NAME: $\qquad$ (

SUBJECT: ELEMENTARY MATHEMATICS
LEVEL/STREAM: SECONDARY 3 EXPRESS

DATE: 4 OCTOBER 2018
TIME: 1 HOUR 30 MINUTES

CODE: 4048/01

## READ THESE INSTRUCTIONS FIRST

Write your name, register number and class on all the work you hand in.
Write in dark blue or black pen.
You may use a pencil for any diagrams or graphs.
Do not use staples, paper clips, highlighters, glue or correction fluid.
Answer all questions.
If working is needed for any question, it must be shown with the answer.
Omission of essential working will result in loss of marks.
The use of an approved scientific calculator is expected, where appropriate.
If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degree to one decimal place.
For $\pi$, use either your calculator value or 3.142 , unless the question requires answer in terms of $\pi$.

At the end of the examination, fasten all your work securely together.
The number of marks is given in brackets [ ] at the end of each question or part question.
The total of the marks for this paper is 60.

| For Examiner's Use |  |
| :---: | :---: |
| Category | Question |
| Accuracy |  |
| Brackets |  |
| Fractions |  |
| Units |  |
| Others |  |
| Marks <br> Deducted |  |

## Compound Interest

$$
\text { Total amount }=P\left(1+\frac{r}{100}\right)^{n}
$$

Mensuration
Curved surface area of a cone $=\pi r l$

$$
\text { Surface area of a sphere }=4 \pi r^{2}
$$

$$
\text { Volume of a cone }=\frac{1}{3} \pi r^{2} h
$$

$$
\text { Volume of a sphere }=\frac{4}{3} \pi r^{3}
$$

Area of triangle $A B C=\frac{1}{2} a b \sin C$
Arc length $=r \theta$, where $\theta$ is in radians

$$
\text { Sector area }=\frac{1}{2} r^{2} \theta, \text { where } \theta \text { is in radians }
$$

## Trigonometry

$$
\begin{gathered}
\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C} \\
a^{2}=b^{2}+c^{2}-2 b c \cos A
\end{gathered}
$$

## Statistics

$$
\begin{aligned}
\text { Mean } & =\frac{\sum f x}{\sum f} \\
\text { Standard deviation } & =\sqrt{\frac{\sum f x^{2}}{\sum f}-\left(\frac{\sum f x}{\sum f}\right)^{2}}
\end{aligned}
$$

Answer all the questions.
1 The total number of visitors arriving in Singapore in 2008 was $1.12 \times 10^{7}$. The visitors spent a total of 16.5 billion dollars. [ 1 billion $=10^{9}$ ]
(a) $1.12 \times 10^{7}$ can be written as $k$ million. [ 1 million $=10^{6}$ ] Find $k$.

Answer $k=$
(b) What is the average amount of money spent by each visitor? Give your answer correct to the nearest dollar.

Answer \$

2 Simplify the following
(a) $5 x^{2} y^{-1} \times x^{-3} y$,

Answer
(b) $\left(\frac{16}{x^{4}}\right)^{-\frac{1}{2}}$.

3 (a) Without the use of calculator, evaluate $3^{0}+9^{-1}+3^{-2}$.

> Answer ....................................
[1]
(b) Solve $\frac{8^{2 x-1}}{4}=\frac{1}{16^{x}}$.

Answer

4 In a class of 10 girls, their heights are $158 \mathrm{~cm}, 155 \mathrm{~cm}, 146 \mathrm{~cm}, 149 \mathrm{~cm}$, $158 \mathrm{~cm}, 155 \mathrm{~cm}, 165 \mathrm{~cm}, 172 \mathrm{~cm}, 155 \mathrm{~cm}$ and 157 cm .

For these heights, find
(a) the mode,

> Answer ............................. cm
(b) the mean,
$\qquad$
(c) the median.

5 (a) Sketch the graph of $y=-(x-4)(x+2)$.

(b) Write down the equation of the line of symmetry of the graph.

Answer
(c) Find the coordinates of the turning point.


The figure shows a triangle $A B C$ with $B(-2,4), C(2,2)$ and $A(a, b)$.
The gradients of $B C, A C$ and $A B$ are $-2 n, 2 n, n$ respectively.
(a) Find
(i) the value of $n$,

Answer $n=$
(ii) the coordinates of $A$,

6 (a) (iii) the length of $B C$.

Answer .......................... units
(b) Given that the area of triangle $A B C$ is 12 units $^{2}$, find the length of the perpendicular line drawn from $A$ to $B C$.

Answer ......................... units

7 (a) Solve the inequality $\frac{2}{3}(x+1) \leq x+2<-(2 x-9)$.
$\qquad$
(b) Hence, state the largest prime number which satisfies the above inequality.

8


In the diagram above, the points $A, B$ and $C$ form an equilateral triangle and the bearing of $B$ from $A$ is $084^{\circ}$.

Find the bearing of
(a) $C$ from $A$,
$\qquad$
(b) $C$ from $B$.

9 The figure shows a circle with centre $O$ and passes through the points $P, Q$ and $R$. It has a radius of 12 cm and $P Q=16 \mathrm{~cm}$.

(a) Show that angle $P O Q=1.46$ radians, correct to 3 significant figures.

## Answer

$\qquad$
$\qquad$
$\qquad$
(b) Find the length of the major $\operatorname{arc} P R Q$.
Answer .............................cm
(c) Find the area of the shaded region.

10 The diagram below shows the speed-time graph of a moving object.

(a) What is the acceleration of the object at $t=10$ seconds?
$\qquad$
(b) Find the speed of the object when $t=5$ seconds.

Answer ..........................m/s
(c) Find the value of $t$ if the total distance travelled by the object is 450 m .

10 (d) On the axes in the answer space below, sketch the distance-time graph for the first 23 seconds and indicate clearly, on the vertical axis, the distance travelled at $t=8 \mathrm{~s}$ and $t=23 \mathrm{~s}$.

Answer


11 Two machines, A and B, are used to manufacture ice cream tubs. 5 ice cream tubs manufactured by each machine are randomly selected from each machine. The mass of the ice cream tubs manufactured by Machine A are weighed and shown in the table below.

| Machine A (mass in g) | 505 | 498 | 502 | 502 | 503 |
| :--- | :--- | :--- | :--- | :--- | :--- |

(a) Find the mean and standard deviation of the mass of the ice cream tubs manufactured by Machine A.
Answer Mean ..... [1]
Standard Deviation ..... [2]
(b) Machine B

Mean $=502 \mathrm{~g}$
Standard Deviation $=3.16 \mathrm{~g}$
Based on your answer in (a) and information given above, decide and explain which machine you will recommend to ice cream manufacturers.

Answer $\qquad$
$\qquad$
$\qquad$
$\qquad$


The figure is a trapezium, which is made up of two right angled triangles, triangle $A B C$ and triangle $A C D . A C=4.8 \mathrm{~cm}$ and $A D=3 \mathrm{~cm}$.

## Calculate

(a) angle $A C D$,
$\qquad$
(b) $A B$,
$\qquad$
(c) area of $A B C D$.
$\qquad$

13 In the diagram, $A, B, C$ and $D$ lie on the circumference of the circle. Angle $A O D=126^{\circ}$, angle $A B D=63^{\circ}$ and angle $O D B=20^{\circ}$.

(i) Explain why $O$ is the centre of the circle.

## Answer

$\qquad$
$\qquad$
$\qquad$
(ii) Find, giving reasons for each answer,
(a) angle $A C D$,

Answer
(b) angle $B A D$,

Answer $\qquad$
$\qquad$
$\qquad$
(c) angle $B C D$.

13 (iii) Is $O D$ parallel to $B C$ ? Explain your answer. Answer
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## End of Paper

NAME:
SUBJECT: MATHEMATICS (PAPER 2)
LEVEL/STREAM: SECONDARY 3 EXPRESS

CLASS: $\qquad$

CODE: 4048/2

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Write your name, register number and class on all the work you hand in.
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## Mathematical Formulae

$$
\text { Total amount }=P\left(1+\frac{r}{100}\right)^{n}
$$

## Mensuration

Curved surface area of a cone $=\pi r l$
Surface area of a sphere $=4 \pi r^{2}$
Volume of a cone $=\frac{1}{3} \pi r^{2} h$
Volume of a sphere $=\frac{4}{3} \pi r^{3}$
Area of triangle $A B C=\frac{1}{2} a b \sin C$
Arc length $=r \theta$, where $\theta$ is in radians
Sector area $=\frac{1}{2} r^{2} \theta$, where $\theta$ is in radians

## Trigonometry

$$
\begin{gathered}
\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C} \\
a^{2}=b^{2}+c^{2}-2 b c \cos A
\end{gathered}
$$

## Statistics

$$
\begin{aligned}
\text { Mean } & =\frac{\sum f x}{\sum f} \\
\text { Standard Deviation } & =\sqrt{\frac{\sum f x^{2}}{\sum f}-\left(\frac{\sum f x}{\sum f}\right)^{2}}
\end{aligned}
$$

Answer all the questions.
1 (a) Express as a single fraction $\frac{3 x}{(x-3)^{2}}-\frac{7}{2 x-6}$.
(b) Simplify $\frac{2 s^{2}+9 s t-5 t^{2}}{3 s^{2}-75 t^{2}} \times \frac{s-5 t}{5}$.
(c) It is given that $\frac{1}{a}+\frac{1}{b}=\frac{1}{c^{2}}$.
(i) Find $b$ when $a=3, c=-1$.
(ii) Express $c$ in terms of $a$ and $b$.

2 (a) (i) The cash price of a particular car is $\$ 94000$.
Shawn decides to buy this car. He paid a deposit of $\$ 10000$ and the rest by monthly instalments of $\$ 1090$ over a period of $7 \frac{1}{2}$ years. The bank charges an interest of $i \%$ per annum on the amount loaned.

Calculate the value of $i$.
(ii) Betty buys an identical car which costs the same.

She pays a deposit of one-fifth of the cash price. She then borrows the remaining cost for 3 years at compound interest of $3 \%$ per year.

Calculate the total amount of money Betty paid for the car.
(b) The exchange rate between US dollars (\$) and Korean won (w) is $\$ 1=1082.50$.

Bill bought 166500 from the bank.
Calculate the total amount in US dollars he paid the bank. Leave your answer to the nearest dollar.

3 Ray represented his class in a 10 km race. He started running at a speed of $x \mathrm{~km} / \mathrm{h}$. After 2 km , he increased his speed by $1 \mathrm{~km} / \mathrm{h}$ and ran the remaining distance at this speed.
(i) Find and simplify, in terms of $x$, an expression for the time taken by Ray to complete the race.
(ii) Given that Ray's average speed for the whole race was $10.5 \mathrm{~km} / \mathrm{h}$, form an equation in $x$ and show that it reduces to $10 x^{2}-95 x-21=0$.
(iii) Solve the equation $10 x^{2}-95 x-21=0$. Give your answers correct to 2 decimal places.
(iv) Find the time, in hours, Ray would have taken if he had ran the entire race at his initial speed.

4 The diagram shows three points, $P, Q$ and $R$ on a piece of horizontal land. $P R=470 \mathrm{~m}$ and $Q R=318 \mathrm{~m}$.


It is given that $\sin \theta=\frac{7}{25}$ and $\theta$ is obtuse.
(a) Calculate the area of $\triangle P Q R$.
(b) Without the use of a calculator, show that the value of $\cos \theta=-\frac{24}{25}$.
(c) Hence, find the distance $P Q$.
(d) $T$ is the top of a building that is standing vertically at $R$ and the angle of elevation of $T$ from $P$ is $12^{\circ}$. Calculate the height of the building.
(e) Eli walks along the path $P Q$ until he reaches a point $E$. Calculate the largest angle of depression from $T$ to $E$.

5 The graph shows the cumulative frequency curve for the number of hours of community service accumulated over four years by 120 students in Vista Secondary School.

(a) Use your graph to find the
(i) median,
(ii) interquartile range,
(iii) percentage of students who accumulated more than 100 hours of community service.
(b) The number of hours of community service accumulated by another 120 students in Venus Secondary School is represented in the following box-and-whisker plot.


Make two comparisons between the number of hours the students spent on community service in the two schools.

6 Answer the whole of this question on a sheet of graph paper.
An analyst was studying the effect of the introduction of a new policy to a company's business profit. He felt that the amount of profit, $y$ hundred thousand dollars, over a period of $x$ months could be modelled by the equation

$$
y=\frac{x^{3}}{5}+\frac{10}{x}-10
$$

Some corresponding values of $x$ and $y$ are given in the following table.

| $x$ | 0.5 | 1.5 | 2 | 3 | 4 | 4.5 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | 10.03 | -2.66 | -3.4 | -1.27 | 5.30 | 10.45 | 17.00 |

(a) Using a scale of 2 cm to represent 1 unit, draw a horizontal $x$-axis for $0 \leq x \leq 5$.
Using a scale of 1 cm to represent 1 unit, draw a vertical $y$-axis for $-4 \leq y \leq 18$.
On your axes, plot the points given in the table and join them with a smooth curve.
(b) Use your graph to state the period when the company is suffering a loss.
(c) Use your graph to find the solution(s) to the equation $\frac{x^{3}}{5}+\frac{10}{x}=15$ in the range $0 \leq x \leq 5$.
(d) By drawing a tangent, find the gradient of the curve at $(1.5,-2.66)$.
(e) (i) On the same axes, draw the line $y=3 x+1$ for $0 \leq x \leq 5$.
(ii) The $x$-coordinates of the points where the line in (e)(i) intersects the curve are the solutions of the equation $x^{4}-a x^{2}-b x+50=0$. Find the value of $a$ and of $b$.

Sec 3E E.Maths EOY P1 2018 Solutions

| Qn | Solution | Marks |
| :---: | :---: | :---: |
| 1a | $\begin{aligned} & 1.12 \times 10 \times 10^{6} \\ & =11.2 \times 10^{6} \\ & k=11.2 \end{aligned}$ | B1 |
| 1b | $\begin{aligned} & \frac{16.5 \times 10^{9}}{1.12 \times 10^{7}} \\ & =\$ 1473.2142 \\ & =\$ 1473 \end{aligned}$ | B1 |
| 2 a | $\begin{aligned} & 5 x^{2} y^{-1} \times x^{-3} y \\ & =5 x^{-1} y^{0} \\ & =\frac{5}{x} \end{aligned}$ | B1 |
| 2b | $\begin{aligned} & \left(\frac{16}{x^{4}}\right)^{-\frac{1}{2}} \\ & =\left(\frac{x^{4}}{16}\right)^{\frac{1}{2}} \\ & =\frac{x^{2}}{4} \end{aligned}$ | B2 |
| 3 a | $\begin{aligned} & 3^{-0}+(9)^{-1}+3^{-2} \\ & =1+\frac{1}{9}+\frac{1}{3^{2}} \\ & =1 \frac{2}{9} \end{aligned}$ | B1 |
| 3b | $\begin{aligned} & \frac{8^{2 x-1}}{4}=\frac{1}{16^{x}} \\ & \frac{2^{3(2 x-1)}}{2^{2}}=\frac{2^{0}}{2^{4 x}} \\ & 6 x-3-2=0-4 x \\ & 6 x-5=-4 x \\ & 10 x=5 \\ & x=\frac{1}{2} \end{aligned}$ | M1 <br> (same base) M1 simplify A1 |
| 4a | 155 cm |  |
| 4b | $\begin{aligned} & \begin{array}{l} \text { Mean } \\ =\frac{1570}{10} \\ =157 \mathrm{~cm} \end{array} \end{aligned}$ | $\begin{array}{\|l} \text { M1 } \\ \text { A1 } \end{array}$ |


| 4c | $\frac{155+157}{2}=156$ |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 5 a | B1 |  |  |  |


| 6aii | Gradient of $A C=2 n$ $\begin{aligned} & \frac{b-2}{a-2}=2\left(\frac{1}{4}\right) \\ & 2 b-4=a-2 \\ & 2 b-a=2----(1) \end{aligned}$ <br> Gradient of $A B=n$ $\frac{b-4}{a+2}=\frac{1}{4}$ $4 b-16=a+2$ $\begin{equation*} 4 b-18=a \tag{2} \end{equation*}$ <br> Sub (2) into (1) $\begin{aligned} & 2 b-(4 b-18)=2 \\ & -2 b+18=2 \\ & b=8 \\ & a=4(8)-18 \\ & a=14 \\ & A(14,8) \end{aligned}$ | M1 <br> M1 <br> A1 |
| :---: | :---: | :---: |
| 6aiii | $\begin{aligned} & \text { Length of } B C \\ & =\sqrt{(-2-2)^{2}+(4-2)^{2}} \\ & =\sqrt{20} \\ & =4.4721 \\ & =4.47 \text { units } \end{aligned}$ | B1 |
| 6b | $\begin{aligned} & \frac{1}{2} \times \sqrt{20} \times h=12 \\ & h=5.3665 \\ & h=5.37 \text { units } \end{aligned}$ | M1 A1 |
| 7a | $\begin{aligned} & \frac{2}{3}(x+1) \leq x+2<-(2 x-9) \\ & \frac{2}{3}(x+1) \leq x+2 \\ & \frac{2}{3} x+\frac{2}{3} \leq x+2 \\ & -\frac{1}{3} x \leq 1 \frac{1}{3} \\ & x \geq-4 \\ & x+2<-(2 x-9) \\ & 3 x<7 \\ & x<2 \frac{1}{3} \\ & -4 \leq x<2 \frac{1}{3} \end{aligned}$ | M1 <br> M1 <br> A1 |


| 7b | 2 | B1 |
| :---: | :---: | :---: |
| 8a | Bearing of $C$ from $A$ $\begin{aligned} & =84^{\circ}+60^{\circ} \\ & =144^{\circ} \end{aligned}$ | B1 |
| 8b | $84^{\circ}-60^{\circ}=24^{\circ}$ <br> Bearing of $C$ from $B$ $\begin{aligned} & =180^{\circ}+24^{\circ} \\ & =204^{\circ} \end{aligned}$ | M1 A1 |
| 9a | $\begin{aligned} & \sin \theta=\frac{8}{12} \\ & \theta=0.72972 \\ & \angle P O Q=0.72972 \times 2 \\ & =1.45944 \\ & =1.46 \mathrm{rad} \text { (shown }) \end{aligned}$ | B1 |
| 9 b | $\begin{aligned} & \text { Reflex angle } P O Q \\ & =2 \pi-1.45944 \\ & =4.82374 \mathrm{rad} \\ & \text { Major } \operatorname{arc} P R Q \\ & =r \theta \\ & =12(4.82374) \\ & =57.88488 \\ & =57.9 \mathrm{~cm} \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \end{aligned}$ |
| 9c | Area of shaded region $\begin{aligned} & =\frac{1}{2}(12)^{2}(1.45944)-\frac{1}{2}(12)^{2} \sin 1.45944 \\ & =105.07968-71.55405 \\ & =33.52563 \\ & =33.5 \mathrm{~cm}^{2} \end{aligned}$ <br> OR $\begin{aligned} & \theta=1.45944 \times \frac{180^{\circ}}{\pi} \\ & =83.61975 \\ & \text { Area }=\frac{83.61975}{360} \times \pi(12)^{2}-\frac{1}{2}(12)^{2} \sin 83.61975 \\ & =33.5356 \\ & =33.5 \mathrm{~cm}^{2} \end{aligned}$ | M2 <br> A1 <br> M2 <br> A1 |
| 10a | $0 \mathrm{~m} / \mathrm{s}^{2}$ | B1 |
| 10b | $\begin{aligned} & \frac{v}{5}=\frac{18}{8} \\ & v=11 \frac{1}{4} \mathrm{~m} / \mathrm{s} \end{aligned}$ | B1 |


| 10c | $\begin{aligned} & \frac{1}{2} \times(15+t)(18)=450 \\ & 15+t=50 \\ & t=35 s \end{aligned}$ | M1 A1 |
| :---: | :---: | :---: |
| 10d | Answer | Shape - B1 <br> Indicate <br> correct <br> distance - <br> B1 |
| 11a | $\begin{aligned} \text { Mean } & =\frac{2510}{5} \\ & =502 \mathrm{~g} \end{aligned}$ <br> SD for Machine A $\begin{aligned} & =\sqrt{\frac{505^{2}+498^{2}+502^{2}+502^{2}+503^{2}}{5}-\left(\frac{2510}{5}\right)^{2}} \\ & =\sqrt{\frac{1260046}{5}-\left(\frac{2510}{5}\right)^{2}} \\ & =2.2803 \\ & =2.28 \end{aligned}$ | B1 <br> Either or M1 <br> A1 |
| 11b | I will recommend Machine A as the standard deviation is smaller which means the machine is more consistent in manufacturing the ice-cream tubs. | B1 |
| 12a | $\begin{aligned} & \sin \angle A C D=\frac{3}{4.8} \\ & \angle A C D=38.6821 \\ & =38.7^{\circ} \end{aligned}$ | M1 <br> A1 |


| 12b | $\begin{aligned} & \cos \angle B A C=\frac{4.8}{A B} \\ & \cos 38.6821=\frac{4.8}{A B} \\ & A B=\frac{4.8}{\cos 38.6821} \\ & A B=6.1489 \\ & A B=6.15 \mathrm{~cm} \end{aligned}$ | M1 <br> A1 |
| :---: | :---: | :---: |
| 12c | By Pythagoras' Thereom, $\begin{aligned} & C D=\sqrt{4.8^{2}-3^{2}} \\ & C D=3.74699 \end{aligned}$ <br> Area $\begin{aligned} & =\frac{1}{2} \times(6.1489+3.74699) \times 3 \\ & =14.8437 \\ & =14.8 \mathrm{~cm}^{2} \end{aligned}$ | M1 <br> A1 |
| 13 (i) | Since $\angle A O B=2 \times \angle A B D$, O is the centre of circle. ( $\angle$ at centre $=2 \angle$ at circumference) | B1 |
| 13(ii) <br> (a) | $\angle A C D=63^{\circ}(\angle \mathrm{s}$ in same segment) | B1 |
| 13(ii) <br> (b) | $\begin{aligned} & \angle O D A=\frac{180-126}{2}=27^{\circ}(\text { base } \angle \mathrm{s} \text { of isos. } \triangle) \\ & \angle B A D=180-63-20-27=70^{\circ}(\text { sum of } \angle \mathrm{s} \text { in } \triangle) \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \end{aligned}$ |
| 13 <br> (ii) <br> (c) | $\angle B C D=180-70=110^{\circ}$ ( $\angle \mathrm{s}$ in opp. segment) | B1 |
| $\begin{aligned} & 13 \\ & \text { (iii) } \end{aligned}$ | $\angle D B C=27^{\circ}(\angle \mathrm{s}$ in same segment) <br> Since $\angle \mathrm{ODB} \neq \angle \mathrm{DBC}$, OD is not parallel to BC . | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \end{aligned}$ |
|  |  |  |
|  |  |  |

3E EM P2 Marking Scheme

| Question | Marking Scheme | Marks |
| :---: | :---: | :---: |
| 1 (a) | $\begin{aligned} & \frac{3 x}{(x-3)^{2}}-\frac{7}{2(x-3)} \\ & =\frac{6 x-7(x-3)}{2(x-3)^{2}} \\ & =\frac{-x+21}{2(x-3)^{2}} \end{aligned}$ | M1 <br> M1 <br> A1 |
| 1 (b) | $\begin{aligned} & \frac{2 s^{2}+9 s t-5 t^{2}}{3 s^{2}-75 t^{2}} \times \frac{s-5 t}{5} \\ & =\frac{(2 s-t)(s+5 t)}{3(s-5 t)(s+5 t)} \times \frac{s-5 t}{5} \\ & =\frac{2 s-t}{15} \end{aligned}$ | M2 (cross method and diff of squares) |
| 1 (c) (i) | $\begin{aligned} & \frac{1}{3}+\frac{1}{b}=\frac{1}{1} \\ & \frac{1}{b}=\frac{2}{3} \\ & b=1 \frac{1}{2} \end{aligned}$ | M1 <br> A1 |
| 1 (c) (ii) | $\begin{aligned} & \frac{1}{a}+\frac{1}{b}=\frac{1}{c^{2}} \\ & \frac{b+a}{a b}=\frac{1}{c^{2}} \\ & c^{2}=\frac{a b}{b+a} \\ & c= \pm \sqrt{\frac{a b}{b+a}} \end{aligned}$ | A2 (A1 $\text { for } \pm \text { ) }$ |
| 2 (a) (i) | $\begin{aligned} & \text { Interest }=1090 \times 7.5 \times 12+10000-94000=\$ 14100 \\ & 14100=\frac{84000 \times i \times 7.5}{100} \\ & i=2 \frac{5}{21} \% \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { M1 } \\ & \text { A1 } \end{aligned}$ |


| 2 (a) (ii) | $\begin{aligned} & \text { Amount borrowed }=\frac{4}{5} \times 94000=\$ 75200 \\ & \text { Amount owed }=75200\left(1+\frac{3}{100}\right)^{3}=\$ 82173.0704 \\ & \text { Amount Betty paid }=82173.0704+\frac{1}{5} \times 94000 \\ & =\$ 100973.07(2 \mathrm{dp}) \end{aligned}$ | M1 <br> M1 A1 |
| :---: | :---: | :---: |
| 2 (b) | $\begin{aligned} & \text { Total amount }=\frac{101.5}{100} \times 166500 \div 1082.50 \\ & =\$ 153.81 \\ & =\$ 154 \end{aligned}$ | M1 A1 |
| 3 (i) | $\begin{aligned} \text { Time } & =\frac{2}{x}+\frac{8}{x+1} \\ & =\frac{2 x+2+8 x}{x(x+1)} \\ & =\frac{10 x+2}{x(x+1)} h \end{aligned}$ | M1 <br> A1 |
| 3 (ii) | $\begin{aligned} & \frac{10}{\frac{10 x+2}{x(x+1)}}=10.5 \\ & \frac{10 x(x+1)}{10 x+2}=10.5 \\ & 10 x^{2}+10 x=105 x+21 \\ & 10 x^{2}-95 x-21=0 \end{aligned}$ | M1 <br> M1 <br> M1 |
| 3 (iii) | $\begin{aligned} x & =\frac{95 \pm \sqrt{(-95)^{2}-4(10)(-21)}}{2(10)} \\ & =\frac{95 \pm \sqrt{9865}}{20} \\ & =9.7161 \text { or }-0.2161 \\ & =9.72 \text { or }-0.22 \end{aligned}$ | M1 <br> M1 <br> A1 |
| 3 (iv) | $\frac{10}{9.7161}=1.03 \mathrm{~h}$ | B1 |
| 4 (a) | $\begin{aligned} & \text { Area }=\frac{1}{2}(318)(470)\left(\frac{7}{25}\right) \\ & =20924 \frac{2}{5} m^{2} \end{aligned}$ | M1 <br> A1 |


| 4 (b) | $\sin \theta=\frac{7}{25}$ $\sin x=\frac{7}{25}$, where x is acute <br> By Pythagoras' Theorem, $\begin{aligned} & \operatorname{adj}=\sqrt{25^{2}-7^{2}}=24 \\ & \cos x=\frac{24}{25} \\ & \cos \theta=-\frac{24}{25} \end{aligned}$ | M1 <br> A1 |
| :---: | :---: | :---: |
| 4 (c) | $\begin{aligned} & P Q^{2}=318^{2}+470^{2}-2(318)(470)\left(-\frac{24}{25}\right) \\ & P Q=\sqrt{318^{2}+470^{2}-2(318)(470)\left(-\frac{24}{25}\right)} \\ & =780.3763 \\ & =780 \mathrm{~m}(3 \mathrm{sf}) \end{aligned}$ | M2 <br> A1 |
| 4 (d) | $\begin{aligned} & \tan 12^{\circ}=\frac{T R}{470} \\ & T R=470 \tan 12^{\circ} \\ & =99.9015 \\ & =99.9 \mathrm{~m}(3 \mathrm{sf}) \end{aligned}$ | M1 <br> A1 |
| 4 (e) | Let the perpendicular dist be $h$. $\begin{aligned} & \frac{1}{2}(h)(780.3763)=20924 \frac{2}{5} \\ & h=53.6264 \\ & =53.6 \mathrm{~m}(3 \mathrm{sf}) \end{aligned}$ <br> Let the angle of depression be x . $\begin{aligned} & \tan x=\frac{99.9015}{53.6264} \\ & x=61.7734 \\ & =61.8^{\circ}(1 d p) \end{aligned}$ | M1 <br> M1 <br> A1 |
| 5 (a) (i) | 70 hours | B1 |
| 5 (a) (ii) | $\begin{aligned} & \mathrm{Q} 3=84 \\ & \mathrm{Q} 1=54 \\ & \mathrm{IQR} \\ & =84-54 \\ & =30 \text { hours } \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \end{aligned}$ |
| 5 (a) (iii) | $\begin{aligned} & \frac{120-112}{120} \times 100 \% \\ & =6 \frac{2}{3} \% \end{aligned}$ | M1 <br> A1 |
| 5 (b) | IQR for Venus Sec |  |



