coordinates of the centre, C and the radius of the circle.

[3]

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(b) Find the equation of the tangent to the circle at the point P(-2, 8).

[3]



(c) If the circle is reflected in the line y = 1, find the equation of the reflected circle.

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[2]

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square the

(d) Find the area of the biggest square that can be drawn inside the circle.

[2]







(b) Hence, express 
$$\frac{8x^3 + 3x + 1}{x(2x+1)^2}$$
 as a sum of a polynomial and a partial fraction. [5]

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Space for Q8(b)

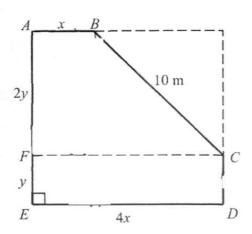
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9.



ABCDEF is the cross-sectional plan of a temporary spectator stand, where AB is parallel to FC and ED and AE is parallel to CD.

Given that  $\overrightarrow{AB} = \overline{x}$ ,  $\overrightarrow{ED} = 4x$ , FE = y, AF = 2y and BC = 10 m.

(a) Express y in terms of x.

[2]



(b) Show that the area, S, of the cross-sectional plan of the spectator stand is given by

$$S = \frac{9}{2} x \sqrt{100 - 9x^2} \; .$$

[3]

(c) Given that x varies, find the stationary value of S.

[5]

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(d) Hence, determine whether it is a maximum or minimum value.

[1]





- 10. A particle moves in a straight line such that its velocity, v m/s, is given by  $v = 9\sin\left(\frac{t}{2}\right)$ , where t is the time in seconds after passing a fixed point O.
  - (a) Find the value of t for which the particle is at its first instantaneous rest after leaving O.

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(b) Find the value of t for which the particle is at its first maximum velocity.

[2]



(c) Calculate the distance travelled by the particle in the first 10 seconds.

[4]



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(d) Find the time that the particle passes through the point O again.

[3]



Sec 4 Exp AM Prelim Exam Paper 2 Marking Scheme

	p AM Prelim Exam Paper 2 Marking Scheme		
1(a)	$y = 2x^2 - 4x + 7$	and the second s	
	$=2(x^2-2x+7/2)$	[M1]	
	$= 2[x^2 - 2x + (-1)^2 + 7/2 - (-1)^2]$	[M1]	
	$=2[(x-1)^2+5/2]$	Bernaldon in the Control of the Cont	
AL	$=2(x-1)^2+5$	[A1]	
MOIN	<u> </u>		
1(b)	$2(x-1)^2 \ge 0$		
	$2(x-1)^2 + 5 > 0$	[M1]	
	=> y >0		
	Therefore, curve lies completely above the x-axis.	[A1]	
Qn 1	(a) $y = 2(x-1)^2 + 5$		
2(a)	$I = \frac{a}{b + 2^{20 - t}}$ When $t = 16$ , $I = 3600$ $3600 = \frac{a}{b + 2^4}$		
	$3600b + 57600 = a \tag{1}$	[M1]	
	When $t = 20$ , $I = 9000$		
	$9000 = \frac{a}{b+1}$		
11	$9000b + 9000 = a \tag{2}$	[M2]	
AL	sub (1) into (2)	[M2]	
CATTLE	9000b + 9000 = 3600b + 57600	Er	
	5400b = 48600 b = 9		
	a = 90000	[A1]	

	2(b)	90000	
AAAAAAAAAAA	_(-,	$\frac{90000}{9+2^{20-t}} = 100$	[M1]
		$90000 = 900 + 100(2^{20-t})$	
		$89100 = 100(2^{20-t})$	
		$891 = 2^{20-t}$	
		$\lg 891 = (20 - t) \lg 2$	
		$t = 20 - \frac{\lg 891}{\lg 2}$	[M1]
	AL	lg 2	Mi
MAR	107	t = 10.2007	TICAL
D - 110	77.7	=> n = 11	[A1]
DAN	2(c)	$t \to \infty, \ 2^{20-t} \to 0$	[LIL]
		$\Rightarrow I \rightarrow \frac{90000}{9} = 10000$	[A1]
		$31 \rightarrow \frac{1}{9} = 10000$	
	Qn 2	(b) $n = 11$ (c) $I \rightarrow 10000$	
	2(0)		4
	3(a)	$\sin 75^0 = \sin (30^0 + 45^0)$	[M1]
		$= \sin 30 \cos 45 + \cos 30 \sin 45$	
		$= \sin 30 \cos 45 + \cos 30 \sin 45$ $= \frac{1}{2} \left( \frac{1}{\sqrt{2}} \right) + \frac{\sqrt{3}}{2} \left( \frac{1}{\sqrt{2}} \right)$ $= \frac{1 + \sqrt{3}}{\sqrt{2}} \times \frac{\sqrt{2}}{\sqrt{2}}$	[M1]
		$\frac{2(\sqrt{2})}{2(\sqrt{2})}$	
		$=\frac{1+\sqrt{3}}{2\sqrt{2}}\times\frac{\sqrt{2}}{\sqrt{2}}$	
		$=\frac{\sqrt{2}+\sqrt{6}}{\sqrt{6}}$	[A 1]
		4	[A1]
	3(b)	$h(t) = -4\cos bt + 12$	
		$Period = \frac{2\pi}{L}$	1
	JAI	Period = 12	OAL
	7		DE
		$\frac{2\pi}{b} = 12$ $\Rightarrow b = \frac{\pi}{6}$	[M1]
		$\pi$	
		=> 6 = -6	[A1]
			L

3(c)		Curve[2] axes/ label [1]
	h(t)	
- N	20	MARI
DANYAL	10	ANYAL
EDC		To control to a significant and a significant an
	0 2 4 6 8 10 12 14 16 18 t	
4(a)	$\frac{d}{dx}\left(\frac{\ln x}{x^4}\right) = \frac{x^4\left(\frac{1}{x}\right) - (\ln x)(4x^3)}{x^8}$ $= \frac{x^3 - 4x^3 \ln x}{x^8}$	M1
	$=\frac{x^3-4x^3\ln x}{x^8}$	M1
	$=\frac{1-4\ln x}{x^5}$ $1  4\ln x$	A.1
4/5	$=\frac{1}{x^5} - \frac{4\ln x}{x^5}$	A1 M1
DANYA MIC	$\int \left(\frac{1}{x^5} - \frac{4 \ln x}{x^5}\right) dx = \frac{\ln x}{x^4} + c$	M1 ATTOM
EDUCAL	$\int \left(\frac{1}{x^5} - \frac{4\ln x}{x^5}\right) dx = \frac{\ln x}{x^4} + c$ $\int \frac{1}{x^5} dx - \int \frac{4\ln x}{x^5} dx = \frac{\ln x}{x^4} + c$ $\int \frac{4\ln x}{x^5} dx = \int \frac{1}{x^5} dx - \frac{\ln x}{x^4} + c$	M1
	$\int \frac{4 \ln x}{x^5} dx = \int \frac{1}{x^5} dx - \frac{\ln x}{x^4} + c$ $\int \frac{\ln x}{x^5} dx = -\frac{1}{16x^4} - \frac{\ln x}{4x^4} + c$	A1

4(c)	$\int f'(x) dx = \int \frac{\ln x}{x^5} dx$ $f(x) = -\frac{1}{16x^4} - \frac{\ln x}{4x^4} + c$		MI
1 1	$f(x) = -\frac{1}{16x^4} - \frac{1}{4x^4} + c$ $\operatorname{sub}\left(1, \frac{3}{4}\right) \text{ into } f(x),$		M1
P	$\frac{3}{4} = -\frac{1}{16} + c$ $c = \frac{13}{16}$		M1 A1
TIIO.	$\therefore f(x) = \frac{1}{16x^4} - \frac{\ln x}{4x^4} + \frac{13}{16}$		A1
Qns 4	(b) $\frac{1}{16x^4} - \frac{\ln x}{4x^4} + c$	(c) $f(x) = \frac{1}{16x^4} - \frac{\ln x}{4x^4} + \frac{11}{16}$	
5(a)	$y = -x^2 + 5x - 4$ $dy$		
	$\frac{dy}{dx} = -2x + 5$		
	$ let \frac{dy}{dx} = 2, $	LAN	M1
	then, $x = \frac{3}{2}$ and $y = \frac{5}{4}$	so, $P\left(\frac{3}{2}, \frac{5}{4}\right)$	A1
	$\int \frac{dy}{dx} = -2$		
	then, $x = \frac{7}{2}$ and $y = \frac{5}{4}$	so, $Q\left(\frac{7}{2}, \frac{5}{4}\right)$	A1
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5(b)	equation of $l_1$ is	$y - \frac{5}{4} = 2\left(x - \frac{3}{2}\right)$		
		$y = 2x - \frac{7}{4}$		
	equation of $l_2$ is	$y - \frac{5}{4} = -2\left(x - \frac{7}{2}\right)$		
N	$2x - \frac{7}{4} = -2x + \frac{33}{4}$ $4x = 10$	$y = -2x + \frac{33}{4}$		MYAL
TION	$2x - \frac{7}{4} = -2x + \frac{33}{4}$		DE	M1
	4x = 10		201	
n dele accepto del constante d	$x = \frac{5}{2}$ and $y = \frac{13}{4}$			
	$\therefore R\left(\frac{5}{2},\frac{13}{4}\right)$		- Canada e principal de la constante de la con	A1
5(c)	Shaded area = 2×	$\left[\frac{1}{2}\left(\frac{5}{4} + \frac{13}{4}\right)(1) - \int_{\frac{3}{2}}^{\frac{5}{2}} \left(-x^2 + 5x - 4\right) dx\right]$		M2
	= 2×	$\left[\frac{9}{4} - \left[\frac{-x^3}{3} + \frac{5x^2}{2} - 4x\right]_{\frac{3}{2}}^{\frac{5}{2}}\right]$		M1
	= 2×	$\left\lceil \frac{9}{4} - \left\lceil \frac{5}{12} - \left( -\frac{3}{2} \right) \right\rceil \right\rceil$		
	$=\frac{2}{3}$	units <sup>2</sup>		A1
Qns 5	(b) $R\left(\frac{5}{2}, \frac{13}{4}\right)$	(c) $\frac{2}{3}$ units <sup>2</sup>		
6(a)	$5x^2 + 12x > 3x + 2$			[M1]
ADT	$5x^{2} + 9x - 2 > 0$ $(5x - 1)(x + 2) > 0$ $x < -2 \text{ or } x > \frac{1}{5}$			Dr. William
770	(5x-1)(x+2) > 0			[M1]
1	$x < -2$ or $x > \frac{1}{5}$			[A1]
	Andrews and the second and the secon			
			1	
	RECORDANGE OF THE PROPERTY OF			

	6(bi)	y = mx + c   (1)	
		$x^2 + y^2 = 8   (2)$	
		Sub (1) into (2),	
		$x^2 + (mx + c)^2 = 8$	
		$x^2 + m^2 x^2 + 2mcx + c^2 - 8 = 0$	F) 643
		$(1+m^2)x^2 + 2mcx + c^2 - 8 = 0$	[M1]
	W	Does not intersect => D=0	Bir
NE	11	Does not intersect -> D-0	CATI
	TIO.	$(2mc)^2 - 4(1+m^2)(c^2-8) < 0$	[M1]
		$4m^2c^2 - 4(c^2 - 8 + m^2c^2 - 8m^2) < 0$	
		$4m^2c^2 - 4c^2 + 32 - 4m^2c^2 + 32m^2 < 0$	[M1]
		$32m^2 - 4c^2 + 32 < 0$	
		$8m^2 + 8 < c^2$	[A1]
	6(bii)	y = 2x + 5	
		m=2, c=5	
		174	
		$8m^2 + 8 = 8(2)^2 + 8 = 40$	[M1]
		$c^2 = 25$	
		Since $8m^2 + 8$ is not $< c^2$ , $y = 2x + 5$ intersect the curve.	[A1]
	Qn 6	(a) $x < -2$ or $x > \frac{1}{5}$	
		3	
		(b) The line intersect the curve.	
	7(a)	$x^{2} + 2x + 1 + y^{2} - 8y + (-4)^{2} = 8 + 1 + 16$	
		$(x+1)^2 + (y-4)^2 = 25$	DB
	777	Centre $C(-1,4)$	[M1] [A1]
	Cyrr	Radius = 5 units	[A1]

DANYA		Grad of CP = -4  Grad of tangent at P = $\frac{1}{4}$ $y = \frac{1}{4}x + c$	[M1]
		$y = \frac{1}{4}x + c$	
A			` I
N.P.		(-2,8)	
NP.	4	$8 = \frac{1}{4}(-2) + c$	[M1]
10	37	$c = \frac{17}{1}$	TANTON
DAL	100	2 1 17	OUCA
EDUC		$y = \frac{1}{4}x + \frac{1}{2}$	[A1]
	/(c)	Centre = $(-1, -2)$ Radius = 5	[M1]
		Equation: $(x+1)^2 + (y+2)^2 = 25$	[A1]
7(	7(d)	Diameter is the diagonal of the biggest square that can be drawn inside the circle.	[M1]
		Let $x$ – side of the square. $x^2 + x^2 = 10^2$ $2x^2 = 100 \Rightarrow x = \sqrt{50}$ Area = $\sqrt{50} \times \sqrt{50} = 50$ units <sup>2</sup>	[A1]
Qı	Qn 7	(a) Centre $C(-1, 4)$ (b) $y = \frac{1}{4}x + \frac{17}{2}$ Radius = 5 units	
		(c) $(x+1)^2 + (y+2)^2 = 25$ (d) 50 units <sup>2</sup>	TAI
8(	8(a)	$\frac{8x^3 + 3x + 1}{x(2x+1)^2} = \frac{8x^3 + 3x + 1}{4x^3 + 4x^2 + x} = 2 + \frac{1 + x - 8x^2}{4x^3 + 4x^2 + x}$	B1 ATTO
DANY	~10	2(22+1)	DUCK

8(b)	so, $\frac{1+x-8x^2}{x(2x+1)^2} = \frac{A}{x} + \frac{B}{2x+1} + \frac{C}{(2x+1)^2}$	M1
	$1 + x - 8x^{2} = A(2x+1)^{2} + Bx(2x+1) + Cx$	
	let x = 0,   1 = A	
	$let x = -\frac{1}{2},  -\frac{3}{2} = -\frac{C}{2}$	
		M3
NU	C = 3 let $x = 1$ , $-6 = 9A + 3B + C$	IVIS
Th	-6 = 9 + 3B + 3	J. D. D.
TIO,	B = -6	DUCE
	$\therefore \frac{8x^3 + 3x + 1}{x(2x+1)^2} = 2 + \frac{1}{x} - \frac{6}{2x+1} + \frac{3}{(2x+1)^2}$	A1
0(0)	$\int_{1}^{3} \frac{8x^{3} + 3x + 1}{x(2x+1)^{2}} dx = \int_{1}^{3} \left(2 + \frac{1}{x} - \frac{6}{2x+1} + \frac{3}{(2x+1)^{2}}\right) dx$	M1
	$= \left[2x + \ln x - 3\ln(2x+1) - \frac{3}{2(2x+1)}\right]^3$	M1
	= 1.046596 + 1.795836	M1
	= 2.8424	
	= 2.84 (3  s.f.)	A1
Qns 8	(a) $2 + \frac{1+x-8x^2}{4x^3+4x^2+x}$ (b) $2 + \frac{1}{x} - \frac{6}{2x+1} + \frac{3}{(2x+1)^2}$	
	(c) 2.84	
9(a)	$10^2 = (2y)^2 + (3x)^2$	M1
	$100 = 4y^2 + 9x^2$	
	$y = \sqrt{\frac{100 - 9x^2}{4}}$	-
JAJ	$y = \sqrt{\frac{4}{4}}$	A1
9(b)	$S = \frac{1}{2} (5x)(2y) + 4xy$	M1
	=9xy	
	$=9x\left(\sqrt{\frac{100-9x^2}{4}}\right)$	M1
	$=\frac{9}{2}x\sqrt{100-9x^2}$ (shown)	

	9(c)	$\frac{dS}{dx} = \frac{9}{2} \left( 100 - 9x^2 \right)^{\frac{1}{2}} + \frac{9}{2} x \left( \frac{1}{2} \right) \left( 100 - 9x^2 \right)^{-\frac{1}{2}} \left( -18x \right)$	M1	
		$= \frac{9}{2} \left( 100 - 9x^2 \right)^{\frac{1}{2}} - \frac{81x^2}{2} \left( 100 - 9x^2 \right)^{-\frac{1}{2}}$		
		$= \frac{9}{2} \left( 100 - 9x^2 \right)^{-\frac{1}{2}} \left[ \left( 100 - 9x^2 \right) - 9x^2 \right]$	M1	
DAN	AL	$=\frac{9(100-18x^2)}{2(100-9x^2)^{\frac{1}{2}}}$	DUCATI	
DAM	TION	$=\frac{9(50-9x^2)^2}{1}$	DUCATI	
EDUC		$=\frac{1}{(100-9x^2)^{\frac{1}{2}}}$	M1	
		let $\frac{dS}{dx} = 0$ ,		
		$\frac{9(50-9x^2)}{(100-9x^2)^{\frac{1}{2}}} = 0$	M1	
		$(100 - 9x^2)^{\frac{1}{2}}$ $50 - 9x^2 = 0$		
		$x^2 = \frac{50}{9}$		
		x = 2.357 or $x = -2.357$ (rej) $\therefore$ stationary value of $S = 74.99999 = 75.0$ m <sup>2</sup> (3s.f.)	A1	
-	9(d)			
		$\frac{dS}{dx} = \frac{9(50 - 9x^2)}{(100 - 9x^2)^{\frac{1}{2}}}$		J.
	JAI	let $x = 2$ , $\frac{dS}{dx} = \frac{63}{4} > 0$ , function is increasing.	DAN	YAL
DAN	ATTO	let $x = 2$ , $\frac{dS}{dx} = \frac{63}{4} > 0$ , function is increasing. let $x = 2.5$ , $\frac{dS}{dx} = -8.504 < 0$ , function is decreasing.	B1 EDU	Ch
EDU	Qns 9	$\therefore$ by first derivative test, $S = 75.0$ is maximum value.		
	N-35	(a) $y = \sqrt{\frac{100 - 9x^2}{4}}$ (c) 75.0 (d) maximum value		
			dela	

10(a)	$9\sin\left(\frac{t}{2}\right) = 0$	M1	
	$\sin\left(\frac{t}{2}\right) = 0$ basic angle = 0 rad so, $\frac{t}{2} = 0$ , $\pi$ $t = 0$ , $2\pi$	M1	
AL	$\therefore t = 2\pi \sec$	A1	
10(b)	Maximum velocity when $\sin\left(\frac{t}{2}\right) = 1$ .	M1	
	$\frac{t}{2} = \frac{\pi}{2}$ $t = \pi \sec$	A1	
10(c)	$s = \int 9\sin\frac{t}{2} dx$		
	$s = 9 \left( \frac{-\cos \frac{t}{2}}{\frac{1}{2}} \right) + c$ $s = -18\cos \frac{t}{2} + c$ when $t = 0$ , $s = 0$ , $c = 18$	M1	
	hence, $s = -18\cos\frac{t}{2} + 18$ when $t = 2\pi$ , $s = -18\cos\pi + 18$ s = 36  m	-1	
MAJ	when $t = 10$ , $s = -18\cos 5 + 18$ s = 12.894  m	M1	
Ch	Dist. travelled in first 10 sec $= 36 + (36 - 12.894)$		
	= 59.1059	M1	
	= 59.1 m (3 s.f.)	A1	

	10(d)	$s = -18\cos\frac{t}{2} + 18$		
		let s = 0,		
		$-18\cos\frac{t}{2} + 18 = 0$		M1
		$\cos\frac{t}{2} = 1$		- 100
-1	W	basic angle = 0		Mi
AN	MON	$\frac{t}{2} = 0 \text{ (rej)}, \qquad 2\pi$		M1
200		$\therefore t = 4\pi$	T. Control of the con	A1
	Qns 10	(a) $t = 2\pi$ sec (b) $t = \pi$ sec	(c) 59.1 m	
		(d) $t = 4\pi$		

DANYAL

Sec 4 Exp AM Prelim Exam Paper 1 Marking Scheme

	p Alvi Frenin Exam Faper 1 Warking Scheme	
1(a)	(x+3)(x-1)	
	f(1) = 0 1 + 4 + 2 + a - b = 0 a - b = -7(1)	[M1]
AL	$f(-3) = 0$ $(-3)^4 + 4(-3)^3 + 2(-3)^2 + a(-3) - b = 0$ $81 - 108 + 18 - 3a - b = 0$ $-3a - b = 9(2)$	[M1]
TIO.	a = -4	[A1]
	b = 3	[A1]
1(b)	Long division	
	$   \begin{array}{r}                                     $	[M1]
	$   \begin{array}{r}                                     $	
YAL	$f(x) = (x^2 + 2x - 3)(x^2 + 2x + 1)$ Other factor is $x^2 + 2x + 1$ .	[A1]
14/11		

2(a)	Let the perpendicular distance be x.	in a constant of the constant	
	$\frac{1}{2}\left(4\sqrt{2}+8\right)x=18$		[M1]
	$\left(4\sqrt{2}+8\right)x = 36$		
1	$x = \frac{36}{8 + 4\sqrt{2}}$ 36  8 - 4\sqrt{2}		MAL
IBE	$= \frac{36}{8+4\sqrt{2}} \times \frac{8-4\sqrt{2}}{8+4\sqrt{2}}$		[M1]
ATTO	$=\frac{288-144\sqrt{2}}{64-32}$		DOC
	$=9-\frac{9}{2}\left(\sqrt{2}\right)cm$		[A1]
2(b)	$\sin 45^\circ = \frac{x}{PS}$		
	$\frac{1}{1} - \frac{9 - \frac{9}{2}\sqrt{2}}{1}$		[M1]
	$PS = \sqrt{2} \left( 9 - \frac{9}{2} \sqrt{2} \right)$ $= 9\sqrt{2} - \frac{9}{2}(2)$ $= -9 + 9\sqrt{2}$		
			[A1]
Qn 2	(a) $9 - \frac{9}{2}(\sqrt{2}) cm$ (b) $PS = -9 + 9\sqrt{2}$ cm		
1		de la companya de proposition de la companya de la	DANYAL

	3(a)	$\frac{dy}{dx} = \frac{1}{2}e^{2x}(2) - \frac{1}{3}e^{-3x}(-3)$	[M1]
		$=e^{2x}+\frac{1}{e^{3x}}$	
		$=\frac{e^{2x}\left(e^{3x}\right)+1}{e^{3x}}$	
	N		[M1]
	TION		[M1]
	3(b)		
		at $P$ , $\frac{dy}{dx} = \frac{e^{5\ln 2} + 1}{e^{3\ln 2}} = \frac{33}{8}$	
		$\therefore \text{ gradient of normal} = -\frac{8}{33}$	[M1]
		$y - \frac{1}{24} = -\frac{1}{33}(x - \ln 2)$ $y = -\frac{8}{33}x + \frac{8}{31}\ln 2 + \frac{55}{33}$	[M1]
		equation of normal is $y - \frac{55}{24} = -\frac{8}{33}(x - \ln 2)$ $y = -\frac{8}{33}x + \frac{8}{33}\ln 2 + \frac{55}{24}$	[A1]
	3(c)	$Q\left(0, \frac{8}{33}\ln 2 + \frac{55}{24}\right)$ (b) $y = -\frac{8}{33}x + \frac{8}{33}\ln 2 + \frac{55}{24}$ (c) $Q\left(0, \frac{8}{33}\ln 2 + \frac{55}{24}\right)$	[A1]
	Qn 3	(b) $y = -\frac{8}{33}x + \frac{8}{33}\ln 2 + \frac{55}{24}$ (c) $Q\left(0, \frac{8}{33}\ln 2 + \frac{55}{24}\right)$	DANYAL
DAN	CATIO	N. C.	EDUCATIO
EDU			

4(a)	du	[M1]
+(a)	$\frac{dy}{dx} = 6x^2 - 18x$	
	let $\frac{dy}{dx} = 0$ ,	
	$6x^2 - 18x = 0$	[M1]
	6x(x-3)=0	
	x = 0   or   x = 3 y = 13   y = -14	-T D
W	$y = 13 \qquad \qquad y = -14$	Bir
7.	(0,13) and $(3,-14)$	[A2]
TIO.		OUC
4(b)	$d^2v$	
	$\frac{d^2y}{dx^2} = 12x - 18$	[M1]
	at $x = 0$ , $\frac{d^2y}{dx^2} = -18 < 0$	
California de Ca		E 4 1 7
	(0,13) is maximum point.	[A1]
	at $x = 3$ , $\frac{d^2y}{dx^2} = 18 > 0$	
	$\therefore$ (3,-14) is minimum point.	[A1]
	(2, 2.) 20	[]
	DUCAT	
Qn 4	(a) $(0, 13)$ and $(3, -14)$ (b) $(0, 13)$ max point; $(3, -14)$ min point.	



4	5(a)	$\frac{d}{dx}(2x\cos 2x) = 2x(-\sin 2x)(2) + 2\cos 2x$ $= 2\cos 2x - 4x\sin 2x$	[M1] [A1]
5	5(b)	$\int (2\cos 2x - 4x\sin 2x) dx = 2x\cos 2x + c$	
X	T	$\int 2\cos 2x  dx - \int 4x \sin 2x  dx = 2x \cos 2x + c$ $\int 4x \sin 2x  dx = \int 2\cos 2x  dx - 2x \cos 2x + c$	[M1]
DANY	TON	$= 2\left(\frac{\sin 2x}{2}\right) - 2x\cos 2x + c$ $= \sin 2x - 2x\cos 2x + c$	[M1]
-		so,	
		$\int_0^{\frac{\pi}{2}} (1 - 4x \sin 2x)  dx = \left[ x - \sin 2x + 2x \cos 2x \right]_0^{\frac{\pi}{2}}$	[M1]
		$=\frac{\pi}{2}-\pi$	[M1]
		$=-\frac{\pi}{2}$	[A1]
L		DALTION	

[	6(a)	$dy$ (2) $2(2-5)^2(2)$ (2 $5)^3$		
		$\frac{dy}{dx} = (x-2) \times 3(2x-5)^{2}(2) + (2x-5)^{3}$	[M1]	
		$= (2x-5)^2 [6x-12+2x-5]$		
		$=(2x-5)^2(8x-17)$	[A1]	
	6(b)	$\frac{dy}{dx} < 0$ , so $(2x-5)^2 (8x-17) < 0$		
	. 1.	since $(2x-5)^2 > 0$ for all values of x,	NA	
1	(AV	then $(8x-17) < 0$ .	[M1]	
DAL	TOID	8x - 17 < 0	OUCA,	
EDUC		$x < \frac{17}{8}$	[A1]	
	6(c)	$\frac{dy}{dt} = \frac{dy}{dx} \times \frac{dx}{dt}$		
		$0.35 = (2x - 5)^{2} (8x - 17) \times \frac{dx}{dt}$	[M1]	
		when $x = 3$ ,	A A A A A A A A A A A A A A A A A A A	
		$0.35 = 7 \times \frac{dx}{dt}$		
		$\frac{dx}{dt} = 0.35 \div 7 = 0.05 \text{ units/s}^2$	[A1]	
	6(d)	$z = y^2$	And a second sec	
		$\frac{dz}{dy} = 2y$		
		$\frac{dz}{dt} = \frac{dz}{dy} \times \frac{dy}{dt}$		
			FB 617	
	4	$=2y\times\frac{dy}{dt}$	[MI]	
1	AD	$=2y \times \frac{dy}{dt}$ $=2(x-2)(2x-5)^{3} \times \frac{dy}{dt}$	DE	
	ATTE	when $x = 3$ ,	EDC	
DAN				
		$=2\frac{dy}{dt}$	[A1]	
	Qn 6	(a) $(2x-5)^2(8x-23)$ (b) $x < \frac{23}{8}$ (c) 0.05 units/s <sup>2</sup>		

	7(a)	$\sqrt{125^x} = \frac{5^{1-x}}{2}$	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,
		$\sqrt{125^x} = \frac{5^{1-x}}{25}$ $\sqrt{5^{3x}} = \frac{5^{1-x}}{5^2}$	[M1]
DANY		$5^{\frac{3}{2}x} = 5^{1-x-2}$ $= > \frac{3}{2}x = -x - 1$ $x = -\frac{2}{5}$	[M1]
DAM		$=>\frac{3}{2}x=-x-1$	TUCAT
EDUC		$x = -\frac{2}{5}$	[A1]
		$\therefore \sqrt{125^x} = 0.3807 = 0.381  (3s.f)$	[A1]
	7(b)	$\log_2 x - \log_{16} x$	
		$= \log_2 x - \frac{\log_2 x}{\log_{16} x}$	[M1]
		2	[M1]
		$=\log_2 x - \log_2 x^{\frac{1}{4}}$	
		$= \log_2 x^{\frac{3}{4}}$	[A1]
		$= \frac{3}{4} \log_2 x$	
		$= \frac{3}{4} \left( \frac{\lg x}{\lg 2} \right) = \frac{3 \lg x}{4 \lg 2}$	[M1]
DAN	Qn 7	(a) 0.381	OA
NA	V E	N .	DE

	8(a)	$T_{r+1} = {}^{12}C_r \left(2x\right)^{12-r} \left(\frac{1}{2x^3}\right)^r$	[B1]
	8(b)	12-r(1)	
		$T_{r+1} = {}^{12}C_r (2x)^{12-r} \left(\frac{1}{2x^3}\right)^r$	[MO]
	N	$= {}^{12}C_r(2)^{12-r-r}(x)^{12-4r}$	[M2]
DAN	TION	Term with $x^4$ : $12-4r = 4$ r = 2	[M1]
		Coef. of $x^4 = {}^{12}C_2(2)^8 = 16896$	K
		Term with $x^0$ : $12-4r=0$ r=3	[M1]
		Coef. of $x^0 = {}^{12}C_3(2)^6 = 14080$	
		Term independent of $x = 1(16896) + (-1)(14080)$	
		= 2816	[A1]
	8(c)	$n = 12 - 4r$ 4r is even => $n = 12 - 4r$ is even.  Therefore, there are no terms containing $x^n$ whereby $n$ is odd.	[M1] [A1]
	Qn 8	(a) $T_{r+1} = {}^{12}C_r (2x)^{12-r} \left(\frac{1}{2x^3}\right)^r$	
		(b) 2816	
	. 1	(c) There are no terms containing $x^n$ whereby $n$ is odd.	1
	10		DP

	9(a)	$LHS = \frac{\sec^2 x}{1 + \sec^2 x}$ $= \frac{1}{1}$		
DANY	AL	$= \frac{1}{\sec^2 x} + 1$ $= \frac{1}{\cos^2 x + 1}$ $= \frac{1}{\frac{\cos 2x + 1}{2} + 1}$ $= \frac{2}{\cos 2x + 3} = RHS$	[M1] [M1] [A1]	
	9(b)	$\frac{\sec^2 2x}{1 + \sec^2 2x} = \frac{4}{7}$ $\frac{2}{\cos 4x + 3} = \frac{4}{7}$	[M1]	
		$14 = 4\cos 4x + 12$ $\cos 4x = \frac{1}{2}$ $ref \angle = \frac{\pi}{3}$ $4x = \frac{\pi}{3}, \frac{5\pi}{3}, \frac{7\pi}{3}, \frac{11\pi}{3}$	[M1]	
		$x = \frac{\pi}{12}, \frac{5\pi}{12}, \frac{7\pi}{12}, \frac{11\pi}{12}$	[A1]	
DAN	9(c)	$-2\pi \le x \le 2\pi \implies -8\pi \le 4x \le 8\pi$ $\therefore \text{ No. of solutions} = 16$	[A1]	
EDU	Qn 9	(b) $\frac{\pi}{12}$ , $\frac{5\pi}{12}$ , $\frac{7\pi}{12}$ , $\frac{11\pi}{12}$ (c) 16 solutions		

10(a)	$\cos \theta = \frac{OB}{A} \implies OB = 4 \cos \theta$	
	$\angle ADO = \theta$	
	$\sin \theta = \frac{OA}{7} \implies OA = 7 \sin \theta$	[M1]
	$\therefore AB = OA + OB = 7\sin\theta + 4\cos\theta$	[A1]
10(b)	$AB = R\sin(\theta + \alpha)$	[M1]
(Br	$R = \sqrt{7^2 + 4^2} = \sqrt{65}$	[MI]
TION	$\alpha = \tan^{-1}\left(\frac{4}{7}\right) = 29.744$	[M1]
	$\therefore AB = \sqrt{65}\sin(\theta + 29.7^{\circ})$	[A1]
10(c)	Max length of AB = $\sqrt{65}$	[A1]
	Max occurs when $\sin(\theta + 29.744^{\circ}) = 1$	
	$\sin(\theta + 29.744^{\circ}) = 1$	
	$ref \angle = 90^{\circ}$	[M1]
	$\theta + 29.744^{\circ} = 90^{\circ}$	
	$\theta = 90^{\circ} - 29.744$	
	$=60.256^{\circ} = 60.3^{\circ} (1dp)$	[A1]
10(4)	[	[M1]
10(d)	$\sqrt{65}\sin(\theta + 29.744^{\circ}) = \sqrt{55}$	[ [MII]
	$\sin(\theta + 29.744^{\circ}) = \frac{\sqrt{55}}{\sqrt{65}}$	
	$ref \angle = 66.906^{\circ}$	[M1]
	$\theta + 29.744^{\circ} = 66.906^{\circ}$	
	$\theta = 66.906^{\circ} - 29.744$	ran - VAL
. 4	$=37.162 = 37.2^{\circ} (1dp)$	[A1]
VA		DE VILO
Qn 10	(b) $AB = \sqrt{65} \sin(\theta + 29.7^{\circ})$	EDUC
CVI	(c) Max AB = $\sqrt{65}$ ; $\theta = 60.3^{\circ}$	- P
	(d) $\theta = 37.2^{\circ}$	

11(a)	$\frac{1}{2}$ $\frac{1}$	
11(a)	3y - 4x + 40 = 0   (1)	
	$4y + x = 48 \tag{2}$	
	From(2): x = 48 - 4y	
	3y - 4(48 - 4y) + 40 = 0	
	19y = 152	111111111111111111111111111111111111111
	$y = 8 \Rightarrow x = 16$	
JAL	P(16,8)	[M1]
ANYAL	1500 ()	[M1]
AT TION	M(8,4)	
DUCE	t when y = 0 x = 10	8
132	$l_2$ : when $y = 0$ , $x = 10$	[M1]
	R(10,0)	[]
	G-1 8 1	1 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
	$Grad_{OP} = \frac{1}{16} = \frac{1}{2}$	
	$Grad_{OP} = \frac{8}{16} = \frac{1}{2}$ $Grad_{MR} = \frac{4 - 0}{8 - 10} = -2$	[M1]
	$Sin ce Grad_{OP} \times Grad_{MR} = -1$	[A1]
Manager and the second	$\Rightarrow$ OP is perpendicular to MR.	
10(b)	$l_2$ : when $x = 0$ , $y = 12$	
	Q(0,12)	[M1]
	Area of $ORPQ = \frac{1}{2} \begin{vmatrix} 0 & 10 & 16 & 0 & 0 \\ 0 & 0 & 8 & 12 & 0 \end{vmatrix}$	[M1]
	Area by $0.10 \ 0.2 \ 0.2 \ 0.3 \ 0$	
	$=\frac{1}{2}[(80+192)-(0)]$	
	. 2	- T N
. 1	= 136 units <sup>2</sup>	[A1]
0-11	(b) 136 units <sup>2</sup>	DB ATT
Qn 11	(b) 130 utilits	COU
CAL		

	12(a)		1	T 2		1.4	- C		Lagaritation of the Control of the C	
		ln y	0.64	0.83	1.04	1.24	5 1.44			
		Table of val		0.05	1.0.	1.201	1 4.1.,			
		Plot points	[1]							
		Smooth Cui	rve [1]							
	10(b)	$y = ae^{bx-1}$							N A	
		$ \ln y = \ln a + \ln e^{bx-1} $							Mr. OH	
EDUC	400	$ \ln y = (bx - bx) $							[M1]	
		$ \ln y = bx +  $								
		gradient =								
		vertical in	tercept = ln a	-1						
		From the gr	raph,							
		$\ln a - 1 = 0$								
		$\ln a = 1.43$								
		$a=e^{1.43}$								
	121	=4.17	86 = 4.18 (3s.	f)					[A1]	
		$Grad = \frac{1.5}{4}$	$\frac{34 - 0.54}{4.5 - 0.5} = 0.$	2						
		$\therefore b = 0.2$							[A1]	
	11(c)	$2.46 = ae^{b}$	x-1						FN (17	
			$> \ln y = 0.9$						[M1]	
		From grap	oh, when ln y						F 4 1 2	
			ز	x = 2.3					[AI]	
DAN	Qn 11	(b) $a = 4.18$	b = 0.2	(c) $x = 2.3$					[A1]	
CAD	mi(	14							EDU	