

NORTH VISTA SECONDARY SCHOOL

END-OF-YEAR EXAMINATION 2018



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CLASS:	
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SUBJECT: ELEMENTARY MATHEMATICS

DATE: 4 OCTOBER 2018

LEVEL/STREAM: SECONDARY 3 EXPRESS

CODE: 4048/01

TIME: 1 HOUR 30 MINUTES

READ THESE INSTRUCTIONS FIRST

Write your name, register number and class on all the work you hand in. Write in dark blue or black pen. You may use a pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

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Answer all questions.

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For π , use either your calculator value or 3.142, unless the question requires answer in terms of π .

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question. The total of the marks for this paper is 60.

For Examiner's Use				
Category Question				
Accuracy				
Brackets				
Fractions				
Units				
Others				
Marks Deducted				

Mathematical Formulae

Compound Interest

Total amount =
$$P\left(1 + \frac{r}{100}\right)^n$$

Mensuration

Curved surface area of a cone = πrl

Surface area of a sphere = $4\pi r^2$

Volume of a cone =
$$\frac{1}{3}\pi r^2 h$$

Volume of a sphere
$$=$$
 $\frac{4}{3}\pi r^3$

Area of triangle $ABC = \frac{1}{2}ab\sin C$

Arc length = $r\theta$, where θ is in radians

Sector area
$$=\frac{1}{2}r^2\theta$$
, where θ is in radians

Trigonometry

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$
$$a^2 = b^2 + c^2 - 2bc \cos A$$



Statistics

Mean =
$$\frac{\sum fx}{\sum f}$$

Standard deviation =
$$\sqrt{\frac{\sum fx^2}{\sum f} - \left(\frac{\sum fx}{\sum f}\right)^2}$$



Answer all the questions.

- 1 The total number of visitors arriving in Singapore in 2008 was 1.12×10^7 . The visitors spent a total of 16.5 billion dollars. [1 billion = 10^9]
 - (a) 1.12×10^7 can be written as k million. [1 million = 10^6] Find k.

(b) What is the average amount of money spent by each visitor? Give your answer correct to the nearest dollar.

Answer \$ [1]

2 Simplify the following (a) $5x^2y^{-1} \times x^{-3}y$,

Answer

(b) $\left(\frac{16}{x^4}\right)^{-\frac{1}{2}}$.

[1]

3 (a) Without the use of calculator, evaluate $3^0 + 9^{-1} + 3^{-2}$.

4

4

Answer cm [1]





The figure shows a triangle ABC with B (-2,4), C (2,2) and A (a,b). The gradients of BC, AC and AB are -2n, 2n, n respectively. (a) Find

6

(i) the value of n,



Answer $n = \dots$ [1]

(ii) the coordinates of A,

Answer A (.....) [3] 6 (a) (iii) the length of BC.

Answer units [1]

(b) Given that the area of triangle ABC is 12 units², find the length of the perpendicular line drawn from A to BC.

Answer units [2]

7 (a) Solve the inequality $\frac{2}{3}(x+1) \le x+2 < -(2x-9)$.

Answer [3]

(b) Hence, state the largest prime number which satisfies the above inequality.

7



In the diagram above, the points A, B and C form an equilateral triangle and the bearing of B from A is 084° .

Find the bearing of (a) C from A,

Answer° [1]

(b) *C* from *B*.

Answer° [2]

9 The figure shows a circle with centre O and passes through the points P, Q and R. It has a radius of 12 cm and PQ = 16 cm.



(a) Show that angle POQ = 1.46 radians, correct to 3 significant figures.

Answer		
	AVAL	[1]

(b) Find the length of the major arc PRQ.

Answer ... cm

(c) Find the area of the shaded region.

[3]

[2]

10 The diagram below shows the speed-time graph of a moving object.



[1] Answer m/s

(c) Find the value of t if the total distance travelled by the object is 450 m.

10

Answer $t = \dots$ [2]

10 (d) On the axes in the answer space below, sketch the distance-time graph for the first 23 seconds and indicate clearly, on the vertical axis, the distance travelled at t = 8 s and t = 23 s.





11 Two machines, A and B, are used to manufacture ice cream tubs. 5 ice cream tubs manufactured by each machine are randomly selected from each machine. The mass of the ice cream tubs manufactured by Machine A are weighed and shown in the table below.

Machine A (mass in g)	505	498	502	502	503
Trideninie II (made m 8)					

(a) Find the mean and standard deviation of the mass of the ice cream tubs manufactured by Machine A.

Answer Meang [1]

Standard Deviationg [2]

(b) <u>Machine B</u>

Mean = 502 g

Standard Deviation = 3.16 g

Based on your answer in (a) and information given above, decide and explain which machine you will recommend to ice cream manufacturers.

12



The figure is a trapezium, which is made up of two right angled triangles, triangle ABC and triangle $ACD \cdot AC = 4.8$ cm and AD = 3 cm.





(b) *AB*,

(c) area of *ABCD*.

Answer cm^2 [2]

13 In the diagram, A, B, C and D lie on the circumference of the circle. Angle $AOD = 126^{\circ}$, angle $ABD = 63^{\circ}$ and angle $ODB = 20^{\circ}$.

126° 20% C B Explain why O is the centre of the circle. (i) Answer [1] Find, giving reasons for each answer, (ii) (a) angle ACD, [1] Answer (b) angle BAD, Answer angle BCD. (c) Answer [1]

(iii)	Is OD parallel to BC? Explain your answer.		
	Answer		
			[2]



13

End of Paper

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NORTH VISTA SECONDARY SCHOOL

END-OF-YEAR EXAMINATION 2018



NAME:()	CLASS:
SUBJECT: MATHEMATICS (PAPER 2)		DATE: 8 OCTOBER 2018
LEVEL/STREAM: SECONDARY 3 EXPRESS		TIME: 1 HOUR 30 MINUTES
CODE: 4048/2		

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$$\pi rl$$

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Statistics

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$$\sqrt{\frac{\sum fx^2}{\sum f} - \left(\frac{\sum fx}{\sum f}\right)^2}$$

Answer all the questions.

(a) Express as a single fraction
$$\frac{3x}{(x-3)^2} - \frac{7}{2x-6}$$
. [3]

(b) Simplify
$$\frac{2s^2 + 9st - 5t^2}{3s^2 - 75t^2} \times \frac{s - 5t}{5}$$
. [3]

(c) It is given that
$$\frac{1}{a} + \frac{1}{b} = \frac{1}{c^2}$$
.
(i) Find *b* when $a = 3, c = -1$. [2]

Express c in terms of a and b. **(ii)** [3]

2 The cash price of a particular car is \$94000. (i) (a)

> Shawn decides to buy this car. He paid a deposit of \$10000 and the rest by monthly instalments of \$1090 over a period of $7\frac{1}{2}$ years. The bank charges an interest of i % per annum on the amount loaned.

Calculate the value of i.

(ii) Betty buys an identical car which costs the same.

She pays a deposit of one-fifth of the cash price. She then borrows the remaining cost for 3 years at compound interest of 3% per year.

Calculate the total amount of money Betty paid for the car.

[4]

[3]

(b) The exchange rate between US dollars (\$) and Korean won (¥) is \$1 = 1082.50₩.

Bill bought 166500# from the bank.

Calculate the total amount in US dollars he paid the bank. Leave your [2] answer to the nearest dollar.

- 3 Ray represented his class in a 10 km race. He started running at a speed of x km/h. After 2 km, he increased his speed by 1 km/h and ran the remaining distance at this speed.
 - (i) Find and simplify, in terms of x, an expression for the time taken by Ray to complete the race.
 [2]
 - (ii) Given that Ray's average speed for the whole race was 10.5 km/h, form an [3] equation in x and show that it reduces to $10x^2 95x 21 = 0$.
 - (iii) Solve the equation $10x^2 95x 21 = 0$. Give your answers correct to 2 decimal places. [3]
 - (iv) Find the time, in hours, Ray would have taken if he had ran the entire race at his initial speed. [1]
- 4 The diagram shows three points, P, Q and R on a piece of horizontal land. PR = 470 m and QR = 318 m.



It is given that $\sin \theta = \frac{7}{25}$ and θ is obtuse.

(a) Calculate the area of ΔPQR .

[2]

- (b) Without the use of a calculator, show that the value of $\cos \theta = -\frac{24}{25}$. [2]
- (c) Hence, find the distance PQ. [3]
- (d) T is the top of a building that is standing vertically at R and the angle of elevation of T from P is 12°. Calculate the height of the building. [2]
- (e) Eli walks along the path PQ until he reaches a point E. Calculate the largest angle of depression from T to E. [3]

4

5 The graph shows the cumulative frequency curve for the number of hours of community service accumulated over four years by 120 students in Vista Secondary School.



Number of hours of community service

(a)	Use your graph to find the (i) median,		
	(ii)	interquartile range,	[2]

- (iii) percentage of students who accumulated more than 100 hours of community service.
- (b) The number of hours of community service accumulated by another 120 students in Venus Secondary School is represented in the following box-and-whisker plot.



Number of hours of community service

Make two comparisons between the number of hours the students spent on community service in the two schools.

5

[2]

[2]

6 Answer the whole of this question on a sheet of graph paper.

An analyst was studying the effect of the introduction of a new policy to a company's business profit. He felt that the amount of profit, y hundred thousand dollars, over a period of x months could be modelled by the equation

$$y = \frac{x^3}{5} + \frac{10}{x} - 10$$
.

Some corresponding values of x and y are given in the following table.

x	0.5	1.5	2	3	4	4.5	5
у	10.03	-2.66	-3.4	-1.27	5.30	10.45	17.00

(a) Using a scale of 2 cm to represent 1 unit, draw a horizontal x-axis for $0 \le x \le 5$.

Using a scale of 1 cm to represent 1 unit, draw a vertical y-axis for $-4 \le y \le 18$.

On your axes, plot the points given in the table and join them with a smooth curve. [3]

(b) Use your graph to state the period when the company is suffering a loss. [2]

(c) Use your graph to find the solution(s) to the equation $\frac{x^3}{5} + \frac{10}{x} = 15$ in the range $0 \le x \le 5$. [2]

(d) By drawing a tangent, find the gradient of the curve at (1.5, -2.66). [2]

(e) (i) On the same axes, draw the line y = 3x + 1 for $0 \le x \le 5$. [1]

(ii) The x-coordinates of the points where the line in (e)(i) intersects the curve are the solutions of the equation $x^4 - ax^2 - bx + 50 = 0$. Find the value of a and of b. [2]

END OF PAPER

Qn	Solution	Marks
1a	$1.12 \times 10 \times 10^{6}$	
	$=11.2 \times 10^{6}$	
	<i>k</i> = 11.2	B1
1b	16.5×10^{9}	
	1.12×10^{7}	
	= \$1473.2142	
	= \$1473	B1
2a	$5x^2y^{-1} \times x^{-3}y$	
	$=5x^{-1}y^{0}$	X
	LS UCALLO	
1	x	B1
26	$\left(\frac{16}{2}\right)^{-\frac{1}{2}}$	
	$\left(\overline{x^4}\right)$	
	$(r^4)^{\frac{1}{2}}$	
	$=\left(\frac{\pi}{16}\right)$	
	r^2	
	$=\frac{\pi}{4}$	B2
3a	$3^{-0} + (9)^{-1} + 3^{-2}$	
	$=1+\frac{1}{9}+\frac{1}{3^2}$	
	$=1\frac{2}{2}$	B1
3h	9 9 ² x-1 1	
50	$\frac{\delta}{4} = \frac{1}{16^x}$	Z
	$2^{3(2x-1)}$ 2^{0}	1/1
	$\frac{2}{2^2} = \frac{2}{2^{4x}}$	MI (same base)
	6x - 3 - 2 = 0 - 4x	M1 simplify
	6x - 5 = -4x	
	10x = 5	A1
	$r = \frac{1}{2}$	
	2	
4a 4b	155 cm Mean	
	1570	M1
	$=\frac{10}{10}$	A 1
	=157cm	Al

Sec 3E E.Maths EOY P1 2018 Solutions



[Turn Over

6aii	Gradient of $AC = 2n$	
	$\frac{b-2}{2} - 2(\frac{1}{2})$	
	$a-2^{-2}(4)$	
	2b - 4 = a - 2	
	2b - a = 2 (1)	M1
	Gradient of $AB = n$	
	$\frac{b-4}{2} = \frac{1}{2}$	
	a+2 4	
	4b - 16 = a + 2	
	4b - 18 = a (2)	M1
	Sub (2) into (1)	
	2b - (4b - 18) = 2	
	-2b+18=2	M
	b = 8	
	a = 4(8) - 18	
	<i>a</i> = 14	A 1
	A(14,8)	
6aiii	Length of BC	
	$=\sqrt{(-2-2)^2+(4-2)^2}$	
	$=\sqrt{20}$	
	= 4.4721	DI
	= 4.47 <i>units</i>	BI
6b	$\frac{1}{1} \times \sqrt{20} \times h = 12$	M1
	2	
	h = 5.3665	A1
L	<i>h</i> = 5.37 <i>units</i>	
7a	$\frac{2}{2}(x+1) \le x+2 < -(2x-9)$	
	3) ALCATION DALCATIO	Ľ.
	$\frac{2}{3}(x+1) \le x+2$	
	$\left \frac{2}{3}x + \frac{2}{3} \le x + 2\right $	
	$-\frac{1}{r} < 1\frac{1}{r}$	
	3^{2} 3	MI
	$x \ge -4$	1711
	x+2 < -(2x-9)	
	3x < 7	M1
	$x < 2\frac{1}{2}$	1711
	3	
	$-4 \le x < 2\frac{1}{3}$	A1

7b	2	B1
8a	Bearing of C from A	
	$=84^{\circ}+60^{\circ}$	
	=144°	B1
8b	$84^\circ - 60^\circ = 24^\circ$	M1
	Bearing of C from B $-180^{\circ} \pm 24^{\circ}$	
	-201°	A1
92	8	
1	$\sin\theta = \frac{\sigma}{12}$	
	$\theta = 0.72972$	
	$\angle POQ = 0.72972 \times 2$	D1
	=1.45944	Ы
	=1.46rad(shown)	0N
9b	Reflex angle POQ = $2\pi - 1.45944$	
	$= 4.82374 rad$ Major arc <i>PRQ</i> $= r\theta$	
	=12(4.82374)	M
	= 57.88488	IMI I
	= 57.9 cm	A1
9c	Area of shaded region	
	$=\frac{1}{2}(12)^2(1.45944) - \frac{1}{2}(12)^2\sin 1.45944$	M2
	=105.07968 - 71.55405	
	= 33.52563	
	$= 33.5 cm^2$	A1
	OR	L
	180°	N
	$\theta = 1.45944 \times \frac{\pi}{\pi}$	
	= 83.61975	
	$Area = \frac{83.61975}{260} \times \pi (12)^2 - \frac{1}{2} (12)^2 \sin 83.61975$	M2
	- 33 5356	
	-33.5550	A 1
10a	= 55.5 cm	B1
10b	v 18	
	$\frac{1}{5} = \frac{2}{8}$	
	1	
1		



12b	$\cos \angle BAC = \frac{4.8}{4R}$	
	AB	
	$\cos 38.6821 = \frac{4.8}{3}$	M1
	AB	IVII
	$AB = \frac{4.8}{1}$	
	cos 38.6821	
	AB = 6.1489	
	AB = 6.15 cm	A1
12c	By Pythagoras' Thereom,	
	$CD = \sqrt{4.8^2 - 3^2}$	
	<i>CD</i> = 3.74699	
	Area	
		M
	$= - \times (6.1489 + 3.74699) \times 3$	M1
	=14.8437	
	$=14.8cm^{2}$	A1
13 (i)	Since $\angle AOB = 2 \times \angle ABD$, O is the centre of circle. (\angle at centre	
	$= 2 \angle$ at circumference)	B1
13(ii)	$\angle ACD = 63^{\circ} (\angle s \text{ in same segment})$	B1
(a)	· · · · · · · · · · · · · · · · · · ·	
13(ii) (b)	$\angle ODA = \frac{180 - 126}{2} = 27^{\circ}$ (base $\angle s$ of isos. \triangle)	M1
	$\angle BAD = 180 - 63 - 20 - 27 = 70^{\circ} (\text{sum of } \angle \text{s in } \Delta)$	A1
13	$\angle BCD = 180 - 70 = 110^{\circ}$ (\angle s in opp. segment)	B1
(ii)		
(c)		
13	$\angle DBC = 27^{\circ} (\angle s \text{ in same segment})$	M1
(iii)	Since $\angle ODB \neq \angle DBC$, OD is not parallel to BC.	A1
	DA JUN DA JUN	DIA
	EDUCA	

3E EM P2 Marking Scheme

Question	Marking Scheme		Marks
1 (a)	3x 7		M1
	$\frac{1}{(x-3)^2} - \frac{1}{2(x-3)}$		
	6x-7(x-3)		M1
	$=\frac{1}{2(x-3)^2}$		
	-x+21		Δ1
	$=\frac{1}{2(x-3)^2}$		AI
1 (b)	$2s^2 + 9st - 5t^2 s - 5t$		M2
	$\frac{3s^2 - 75t^2}{5}$		(cross method
	(2s-t)(s+5t) = s-5t	NAL	and diff
D	$=\frac{3(s-5t)(s+5t)}{3(s-5t)(s+5t)}\times\frac{5}{5}$	1 NITIO	of
E	2s-t	JUCIE.	squares)
	- 15		
			A1
1 (c) (i)	$\frac{1}{1+1} = \frac{1}{1}$		M1
	3 b 1		
	$\frac{1}{1} = \frac{2}{2}$		
	$b=1\frac{1}{2}$ EDUCAT		A1
1 (c) (ii)	1,1 1		
	$\frac{a}{a} + \frac{b}{b} = \frac{c^2}{c^2}$		
	b+a		M1
	$ab - c^2$		
	$c^2 = \frac{ab}{ab}$	TAT	
D	b+a	NTO	
	$c = \pm \sqrt{\frac{ab}{ab}}$	JUCAILO	A2 (A1
	$\sqrt{b+a}$		for ±)
2 (a) (i)	Interest = $1090 \times 7.5 \times 12 + 10000 - 94000 = 14100		M1
	$14100 = \frac{84000 \times i \times 7.5}{100}$		M 1
	100		
	$i = 2\frac{3}{21}\%$		A 1
	21		A1

2 (a) (ii)	Amount borrowed = $\frac{4}{5} \times 94000 = \75200	
	Amount owed = $75200(1 + \frac{3}{100})^3 = \82173.0704	M1
	Amount Betty paid = $82173.0704 + \frac{1}{5} \times 94000$	M1
	= \$100973.07(2 <i>dp</i>)	A1
2 (b)	Total amount = $\frac{101.5}{100} \times 166500 \div 1082.50$	M1
8	=\$153.81	
	=\$154	A1
3 (i)	Time = $\frac{2}{x} + \frac{8}{x+1}$ = $\frac{2x+2+8x}{x(x+1)}$ 10x+2	M1
	$=\frac{1}{x(x+1)}h$	A1
3 (ii)	$\frac{\frac{10}{10x+2}}{\frac{10}{x(x+1)}} = 10.5$	M1
	$\frac{10x(x+1)}{10x+2} = 10.5$	M1
	$10x^2 + 10x = 105x + 21$ $10x^2 - 95x - 21 = 0$	M1
3 (iii)	$x = \frac{95 \pm \sqrt{(-95)^2 - 4(10)(-21)}}{2(10)}$	M1
Γ	$=\frac{95\pm\sqrt{9865}}{20}$ = 9.7161 or -0.2161	M1
	=9.72 or -0.22	Δ1
3 (iv)	$\frac{10}{9.7161} = 1.03h$	B1
4 (a)	Area = $\frac{1}{2}(318)(470)(\frac{7}{25})$	M1
	$=20924\frac{2}{5}m^2$	A1

4 (b)		
	$\sin\theta = \frac{1}{25}$	
	$\sin x = \frac{7}{25}$, where x is acute	
	25 By Pythagoras' Theorem,	
	$adj = \sqrt{25^2 - 7^2} = 24$	M1
	24	
	$\cos x = \frac{1}{25}$	
	$\cos\theta = -\frac{24}{25}$	A1
4 (c)	$PO^2 = 318^2 + 470^2 - 2(318)(470)(-\frac{24}{2})$	M2
E E	$PQ = \sqrt{318^2 + 470^2 - 2(318)(470)(-\frac{24}{25})}$	
	= 780.3763	
	= 780m(3sf)	A1
4 (d)	$\tan 12^\circ = \frac{TR}{470}$	M1
	$TR = 470 \tan 12^{\circ}$	
	= 99.9015	
	=99.9m(3sf)	A1
4 (e)	Let the perpendicular dist be h.	
	$\frac{1}{2}(h)(780.3763) = 20924\frac{2}{5}$	M1
	h = 53.6264	
	= 53.6m(3sf)	
	Let the angle of depression be x.	4
\mathbf{D}	$\tan r = \frac{99.9015}{10000000000000000000000000000000000$	M1
E	53.6264 EDUCA	
	x = 61.7734	A 1
5 () ()	$= 61.8^{\circ}(1dp)$	AI D1
5(a)(1)	70 hours	Ы
5 (a) (11)	Q1=54	
	IQR	
	= 84 - 54	M1 A1
5 (a) (22)	= 30 <i>hours</i>	M1
5 (a) (111)	$\frac{120-112}{120}$ ×100%	1911
	$=6\frac{2}{3}\%$	A1
5 (b)	IQR for Venus Sec	

