Class:

YIO CHU KANG SECONDARY SCHOOL END-OF-YEAR EXAMINATION 2018 SECONDARY TWO EXPRESS

MATHEMATICS Paper 1

1 hour

8 October 2018 (Monday)

READ THESE INSTRUCTIONS FIRST

Candidates answer on the Question Paper.

Write your index number and name on all the work you hand in. Write in dark blue or black pen. You may use a HB pencil for any diagrams or graphs. Do not use staples, paper clips, glue or correction fluid.

Answer all the questions. The number of marks is given in brackets [] at the end of each question or part question.

If working is needed for any question it must be shown with the answer. Omission of essential working will result in loss of marks. The total of the marks for this paper is 40.

The use of an approved scientific calculator is expected, where appropriate. If the degree of accuracy is not specified in the question and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For π , use either your calculator value or 3.142.

Setter: Miss Chia Yi Ying







Compound interest

Total Amount =
$$P(1 + \frac{r}{100})^n$$

Mensuration

Curved surface area of a cone = $\pi r l$ Surface area of sphere = $4\pi r^2$ Volume of cone = $\frac{1}{3}\pi r^2 h$ Volume of sphere $\frac{4}{3}\pi r^3$



During a production, a batch of 25 light bulbs were produced. In this batch, 5 light bulbs were 1 defective. One bulb was chosen at random. It was defective and thrown away. A second bulb was chosen at random.

Find the probability that the second bulb was not defective.

Answer [2] EDUC Factorize $4ab - 10c + 6a^2b - 15ac$ completely. 2 Write down the coordinates of the points where the curve y = (4x+1)(1-x) meets the 3 ANYAL

x-axis.

Answer	(,)	[1]
	and			

(.....) [1]

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The diagram below shows a vertical flagpole *PC* placed at the top of the hill. *B* is vertically below *C* and angle $ABC = 90^{\circ}$, angle $PAB = 18^{\circ}$, AB = 120 m and AC = 125 m. 4



Find the height of the flagpole.

.

Answer m [3]

2E END-OF-YEAR EXAM 2018 263

5 The diagram below shows two similar trapeziums, *ABCF* and *FCDE*.



Given that FC = 3.6 cm, DE = 9 cm and AF = 1.5 cm, find the



(b) the length of FE.





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In the diagram above, triangle PQR is an isosceles triangle with PQ = PR = a cm and QR = 10 cm.

(a) Express in terms of a,

6

(i) the value of $\cos \angle PQR$,

(ii) the shortest distance from P to QR.

(b) Given that a = 13, find the value of $\sin \angle PRQ$. Leave your answer as a fraction.

 $32wu^2 - 18wv^2$, (a)

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(b) $3x^2 - 13x - 30$.

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- 8 The graph of y + x = 2 is drawn on the grid below.
 - (a) Complete the table for y = x and draw its graph on the grid below.



[2]

(b) From the graph, solve the following simultaneous equations.

$$y + x = 2$$

$$y = x$$

Answer $x = \dots$ [1]

y = [1]

2E END-OF-YEAR EXAM 2018

- 9 The force of attraction, F (in N), between 2 magnets is inversely proportional to the square of the distance, x (in cm), between the magnets. When the magnets are 2 cm apart, the force is 5 N.
 - (a) Find the equation connecting F and x.

(b) Find the percentage decrease in the force of attraction when the distance between them is doubled.

-

Answer% [2]

2E END-OF-YEAR EXAM 2018 267

10 A rubber cone of diameter 6 cm, height 10 cm and slant height 10.5 cm is cut in half to make two rubber door stoppers.



Find

(a) the volume of each rubber stopper,

(b) the surface area of each rubber stopper.

Answer cm^2 [2]

11

11 (a) Expand (a+b)(a-b).

(b) _W

Without using a calculator, use algebraic rules to evaluate $\frac{121}{121^2 - 125 \times 117}$. Leave your answer as a fraction.

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- 12 The back-to-back stem-and-leaf diagram shows the Test 1 and Test 2 scores of a class of 10 students.

12

Leaves for Test 1 scores	Stem	Leaves for Test 2 scores
74	3	
3 1 0	4	9
981	5	8
7 3	6	0 3 5 6
	7	4 4
	8	0 3

Stem | Leaves Key: 3 | 4 means 34 marks

(a) Given that the passing marks for both tests is 50, find the percentage of students who passed

(i) Test 1,

(ii) Test 2.

(b) Find the ratio of students who score above 50 but less than 65 in Test 2 to those in Test 1.

(c)	Which test is easier?	
	Give a reason to justify your answer.	3.
		1
		•••••
		[1]

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YIO CHU KANG SECONDARY SCHOOL END-OF-YEAR EXAMINATION 2018 SECONDARY TWO EXPRESS



MATHEMATICS

Paper 2

1 hour 30 minutes

Additional materials: Answer Paper Graph Paper (1 sheet) 11 October 2018 (Thursday)

READ THESE INSTRUCTIONS FIRST

Write your index number and name on all the work you hand in. Write in dark blue or black pen on both sides of the paper. You may use a HB pencil for any diagrams or graphs. Do not use staples, paper clips, glue or correction fluid.

Answer all questions.

If working is needed for any question it must be shown with the answer.

Omission of essential working will result in loss of marks.

The use of an approved scientific calculator is expected, where appropriate. If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place. For π , use either your calculator value or 3.142, unless the question requires the answer in terms of π .

At the end of the examination, fasten all your work securely together. The number of marks is given in brackets [] at the end of each question or part question. The total number of marks for this paper is 60.

For Exami	ner's Use
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	60

Setter: Madam Lee Ching Fong

Mathematical Formulae

Mensuration

Curved surface area of a cone = πrl Surface area of a sphere = $4\pi r^2$ Volume of a cone = $\frac{1}{3}\pi r^2 h$ Volume of a sphere = $\frac{4}{3}\pi r^3$

2E END-OF-YEAR EXAM 2018 276

The quantity of paint needed to cover the outside of a container is proportional to the square of the depth of the container.
 When the depth is 50 cm, the quantity of paint needed is 1500 ml.

Calculate

(a) the quantity of paint needed when the depth is 70 cm. [2]

[2]

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- (b) the depth when the quantity of paint needed is 540 ml.
- 2 The following table shows the age group of members of a country club.

	Age	e (years)	$35 < x \le 40$	$40 < x \le 45$	$45 < x \le 50$	$50 < x \le 55$	$55 < x \le 60$	
	No. mer	of nbers	20	k	75	80	90	
	(a)	Write down	the largest val	ue of <i>k</i> such th	at $55 < x \le 60$	is the modal ag	ge group.	[1]
	(b)	Write down	the smallest v	alue of k such t	hat the median	n group is 45 <	$x \leq 50$.	[1]
	(c)	If $k = 50$, fi	nd the mean ag	e group, correc	et to 2 decimal	places.	5	[2]
3	An a	ctual distanc	e of 60 km bet	ween two point	s on a map is r	epresented by	a length of 20 c	m.
	(a)	Find the sca	ale of the map	in the form of 1	: <i>n</i> .			[1]
	(b)	Given that a diameter of	a circular field the field.	has an area of	12.5 cm^2 on the	e map, calculat	e the actual	[3]
4	Jenn y km	ifer drove 4 l /h.	hours at an ave	rage speed of x	km/h and ther	n for 6 hours at	an average spe	ed of
	She	drove a total	distance of 810	6 km.				
	(a)	Write down $2x + 3y = 4$	n an equation in 408.	terms of x and	d y, and show t	hat it simplifie	s to	[1]
(b) Kenny drove for 3 hours at an average speed of x km/h and then for 5 hours at an average speed of y km/h.								
		He drove a	total distance of	of 654 km.				
		Write down	n an equation, i	n terms of x and	d y , to represent	nt these inform	ation.	[1]

(a) It is given that $a = \frac{4b - 5c}{b + c}$. 5

- (i) Find a when b = 4 and c = -1. [1]
- (ii) Express b in terms of a and c. [2]
- (b) Given that $(2x-2y)^2 = 16$ and $x^2 + y^2 = 8$, find the value of xy. [3]
- The diagram shows a circular area. Three points, P, Q and R are on the circumference of the circle 6 and O is the centre of the circle.



	(a)	Show that triangle PQR is a right angled triangle.	[2]
	(b)	Hence, find the area of triangle PQR.	[2]
	(c)	An object falls within the circular area, find the probability that the object will land within triangle <i>PQR</i> . Leave your answer in 3 significant figures.	[2]
7	(a)	Expand and simplify $(2-5x)^2 - (x-2)(2x+1)$.	[2]
	(b)	Simplify $\frac{x^2 - 9}{x^2 - 4x - 21} \div \frac{3x - 6}{3x - 21}$.	[2]
	(c)	Express as a single fraction in its simplest form $\frac{3}{(5-x)} - \frac{5}{(x-5)^2}$.	[3]



8 Two triangles, A and B, each has a vertical height of x cm and (x + 3) cm respectively. The area of the triangles A and B are 30 cm² and 32 cm² respectively.



(a) Find, in terms of x, an expression for the length of the base of

(i) triangle A,
(ii) triangle B.

(b) Given that the length of the base of tringle A is 4 cm more than that of triangle B, form

an equation in x and show that it reduces to $x^2 + 4x - 45 = 0.$ [3]

[3]

[1]

[3]

[1]

1

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(c) Solve the equation and find the vertical height of triangle B.

9 Answer the whole of this question on a sheet of graph paper.

The variables x and y are connected by the equation

$$y = 4x^2 - 40x + 100.$$

Some corresponding values of x and y are given in the following table.

x	2	3	4	5	6	7	8
у	36	р	4	0	4	16	36

(a) Find the value of p.

- (b) Using a scale of 2 cm to represent 1 unit on the horizontal x-axis and 2 cm to represent 5 units on the vertical y-axis, draw the graph of $y = 4x^2 40x + 100$ for $2 \le x \le 8$.
- (c) From the graph, find the

(i) equation of the line of symmetry, [1]

- (ii) values of x when y = 25, [2]
- (iii) coordinates of the minimum point.

10 (a) The candle in diagram I can be modelled by the pyramid ABCDE in diagram II. ABCD is a square of side 8 cm and AE = BE = CE = DE = 10 cm.



(ii) Calculate the amount of wax needed to make one candle.

[2]

[2]

(b) Another candle is made in the shape of a hemisphere. The volume of this candle is the same as the volume of candle ABCDE.

Show that the radius of the hemisphere is 4.38 cm, correct to 3 significant figures. [2]

(c) The diagram shows the plan view of a box holding six of the hemispherical candles. The box is in the shape of a cuboid and the candles just fit into the box.



Calculate the volume of the box.

[2]

Yio Chu Kang Secondary School 2018 End-of-Year Examination Sec 2 Express Maths Paper 1 Marking Scheme

1.	Probability = $\frac{25-5}{25-1}$	[M1]
	25-1	
	$=\frac{5}{6}$	[A1]
	0	
2	$4ab-10c+6a^2b-15ac$	
	$=4ab+6a^2b-10c-15ac$	
	=2ab(2+3a)-5c(2+3a)	[M1]
	=(2+3a)(2ab-5c)	[A1]
	AV	A
3	$\left(-\frac{1}{2},0\right)$	[B1]
		0
	and $(1 0)$	
	(1,0)	
4	$\tan 18^\circ - \frac{PB}{2}$	N
	$\frac{1}{120}$	5
	$PB = 120 \times \tan 18^{\circ}$	
	= 38.990 (5 \$.2)	600.3
	By the Pythagoras Theorem, J	2800
	$(125^2 \neq 120^2 + BC^2)$	IN .
	$\sqrt{200^2 = 125^2 - 120^2}$	
	BC= 1252 -1202 05 5 matsar	[M1]
	Height offamole=38 990-35-iNer	
	Theight of thighest to 200 a 2001	
	-300 m (3 s f)	[A1]
	ISLATALY III (5 S.I.)	
5	(a) $AB FC$	DECARO
	$\overline{FC} = \overline{ED}$	
	$=\frac{3.6}{1}$	
	9	
	$=\frac{2}{2}$	[A1]
	5	
	(b) $FE ED$	
	$\overline{AF} = \overline{FC}$	
	FE 9	× 11
	$\frac{1.5}{1.5} = \frac{1}{3.6}$	[M1]
	$FE = \frac{9}{1.5} \times 1.5$	
	3.6	F & 13
	= 3.75 cm	[AI]

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Yio Chu Kang Secondary School 2018 End-Of-Year Examination Sec 2 Express Maths Paper 2 Marking Scheme

1	(a)	$V = kd^2$ When $d = 50cm$, $V = 1500ml$,	
		$1500 = k(50)^2$	
		, 1500	
		$\kappa = \frac{1}{50^2}$	
		_ 3	
		$-\frac{1}{5}$	
		$V = \frac{3}{2}d^2$	
		5	
		When $d = 70 \text{ cm}$	
		when $a = 70 \text{ cm}$	[M1]
		$V = \frac{1}{5} \times 70^2$	
		= 2940 ml	[A1]
	(b)	When $V = 540ml$,	
		$\frac{3}{2}d^2 - 540$	
		5 ^u - 540	
		$d^2 = \frac{540 \times 5}{3} \qquad (2)$	[M1]
		= 900	
		$d = \pm \sqrt{900}$	
	<	======================================	
		a/= 30 cm	[A1]
2	(a)	A Egg UU and	
		Largest value of to = 89 Bill	[A1]
	(b)	k + 20 + 74 = 80 + 90 : 000	
	(~)	$k = 170^{-94}$	
		15/76	[A1]
		Smallest value of $k = 76$	
	(c)	Mean age group = $37.5 \times 20 + 42.5 \times 50 + 47.5 \times 75 + 52.5 \times 80 + 57.5 \times 90$	
		20 + 50 + 75 + 80 + 90	[M1]
		$=\frac{15812.5}{1}$	
		315	
		= 50.1984	
		= 50.20 (2 dp)	[A1]
3	(a)	20 cm : 60 km	
		1 cm : 300 000 cm	· · ·
		1 : 300 000	[A1]
	(b)	1 cm : 3 km	
	. /	$(1 \text{ cm})^2$: $(3 \text{ km})^2$	
		1 cm^2 : 9 km ²	

	(b)	Actual area = 12.5×9 = 112.5 km^2	[M1]	
		$\pi r^2 = 112.5$ $r^2 = \frac{112.5}{\pi}$	[M1]	
		$r = \sqrt{\frac{112.5}{\pi}}$ $= 5.9841$	•	
		$d = 2 \times 5.9841$ = 11.968 km = 12 .0 km (3 sf)	[A1]	
4	(a)	4x + 6y = 816	NYAL	
		2x + 3y = 408 (shown)	[B1]	
	(b)	3x + 5y = 654	[B1]	
	(C)	2x + 3y = 408(1)	IN S	
	а.	3x + 5y = 654(2)	265	
		(1) x 3 => $6x + 9y = 1224$ (3)		
		(2) x 2 => $6x + (0y = 1308 - (4))$	66005	
		(4) - (3) = (6x + 10y) - (6x + 9y) = 1308 -	1224 80°	
	4	1 9=84	pp (M1]	
	$\langle \rangle$	Substitute $y \neq 84$ into (1) (3) mat 30	[A1]	
		2x+3(84) = 408		
		=.150		
		andw156		
		$\sqrt{5}\sqrt{\alpha} x = \frac{1}{2}$		
		= 78	EDUC	



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 $\therefore x = 78, y = 84$

5 (a) (i)
$$a = \frac{4b-5c}{b+c}$$

 $= \frac{4(4)-5(-1)}{4+(-1)}$
 $= \frac{16+5}{3}$
 $= 7$

[A1]

(ii)
$$a = \frac{4b - 5c}{b + c}$$

 $a(b + c) = 4b - 5c$ [M1]
 $ab + ac = 4b - 5c$
 $ab - 4b = -5c - ac$
 $b = \frac{-5c - ac}{a - 4}$ or $b = \frac{-c(5 + a)}{a - 4}$ [A1]
(b) $(2x - 2y)^2 = 16$
 $4x^2 - 8xy + 4y^2 = 16$
 $x^2 - 2xy + y^2 = 4$
 $x^2 + y^2 - 2xy = 4$ [M1]
Given $x^2 + y^2 = 8$
 $8 - 2xy = 4$
 $-2xy = 4 - 8$
 $xy = \frac{4 - 8}{-2}$
 $= 2$ [A1]
6 (a) $PQ^2 + QR^2 = 9^2 + 7^2$
Thangle $PQR^2 = 9R^2$
Thangle PQR^3 anyth angle angles. [A1]
 $PR^2 = (\sqrt{130})^{4}$ [A1]
6 (c) $P_{(mage + PQR)} = \frac{31.5}{\pi(\frac{\sqrt{130}}{2})^2}$ [M1]
 $= \frac{31.5}{\pi(\frac{\sqrt{130}}{4})^2}$ [M1]
 $= 0.3085$
 $= 0.309 (35f)$ [A1]

7 (a)
$$(2-5x)^2 - (x-2)(2x+1) = 4 - 20x + 25x^2 - [2x^2 + x - 4x - 2]$$
 [M1]
= $4 - 20x + 25x^2 - 2x^2 - x + 4x + 2$
= $23x^2 - 17x + 6$ [A1]

(b)
$$\frac{x^2 - 9}{x^2 - 4x - 21} \div \frac{3x - 6}{3x - 21} = \frac{(x + 3)(x - 3)}{(x - 7)(x + 3)} \times \frac{3(x - 7)}{3(x - 2)}$$
[M1]

$$=\frac{x-3}{x-2}$$
 [A1]

15.1

100



= 8 cm

9	(a) $p = 16$	[B1]
	(b) (See below) Correct scale and axes Points plotted correctly Smooth curved line drawn with labelling	[S1] [P1] [L1]
	(c) (i) From the graph, equation of the line of symmetry is $x = 5$	[B1]
	(ii) From the graph, $x = 2.5 \pm 0.1$ and $x = 7.5 \pm 0.1$ (iii) From the graph, coordinates of the minimum point is (5, 0)	[B1]+[B1] [B1]
(b)	29	
	Some Some	en ze sxis its on y-axis
	40	32
	To Contracts appoint of the second se	4
	20 Estandivide Opiniu Islandivide Opiniu	y=4x24px+100
	10	
	cc7c51 2 x-25 3 4 5670107 6 7x	X 3 X

10 (a) (i)
$$AC = \sqrt{8^2 + 8^2} = \sqrt{128}$$

 $OC = \frac{\sqrt{128}}{2}$
Height of pyramid $= \sqrt{10^2 - (\frac{\sqrt{128}}{2})^2}$ [M1]
 $= 8.2462$
 $= 8.25 \text{ cm (3sf)}$ [A1]
(ii) Volume of pyramid candle $= \frac{1}{3} \times 8^2 \times 8.2463$ [M1]
 $= 175.919 \text{ cm}^3$
 $= 176 \text{ cm}^3 (3sf)$ [A1]
(b) Volume of hemisphere = volume of pyramid
 $\frac{2}{3} \times \pi r^3 = 175.919$ [M1]
 $r^3 = \frac{175.919 \times 3}{2\pi}$
 $= 83.995$
 $r = \sqrt{38.3995}$
 $= 4.3794 \text{ cm}$
 $= 4.38 \text{ cm (3sf)} (\text{shown)}$ [A1]
(c) Length of box = $6x 4.3794 \text{ cm}$ [A1]
Breadth of box = $4x 4.3794 \text{ cm}$ [A1]
Height of box = 26.277 cm [A1]
Height of box = $26.272 \text{ cm}^3/5.17 \times 4.3794$ [M1]
 $= 20159 \text{ cm}^3$ (3sf) [A1]

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