

BEDOK VIEW SECONDARY SCHOOL END-OF-YEAR EXAMINATION 2018

CANDIDATE NAME		
REGISTER NUMBER	CLASS	

MATHEMATICS SYLLABUS A Secondary 2 Normal Academic

4045/01 4 October 2018 1 hour 15 minutes

Paper 1

Candidates answer on the Question Paper.

READ THESE INSTRUCTIONS FIRST

Write your index number and name on all the work you hand in. Write in dark blue or black pen. You may use a pencil for any diagrams or graphs. Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer all questions.

The number of marks is given in brackets [] at the end of each question or part question.

If working is needed for any question it must be shown with the answer. Omission of essential working will result in loss of marks. The total of the marks for this paper is 50.

The use of an approved scientific calculator is expected, where appropriate. If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For π , use either your calculator value or 3.142.

Total

Setter: Ms Beevi

Parent's / Guardian's Signature:

This document consists of 10 printed pages.

Do not turn over the page until you are told to do so.

Mathematical Formulae

Compound Interest

Total amount =
$$P\left(1 + \frac{r}{100}\right)^n$$

Mensuration

Curved surface area of a cone = $\pi r l$

Surface area of a sphere = $4\pi r^2$

Volume of a cone = $\frac{1}{3}\pi r^2 h$

Volume of a sphere = $\frac{4}{3}\pi r^3$

Area of triangle
$$ABC = \frac{1}{2}ab\sin C$$

Arc length = $r\theta$, where θ is in radians

Sector area = $\frac{1}{2}r^2\theta$, where θ is in radians

 $\frac{b}{\sin B}$

 $a^2 = b^2 + c^2 - 2bc\cos A$

 $=\frac{c}{-in C}$

Mean =
$$\frac{\sum fx}{\sum f}$$

Standard Deviation =
$$\sqrt{\frac{\sum fx^2}{\sum f} - \left(\frac{\sum fx}{\sum f}\right)^2}$$

Statistics

Answer all the questions.

1 (a) Expand and simplify $x^2 - (x+2)^2$.

(b) Factorise $2y^2 - 9y - 5$.



2 (a) Simplify $\frac{2x+4}{x^2+5x+6}$.

Answer (a)[3]

(b) Simplify
$$\frac{24(x+y)}{8x^2} \div \frac{(x^2-y^2)}{3x}$$
.

3 Triangle *ABE* is similar to triangle *ACD*. AB = 14 cm, BC = 8 cm, ED = 6 cm and AE = x cm.



Find the value of x.



4 A shopping centre carried out a survey to find out the colour preference of the shoppers. The table below shows the results of the survey.

Colour preference	Number of shoppers	
Yellow	40	
Blue	20	
Red	30	
Green	10	



Find

(a) the probability that the shoppers chose blue,

Answer (a) [1]

(b) the probability that the shoppers did not choose green.

Answer (b) [2]

- 5 The variables x and y are connected by the equation y = 2 2x. The table below shows some corresponding values of x and y.
 - (a) Complete the following table for y = 2-2x.

Answer (a)

x	-2	-1	0	1	2	3	
у	6		2	0		-4	[2]

(b) Using the axes provided below, draw the graph of y = 2 - 2x for $-2 \le x \le 3$.



(c) Find the gradient of the line.

[1]

- (d) On the grid provided above, draw the line x = -2.
- (e) Calculate the area of the triangle enclosed by the lines x = -2, y = 2 2x and the x-axis.

Answer (e) [2]

- 6 Given that y is directly proportional to x^2 and y = 14 when x = 2,
 - (a) express y in terms of x,

Answer (a) $y = \dots$ [2]

(b) find the value of y when x = 3,



Answer (b) $y = \dots$ [2] y when x changes from 2 to 3.

(c) hence, find the percentage change in y when x changes from 2 to 3.

7 (a) Construct triangle *DEF*, given that *DE* = 8 cm, *DF* = 10 cm and *EF* = 6 cm. The line *DF* has been drawn for you.
[2] Answer (a), (b) and (c)



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(b) Using a ruler and a compass, construct

(i) the perpendicular bisector of line DF ,	[1]
(ii) the angle bisector of angle <i>EFD</i> .	[1]

(c) Mark clearly the point of intersection of (b)(i) and (b)(ii). Label the point as G. [1]

(d) Measure the length of FG.

8 Express each of the following as a single fraction in its simplest form.

(a)
$$2-\frac{2x-5}{2}$$



Answer (b)[2]

9 Given that $\frac{2p+q}{3q-4p} = \frac{5}{8}$, find the value of $\frac{p}{q}$.

10 (a) Expand (x-3)(x+3).





(b) Hence, without the use of calculator, find the value of 397 × 403. Show your working clearly.

11 The first four terms of a sequence are shown below.

$$3+9=3\times 2^{2}=12$$

$$3+9+15=3\times 3^{2}=27$$

$$3+9+15+21=3\times 4^{2}=48$$

(a) Write down the 4th line of the pattern.



(b) A given line of the sequence is as follows:

 $3 + 9 + 15 + 21 + 27 + \dots + x = 3 \times y^2 = 507$

Find the value of *x* and of *y*.



Answer (b) $x = \dots$,

END OF PAPER



BEDOK VIEW SECONDARY SCHOOL **END-OF-YEAR EXAMINATION 2018**

CANDIDATE NAME	
REGISTER NUMBER	CLASS
	1.

MATHEMATICS SYLLABUS A

Secondary 2 Normal Academic

4045/02 8 October 2018 1 hour 30 minutes

Paper 2

Additional Materials: Answer Paper

READ THESE INSTRUCTIONS FIRST

Write your answers and working on the separate Answer Paper provided. Write your index number and name on all the work you hand in. Write in dark blue or black pen. You may use a pencil for any diagrams or graphs. Do not use staples, paper clips, highlighters, glue or correction fluid.

The number of marks is given in brackets [3] at the end of each question or part question. The total number of marks for this paper is 50.

The use of a scientific calculator is expected, where appropriate. If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place. ANYAL For π , use either your calculator value or 3.142.

At the end of the examination, fasten all your work securely together.

Setter: Ms Beevi

Parent's / Guardian's Signature:

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Mathematical Formulae

Compound Interest

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$$P\left(1 + \frac{r}{100}\right)^{n}$$

Mensuration

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Area of triangle
$$ABC = \frac{1}{2}ab\sin C$$

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Trigonometry

Mean =
$$\frac{\sum fx}{\sum f}$$

Standard Deviation =
$$\sqrt{\frac{\sum fx^2}{\sum f} - \left(\frac{\sum fx}{\sum f}\right)^2}$$



$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc\cos A$$

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Statistics

3

Answer all the questions.

1 The figure below shows Triangle *ABC* and Quadrilateral *DEFG* with the respective angles.



2

3

- 4 A florist sells a bouquet of flowers at \$25 each. If the florist wants to have total sales of at least \$520 for a particular day, she needs to sell x bouquet of flowers.
 - (a) Using the above information, form and simplify an inequality for the number of bouquets of flowers she needs to sell.
 - (b) Hence write down the minimum number of bouquets that she needs to sell. [1]

[2]

5 The *Evan Millenium* Mineral bottle shown below can be modelled by attaching a cone to a hemisphere. The height of the cone is 12 cm and the slant height of the cone is 13 cm.

	evan reciliement	[2]
(a)	Find the radius of the model cone.	[2]
(b)	Using your answer in (a), find the estimated total surface area of the Evan	
	Millenium Mineral bottle.	[2]
(c)	Find the estimated volume of the Evan Millenium Mineral bottle.	[2]

6 The data below shows the number of hours spent by 20 students on the internet every day.

			4	3	4	6	4	
			0	2 80	5	0	4	
			1	3	4	4	1	
			4	5	6	3	4	
(a)	Draw	v a dot diagra	am to rep	resent the	e data abo	ove.		[2]
(b)	Find							
	(i)	the modal n	umber of	f hours th	at studen	its spend	on the internet every day,	[1]
	(ii)	the mean nu	umber of	hours that	at student	ts spend o	on the internet every day,	[2]
	(iii)	the percenta	age of stu	idents wh	no did not	t use the	internet,	[1]
	(iv)	the probabi day.	lity that t	he studer	nts spent	more that	n 3 hours on the internet every	[2]

7 If
$$x^2 + y^2 = 14$$
 and $xy = 5$, find the value of $(3x + 3y)^2$. [3]

8 The ArtScience Museum is made up of a base and a flower-like structure consisting of 10 petals. The heights of the petals vary.



Diagram I

Diagram II

(a) On the design drawing as shown in Diagram I, the height of the highest petal is 2.5 cm. The actual height of the highest petal is 60 m as shown in Diagram II.

Find

- (i) the scale of the design drawing in the form 1: n, [1]
- (ii) the height of the petal, in metres, that measures 1.9 cm on the design [2]
- (iii) the area of the petal on the design drawing if its actual area is 1728 m². [3]
- (b) Using the price list below, find the cheapest combination of tickets for a group of 6 adults, 3 senior citizens and 2 children. Explain your answer with clear working.
 [3]

Exhibition	Category	Price
	Adult	\$17
FUTURE WORLD:	Senior Citizen	\$14
Where Art Meets Science	(65 years old and above)	VICAN
LION	Child (2-12 years old)	\$10
	Family (2 Adults + 2 Children)	\$44

(Source: https://www.marinabaysands.com/museum.html. Correct as of Aug 2018)



Triangle *ABC* above has lengths, such that AC = 25 cm, BC = 15 cm and BD = 8 cm.

(a)	Given that $CD = 17$ cm, determine if triangle <i>BCD</i> is a right-angled triangle.	[2]
(b)	Find the length of AB.	[2]
(c)	Find the area of triangle ABC.	[2]
(d)	Find the shortest distance from B to AC .	[2]

END OF PAPER

No.		Working		Remarks
1	(a)	$x^{2} - (x + 2)^{2} = [x - (x + 2)][x + (x + 2)]$ = (x - x - 2)(2x + 2) = -2(2x + 2) = -4x - 4 [A1] OR	[M1] Correct Expansion	
	ĵ.	$x^{2} - (x + 2)^{2} = x^{2} - (x^{2} + 4x + 4)$ [M1] = $x^{2} - x^{2} - 4x - 4$ = $-4x - 4$ [A1]		J.
DAN	(b)	$2y^{2} - 9y - 5 = (2y + 1)(y - 5)$ $2y + 1 + y$ $1y -5 -10y$ $2y^{2} - 5 - 9y$ $2y^{2} - 5 - 9y$ $2y^{2} - 9y - 5 = (2y + 1)(y - 5)$ [A1]	7	EDUCATION
L	1	DANTON		[Total : 4m]

[Total:4m]

2	(a)	$\frac{2x+4}{x^2+5x+6} = \frac{2(x+2)}{(x+3)(x+2)} [M1] \\ = \frac{2}{(x+3)} [A1]$	NYAL
DA	(b)	$\frac{\frac{24(x+y)}{8x^2} \div \frac{(x^2-y^2)}{3x}}{\frac{24(x+y)}{8x^2} \times \frac{3x}{x^2-y^2}}$ [M1] : Change to Multiplication	DA1 EDUCATIO
		$= \frac{24(x+y)}{8x^2} \times \frac{3x}{(x-y)(x+y)}$ [M1] : Factorize $= \frac{9}{x(x-y)}$ [A1]	

[Total: 6m]

3	scale factor = $k = \frac{22}{14} = \frac{11}{7}$ [M1]	
	$k = \frac{AD}{AE} = \frac{AC}{AB}$ $k = \frac{11}{7} = \frac{x}{x+6}$ $Multiplication$	
	$\frac{x+6}{x} = \frac{11}{7}$ (M1): Cross-Multiplication 11x = 7x + 42 11x - 7x = 42 4x = 42	
	$x = \frac{42}{4} = 10.5$ [A1]	

A	AL .	ION D	[Total: 3m]
40	(a)	$P(Blue) = \frac{20}{100} = \frac{1}{5} \text{ or } 0.2 $ [B1]	
	(b)	P(Green) = $\frac{10}{100} = \frac{1}{10}$ or 0.1 [M1] P(Not Green)= $1 - \frac{1}{10}$ = $\frac{9}{10}$ or 0.9 [A1]	
	<u> </u>	DANYAL	[Total: 3m]



Bedok View Secondary School 2018 EOY Sec 2NA Paper 1 Marking Scheme



[Total: 8m]

6	(a)	$y = kx^{2}$ y = 14, x = 2 $14 = k(2)^{2}$ $k = \frac{14}{4} = 3.5$ [M1] $y = 3.5x^{2}$ [A1]
	(b)	When $x = 3$, $y = 3.5(3^2)$ [M1] $y = 31.5$ [A1]
DAT	(c)	% change in $y = \frac{31.5 - 14}{14} \times 100\%$ [M1] = $\frac{17.5}{14} \times 100\%$ = 125% [A1]

[Total: 6m]

7 Refer to the Answer booklet attached for drawing of locus	7	Refer to the Answer booklet attached for drawing of locus	
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[Total: 6m]





Bedok View Secondary School 2018 EOY Sec 2NA Paper 1 Marking Scheme

9	$\frac{2p+q}{2p-4r} = \frac{5}{2}$		
	3q - 4p = 8 8(2p + q) = 5(3q - 4p)	[M 1]	
	16p + 8q = 15q - 20p		
	16p + 20p = 15q - 8p		
	36p = 7q	[M1]	
	$\frac{p}{q} = \frac{7}{36}$	[A1]	
	-		



10	(a)	$(x - 3) (x + 3) = (x)^2 - (3)^2 = x^2 - 9$ [B1]		DANYAL
EDC	(b)	(x - 3)(x + 3) = (397)(403) (x - 3)(x + 3) = (400 - 3)(400) $\therefore x = 400$ $(x)^{2} - (3)^{2} = (400)^{2} - (3)^{2}$ $x^{2} - 9 = (400)^{2} - (3)^{2}$ $x^{2} - 9 = 160000 - 9$ = 159991	+ 3) [M1]	
		157771	[]	

[Total: 3m]

		DANTION	[Total: 3m]
11	(a)	$3 + 9 + 15 + 21 + 27 = 3 \times 5^2 = 75$ [B1]	
	(b)	$3y^2 = 507$ $y^2 = 169$ y = 13 [A1]	NAL
0Å	ZZ.	When $y = 12$, = $3 \times y^2 = 3(144) = 432$ [M1]	DANIATION
ED	UCA	x = 507 - 432 x = 75 [A1]	



ABedok View Secondary School 2018 EOY Sec 2N Paper 2 Marking Scheme

No.		Working	Remarks
1	(a)	$131^{\circ} + 5p^{\circ} + 4q = 180^{\circ} - \dots (1)$ $150^{\circ} + 159^{\circ} + 6q + 3p = 360^{\circ} - \dots (2)$ From (1): $5p + 4q = 180 - 131$ $5p + 4q = 49 [B1]$ From (2): $3p + 6q = 360 - 150 - 159$ $3p + 6q = 51 [B1]$	*Don't have to state the reasons for the angles
DAD	(b)	(1)×3: 15 p + 12 q = 147 (3) (2))×5: 15 p + 30 q = 255 (4) (4)-(3): 30 q - 12 q = 255 - 147 18 q = 108 $q = \frac{108}{18} = 6$ Sub $q = 6$ into (2): 3 p + 6 q = 51 3 p = 51 - 6 q 3 p = 51 - 6 q 3 p = 51 - 6 q 3 p = 51 - 6 q p = 5 [A1], q = 6 [A1] OR 5 p + 4 q = 49 (1)	ANYAL
DA	A.A.	$3p + 6q = 51 - \dots (2)$ (2): $3p = 51 - 6q$ $p = \frac{51 - 6q}{3} - \dots (3)$ Sub (3) into (1): (1): $5p + 4q = 49$ $5\left(\frac{51 - 6q}{3}\right) + 4q = 49$ $255 - 30q + 4q(3) = 49$ $255 - 30q + 12q$ 3 $255 - 18q = 49(3)$ $-18q = 147 - 255$ $q = \frac{-108}{-18} = 6$ Sub q = 6 into (2): (2): $3p + 6q = 51$ $3p + 6(6) = 51$ $p = \frac{15}{3} = 5$ $p = 5$ [A1], $q = 6$ [A1]	DANYAL

ABedok View Secondary School 2018 EOY Sec 2N Paper 2 Marking Scheme

2	(a)	$27x^{2} - 3y^{2} = 3(9x^{2} - y^{2})$ = 3[(3x)^{2} - (y)^{2}] = 3(3x - y)(3x + y)	[M1] [A1]	
	(b)	$27x^{2} - 3y^{2} = 33$ 3(3x - y)(3x + y) = 33 (3x - y)(3x + y) = 11 Since $(3x - y) = 1$, (3x + y)(1) = 11	[M 1]	
	~1	3x + y = 11	[A1]	LAVAL

[Total: 4m]

3	(a)	(i)	Jacie = x years old Olivia = $(x + 11)$ years old [B1]	
		(ii)	Mother's age = $3x$ years old [B1]	
	(b)	(i)	Total age = Jacie + Olivia + Mother = 111 x + (x + 11) + 3x = 111 or 5x + 11 = 111 or $5x = 100$ [B1]	
		(ii)	5x = 111 - 11 $x = \frac{100}{5} = 20$ [B1]	ANYAL

D	AN	ATION		[Total: 4m]
4	(a)	1 bouquet = $$25$ Let x be the number	rs of houquets to be sold	
		$25x \ge 520$ $x \ge \frac{520}{25}$	[M1]	
		$x \ge 20.8$	[A1]	
	(b)	Min no. of $x = 21$	[A1]	

[Total: 3m]

ABedok View Secondary School 2018 EOY Sec 2N Paper 2 Marking Scheme

-		
5	(a)	$r = \sqrt{13^2 - 12^2}$ [M1]
		$r = \sqrt{25} = 5 \text{ cm}$ [A1]
	(b)	Total surface area of Evan mineral bottle
		= Surface area of cone + surface area of hemisphere
		$=\pi rl+2\pi r^2$
		$=\pi(5)(13) + 2\pi(5)^2$ [M1]
		$=115\pi$
		= 361.281552
		$= 361 \ cm^2 \ (3sf) $ [A1]
	(c)	Volume of Evan mineral bottle
		= Volume of cone + Volume of hemisphere
-	N	$=\frac{1}{\pi}r^{2}h+\frac{2}{\pi}r^{3}$
NB	2	
Pa	SCA	$= \frac{1}{3}\pi(5)^{2}(12) + \frac{1}{3}\pi(5)^{3} [MI]$
EN		$=100\pi + \frac{250}{2}\pi$
		_ 550 <i>π</i>
		$-\frac{3}{3}$
		= 575.9586532
		$= 576 \ cm^{3}(3sf)$ [A1]

[Total: 6m]



[Total: 8m]

 $x^2 + y^2 = 14$ and xy = 57 $(3x + 3y)^{2} = [3(x + y)]^{2}$ = (3)²(x + y)² = 9(x + y)² [M1]: Proper Expansion of $(3x + 3y)^2$ $=9(x^{2}+y^{2}+2xy)$ = 9[(14 + 2(5)][**M1**]: Proper Substitution of $x^2 + y^2 = 14$ and xy = 5= 9(24) = 216[A1] EDUCATION

[Total: 3m]

8	(a)	(i)	Diagram I: Diagram II 1: n 2.5cm: 60m 1cm: 24m 1cm: 2400 cm 1: 2400 [B1]	
	V	(ii)	Diagram I: Diagram II 1 : 2400 $1.9: 2400 \times 1.9$ Height of the petal in Diagram II= $(2400 \times 1.9)cm$ [M1 = $4560cm = 45.6m$ [A1]	I WAL
DA	DCAT	(iii)	Diagram I: Diagram II 1cm : 2400 cm 1cm : 24m $(1cm)^2 : (24m)^2$ [M1] $1cm^2 : 576m^2$ $\frac{1728}{576} : 1728m^2$ [M1] Area of the highest petal on the I: $\frac{1728}{576} \times 1cm^2$ $= 3cm^2$ [A1]	DUCATA
	(b)	Comb = 6(1) = 816 $Comb = (2A) = 1 F = 44$	bination $A = 6$ Adults + 3 Senior Citizens+ 2 Children (7) + 3(14) + 2(10) (M1) bination $B = 6$ Adults + 3 Senior Citizens + 2 Children +2C)+4A+3S amily + $4A + 3S$ +4(17)+3(14)	NYAL
DE	DOC.	=\$15 *1m f *1m f Since worth	[M1] for working to show the cheapest combination for explanation of the chosen combination. Combination B < Combination A, by \$10, hence it is more a it to purchase Combination B. [A1]	*[A1] as long as able to make a decision on the best combination

[Total: 9m]

9	(a)	If ΔBCD is a right- angled triangle, $BC^2 + BD^2 = CD^2$ $LHS = BC^2 + BD^2 = 15^2 + 8^2$ LHS = 289 $RHS = CD^2$ $RHS = 17^2$ RHS = 289 = LHS Since $LHS = RHS = 289$, $\therefore \Delta BCD$ is a right- angled Triangle. [A1]
DA	(b)	$25^{2} = 15^{2} + AB^{2} [M1]$ = 25 ² - 15 ² $AB^{2} = 400$ $AB^{2} = 20^{2}$ $AB = 20 \text{ cm} \qquad [A1]$
	(c)	Area of triangle $= \frac{1}{2} \times Base \times Perpendicular height$ $= \frac{1}{2} \times 15 \times 20 = 150 \text{ cm}^{2}$ [M1] [A1]
	(d)	Let the shortest distance be BX. Area of $\triangle ABC = 150cm^2$ $150cm^2 = \frac{1}{2} \times 25 \times BX$ [M1] BX = 12 cm [A1]

[Total: 8m]