

NORTH VISTA SECONDARY SCHOOL

END-OF-YEAR EXAMINATIONS 2018

(



NAME: _____

) CLASS: ____

SUBJECT: MATHEMATICS (PAPER 1)

LEVEL/STREAM: SECONDARY 2 EXPRESS

DATE: 4 OCTOBER 2018

TIME: 1 HOUR

READ THESE INSTRUCTIONS FIRST

Write your register number and name on all the work you hand in. Write in dark blue or black pen.

You may use a pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer all questions.

If working is needed for any question, it must be shown with the answer.

Omission of essential working will result in loss of marks.

The use of an approved scientific calculator is expected, where appropriate.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For π , use either your calculator value or 3.142, unless the question requires the answer in terms of π .

The number of marks is given in brackets [] at the end of each question or part question. The total of the marks for this paper is 40.

For Examiner's Use						
Category Question No.						
Accuracy						
Brackets						
Fractions						
Units						
Others						
Marks Deducted						

This paper consists of 9 printed pages.

[Turn Over

Answer all the questions.

1 Simplify (a) -4(2x-5)+2-(x-1),

Answer (a)[1]

(b) $(2x+1)^2 - (x-3)^2$.

Answer (b)[2]

2

It is given that a+b=5 and ab=-3. Find the value of a^2+b^2 . 2



Answer[2]

4 Factorise

(a)
$$\frac{x}{2} - 3xy + x^2$$
,

(b)
$$2p(1-4q)-(4q-1)$$
.

5

6

The diagram below shows three identical circles fitted inside a rectangle. The diameter of each circle is 10 cm. Line *EF* passes through the centre of the circle.



Find the length of line BF.



It is given that $V = \frac{1}{3}\pi r^2 h$. (a) Find the value of V when $\pi = \frac{22}{7}$, r = 9 and h = 21.

(b) Express r in terms of V, π and h.

7 Trapezium *ABCD* is congruent to the trapezium *PQRS*. It is given that AD = 24 cm, CD = 35 cm, angle $DAB = 130^{\circ}$ and angle $BCD = 78^{\circ}$.



4₄ 80

It is given that AC = 15 cm, AD = 12 cm, BC = 26 cm and CD = 9 am.



- (a) Expressing as a fraction in its lowest form, find
 - (i) $\tan \angle ACD$,
 - (ii) $\sin \angle BAD$.

(b) Find the shortest distance from C to AB.

Answer (b) cm [2]

- 10 A map of Singapore has a scale of 1: 250 000.
 - (a) The length of the Singapore river on the map is 1.2 cm.Calculate the actual length, in kilometres, of the Singapore river.





Answer (a) km [1]

(b) The area of Sentosa is 4.71 km².
 Calculate, the area, in square centimetres, of Sentosa on the map.

17. ...

1.5

Answer (b) cm^2 [2]

11 The solid shown below consists of a solid cone attached to a solid hemisphere. The base radius of the cone is 8 cm and the height of the solid is 23 cm.



(a) Given that the slant height of the cone is 17 cm, explain why angle $ABC = 90^{\circ}$.

Answer			· · · · · · · · · · · · · · · · · · ·	
	••••••	••••••		•••••
		••••••	•••••	•••••
				[2]
			••••••••	[2]

- (b) Calculate
 - (i) the total surface area of the solid,

 $. \text{ cm}^2$ [2] Answer (b)(i)

(ii) the volume of the solid.

12 The table below shows the pocket money of 20 students, rounded off to the nearest whole number.

23	24	23	25	20
21	20	24	22	21
23	25	25	20	23
23	20	21	22	25

(a) Draw a dot diagram to represent the information in the table.

Answer

- (b) Find the modal amount of pocket money.
- Answer (b) \$.....[1]

[2]

(c) Explain two limitations of using a dot diagram.
Answer
(d) Is a line graph a suitable way to represent the data? Explain your answer.
Answer
(1]

END OF PAPER

Question that are similar to P2 and thus removed:

11 The following stem-and-leaf diagram shows the English and Mathematics scores of a class of 20 students.

Leaves for English scores					Stem	Le	eave	es f	or	Ma	the	mai	tics	sco	ores		
					×.		3	8			2						
				0	3	5	4	9	5	3							
		2	3	4	4	6	5	9	7	5	4	4	4	3			
	5	6	7	7	8	9	6	8	7	6	4	3	0				
		3	4	5	6	9	7	5	4	1							
						0	8										

Key: 5 | 0 means 50 marks

(a) Find the modal score in the Mathematics test.

Answer (a) marks [1]

(b) Find the ratio of students who scored more than 50 marks in the English test to those in the Mathematics test.

Answer	(b)		:		[2]	
--------	-----	--	---	--	-----	--

(c) Which test is easier? Give a reason to justify your answer.

Answer	(c)	
		[2]

7 Trapezium *ABCD* is similar to the trapezium *PQRS*. It is given that AD = 24 cm, CD = 35 cm, RQ = 12 cm, $\measuredangle DAB = 130^{\circ}$ and $\measuredangle BCD = 78^{\circ}$.





NORTH VISTA SECONDARY SCHOOL

END-OF-YEAR EXAMINATION 2018



NAME:

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_		1

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SUBJECT: MATHEMATICS (PAPER 2)

DATE: 8 OCTOBER 2018

LEVEL/STREAM: SECONDARY 2 EXPRESS

TIME: 1 HOUR 30 MINUTES

READ THESE INSTRUCTIONS FIRST

Write your register number and name on all the work you hand in. Write in dark blue or black pen.

You may use a pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer all questions.

If working is needed for any question, it must be shown with the answer.

Omission of essential working will result in loss of marks.

The use of an approved scientific calculator is expected, where appropriate.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For π , use either your calculator value or 3.142, unless the question requires the answer in terms of π .

The number of marks is given in brackets [] at the end of each question or part question. The total of the marks for this paper is 60.

For Examiner's Use						
Category	Question No.					
Accuracy						
Brackets						
Fractions						
Units						
Others						
Marks Deducted						

This paper consists of 12 printed pages.

The stem-and-leaf diagram shows the distance Edward run to prepare for his 1 physical fitness test.



Calculate

- the mean distance, (i)
- the median distance, (ii)
- (iii) the modal distance.

[1] [1] [1]

[2]

1.7 *

1

EDUCATIO [1]

- The displacement, s metres of a car is directly proportional to the square of its 2 velocity, v metres per second. The car with velocity 26 m/s has a displacement of 3380 m.
 - Express s in terms of v. (a)
 - Calculate the displacement of the car with a velocity of 12 m/s. **(b)**

3 If $y = \frac{x+1}{x-1}$, express x in terms of y.

4 The table shows information about a group of students in a class.

	Boys	Girls
Wear spectacles	2	5
Do not wear spectacles	21	12

- (i) A member of the group is selected at random.Find the probability that the student(a) is a boy,
 - (b) does not wear spectacles.

is $\frac{1}{36}$.

(ii) Calculate the number of students to be removed so that the probability of drawing a girl who wear spectacles from the remaining students in the class

[2]

[1]

[1]

[3]

3

5 The diagram shows a part of a polygon shaped bracelet made up of identical triangles. $\angle CDE = 150^{\circ}$.



(a) Calculate the

(i) number of triangles used to make a bracelet,
(ii) sum of interior angles of the polygon formed by the bracelet.

(b) Calculate ∠ADE.

5

6 Simplify the following algebraic fractions.

(a)
$$\frac{b}{7c^2} \times \frac{2}{bc} \div \frac{1}{c^2}$$
,
(b) $4r^2 - v^2$ 5

$$\frac{4x^2 - y^2}{2x + y} \times \frac{5}{x^2 - 6x - 7}$$

[2]

[3]

7 In the diagram $\triangle PQR$ is similar to $\triangle ABC$. It is given that PR = 12 cm, $PQ = (x^2 - 4)$ cm, AB = x cm and AC = 6 cm. $\angle PQR = 60^\circ$ and $\angle ACB = 40^\circ$.



- (a) Calculate the value of x.
- (b) Calculate reflex $\angle BAC$.

[3] [2]

2

1

DANVAL

- 2 5 x x *x*+1 х 17
- By considering the area, show that $5x^2 + 19x 4 = 0$. (a) Hence, solve $5x^2 + 19x - 4 = 0$ **(b)** Calculate the perimeter of the playground. (c)
- 8 The diagram shows the shape of a children playground with an area of 21 m^2 .

[3]

[2]

[1]

9 The diagram shows a frame that is used to support a hanging weight. *ABC* is a vertical beam and *BED* is a horizontal beam. *AD*, *AE* and *CD* are three supporting struts.



[1]

[2]

[2]

[2]

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1.10

Given that BE = 5 m, BC = 8 m, AE = 7 m and $\angle BDC = 20^{\circ}$, calculate

- (a) the length of AB,
- (b) the length of CD,
- (c) the length of ED,
- (d) $\angle BDA$.

- 10 A car park can accommodate cars and buses. On a particular day there were x buses and y cars in the car park, giving a total of 500 vehicles. The parking area for a bus is 50 m² and the parking area for a car is 10 m². On that day a total area of 8000 m² was occupied by buses and cars.
 - (i) Write down a pair of simultaneous equations to represent the above [2] information.
 - (ii) Solve your simultaneous equations to find the value of x and of y.

There is a flat rate charge per day for parking.

The flat rate for buses is 2 times that for cars. On that day, an income of \$2300 was earned by the company.

(iii) Calculate the flat rate of the car.

[1]

[3]

11 A manufacturer decides to produce solid ornament of mass 3500g floating in a container filled with liquid. The ornament is made up of a cone and a hemisphere. The diameter of the cone and the hemisphere are 6 cm and 26 cm respectively. The height of the cone is 15 cm.



- (a) Calculate the surface area of the ornament.
- (b) The table shows the density of three liquids.

	Liquid A	Liquid B	Liquid C
Density (g/ cm ³)	0.6	0.7	0.8

Determine which liquid the manufacturer will use to fill the container. Justify your decision with calculations.

[Curved surface area of cone = πrl , Surface area of sphere = $4\pi r^2$]

[Volume of cone = $\frac{1}{3}\pi r^2 h$, Volume of sphere = $\frac{4}{3}\pi r^3$]

[3]

[4]

14

....

Answer the whole of question 11 on this page.

12 Answer the whole of this question on a sheet of graph paper.

A model rocket is launched straight upward. The solid fuel propellant pushes the rocket off the ground.

The height y metres of the rocket above ground level at time x seconds is given by $y = -4x^2 + 50x$ for $0 \le x \le 8$. The following table shows some corresponding values of x and y.

x	0	2	4	6	8	10	12	12.5
v	0	84	a	156	144	100	24	0

- [1] Calculate the value of a. (a) Using 2 cm to represent 2 seconds, draw a horizontal x-axis for $0 \le x \le 14$. **(b)** Using 2 cm to represent 20 m, draw a vertical y-axis. On your axes, plot the points given in the table and join them with a smooth [3] curve. Using your graph, (c) (i) find the values of x when the rocket is 80 m from the ground, [1] (ii) write down the equation of the line of symmetry of the graph. [1] [1]
- From the graph, find the maximum height reached by the rocket. (d)

12

End of Paper

	NORTH VISTA SECONDARY	SCHOOL	
Contraction of the second seco	END-OF-YEAR EXAMINATIO Answer Scheme	ONS 2018	40
AME:) CLASS: _	
SUBJECT: MA	THEMATICS (PAPER 1)	DATE:	
EVEL/STREAM	I: SECONDARY 2 EXPRESS	TIME: 1 H	OUR
	UCATION	0	UCATION
READ THESE I	NSTRUCTIONS FIRST	ET >	2
Vrite your registe Vrite in dark blue You may use a pe Do not use staple	r number and name on all the work you he or black pen. encil for any diagrams or graphs. s, paper clips, highlighters, glue or correcti	on fluid.	,0031
Answer all question f working is need Omission of essen The use of an app	ons. ed for any question, it must be shown with itial working will result in loss of marks. proved scientific calculator is expected, whi	the answer?	st event give the
f the degree of action answer to three since π , use either of π .	scuracy is not specified in the question, and gnificant figures. Give answers in degrees your calculator value or 3,642, unless the	to one decimal plac question requires the	texact, give the ce. he answer in terr
The number of ma The total of the m	arks is given in brackets [] at the end of earks for this paper is 40.	ach question or par	t question.
	10	For Exa	miner's Use
		Category	Question No.
		Accuracy	
		Brackets	
		Fractions	
		Units	

This paper consists of 9 printed pages.

Others

Marks Deducted 18

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-

Answer all the questions.

1 Simplify

(a) -4(2x-5)+2-(x-1),

$$-4(2x-5)+2-(x-1) = -8x+20+2-x+1 = -9x+23 \quad ----- B1$$



3 Write as a single fraction in its simplest form $\frac{2x}{(2x-3)^2} - \frac{1}{2x-3}$.

$$\frac{2x}{(2x-3)^2} - \frac{1}{2x-3} = \frac{2x - (2x-3)}{(2x-3)^2} \quad \text{or} \quad \frac{2x - 2x + 3}{(2x-3)^2} \quad --- \text{M1}$$
$$= \frac{3}{(2x-3)^2} \quad --- \text{A1}$$



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The diagram below shows three identical circles fitted inside a rectangle. The diameter of each circle is 10 cm. Line EF passes through the centre of the circle.

4



Find the length of line BF.



Express r in terms of V, π and h. (b)

$$V = \frac{1}{3}\pi r^{2}h$$

$$\pi r^{2}h = 3V$$

$$r^{2} = \frac{3V}{\pi h} \quad ---- \text{ M1 (make r}^{2} \text{ the subject)}$$

$$r = \pm \sqrt{\frac{3V}{\pi h}} \quad ---- \text{ A1}$$



It is given that AC = 15 cm, AD = 12 cm, BC = 26 cm and CD = 9 am.

9





Answer (b) cm [2]

- 10
- A map of Singapore has a scale of 1: 250 000.
 (a) The length of the Singapore river on the map is 1.2 cm. Calculate the actual length, in kilometres, of the Singapore river.

	1 : 250 000	
	1 cm: 2.5 km	
	1 0111. 2.3 Kitt	
	Actual length = 1.5×2.5 M1	
	= 3 km A1	
		COUCAU
	6	1.5
		(i) Kiii [1]
(b)	The area of Sentosa is 4.71 km^2 .	C003
	Calculate, the area, in square centimetres, of Sentosa	the map 60°
		N DO
		Oun
	90-01-02	7
	1/250 000 (D)	
	1 cm 25 km	
	cm^2 : 6.25 km ² (-+ Wfl (areascale)	
	La allos allos	
	470	TAT
	Area on the map = $\frac{1}{1000}$	- NYAL
	0.23 -0.7526 am^2 A1	DALATION
	AI	-DIULT

Answer (b) cm² [2]

11

The solid shown below consists of a solid cone attached to a solid hemisphere. The base radius of the cone is 8 cm and the height of the solid is 23 cm.



(a) Given that the slant height of the cone is 17 cm, explain why $\measuredangle ABC = 90^{\circ}$.



(ii) the volume of the solid.

Volume of solid

$$= \frac{1}{3}\pi(8^{2})(15) + \frac{2}{3}\pi(8^{3}) - -- M1$$

$$= 661\frac{1}{3}\pi$$

$$= 2077.6399 = 2080 \text{ cm}^{3} (3 \text{ s.f}) - -- A1$$

Answer (b)(ii)

..... cm^{3} [2]

12 The table shows the pocket money of 20 students, rounded off to the nearest whole number.

22	24	00	25	20
23	24	23	25	20
21	20	24	22	21
21	20	21	20	21
23	25	25	20	23
23	20	21	22	25

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3

Sale and

(a) Draw a dot diagram to represent the information in the table.

Answer

Explain two limitations of using Edot diagram. It is difficult to represent decimals in a det <u>Ve cannot represent a late</u> [2] [2] (a) (b) Answer [2] Is a line chart a suitable way to represent the data? Explain your answer. (c) Answer No. A line graph is suitable for time-based data. [1]

END OF PAPER

Ouestion that are similar to P2 and thus removed:

The following stem-and-leaf diagram shows the English and Mathematics scores of a class of 11 20 students.

Leaves for English scores						Stem	Le	eave	es f	or	Ma	the	ma	tics	sco	res
						3	8									
			0	3	5	4	9	5	3							
	2	3	4	4	6	5	9	7	5	4	4	4	3			
5	6	7	7	8	9	6	8	7	6	4	3	0				
	3	4	5	6	9	7	5	4	1							
					0	8										

Key: 5 | 0 means 50 marks

(a)

Find the modal score in the Mathematics test.

(b)

e ratio of students who scored more than 50 marks in the English test to those Islandwide Deliver Find the ratio of st in the Mathematics test

..... marks [1]

Which test is easier? Give a reason to justify your answer. (c)

Answer	(c)	
		 •••••

11



(e)

∡PQR .

[2] Answer (c)

....

20

". " But a

2

No.

Marking Scheme

1(i)	198	5
	18	
	=11	B1
(ii)	10	B1
(iii)	20	B1
2(a)	$s = kv^2$ where k is a constant	M1
	$3380 = k(26)^2$	AI
	<i>k</i> = 5	
	$s = 5v^2$	
(b)	$s = 5v^2$	NYAP
Ð	$=5 \times 12^2$	ICATION .
·F	= 720 m	31
3	$y = \frac{x+1}{x+1}$	
	x-1	Cross
	y(x-1) - x + 1	multiply)
	xy - x = 1 + y	
	x(y-1) = 1 + y	c600.3
a a	$x = \frac{1+y}{2}$	SMT (factorise)
1(i)(a)	22	Al
+(1)(a)	To Colinatsat	DI
(i)(b)	33 40	B1
(ii)	5-F-SE Della	M1 (equate)
D	40-+1-30 (wide	NTION
	-35x = -150	A1
1	x = 4	
5(a)(i)	$ext \angle = 30^{\circ}$	M1
-	number of triangles	
s.	$=\frac{360}{100}$	
	- 30	
	=12	A1
(ii)	$sum = 10 \times 180^{\circ}$	B1
	$=1800^{\circ}$	

÷

(b)	$(4DE - 150^{\circ} - 360^{\circ} - 150^{\circ} - 150^{\circ}$	M1
	$\angle ADE = 150 - \frac{2}{2}$	A1
	=120°	
6(a)	$\frac{b}{7c^2} \times \frac{2}{bc} \div \frac{1}{c^2}$	
	$= \frac{b}{7c^2} \times \frac{2}{bc} \times c^2$ $= \frac{2}{3c^2}$	M1 for flip
	7c	Al
(b)	$\frac{4x^2 - y^2}{2x + y^2} \times \frac{5}{x^2 - 5}$	NYAL
	$2x + y$ $x^{2} - 6x - 7$ (2x + y)(2x - y) 5	Al fan
	$=\frac{(2x+y)(2x-y)}{2x+y} \times \frac{z}{(x+1)(x-7)}$	(2x+y)(2x-y)
	$=\frac{5(2x-y)}{2}$	ha.
	(x+1)(x-7)	(x+1)(x-7)
	C	660031
7(a)	$\frac{x^{2}-4}{x} = \frac{18}{6}$ $x^{2}-4 = 3x$ $x^{2}-4 = 3x$ $x^{2}-4 = 0$	M1 M1(Form equ)
	x = -1 or y = 4 (rejected) 4 wide Delive.	A1 (no marks if do not reject)
(b)	ZBAC 1512MU	DUCAL
	$= 180^{\circ} - 60^{\circ} - 40^{\circ} (\angle \text{ sum of } \Delta)$	
	$=80^{\circ}$	M1
	reflex $\angle BAC$	
	$=360^{\circ}-80^{\circ}((\angle s \ at \ a \ po \ int)$	A 1
	$=280^{\circ}$	AI
8(a)	$5x^2 + 17(x+1) + 2x = 21$	M1 M1
	$5x^2 + 17x + 17 + 2x - 21 = 0$	
	$5x^2 + 19x - 4 = 0$	

1.1

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(b)	$5x^2 + 19x - 4 = 0$	
	(5x-1)(x+4) = 0	M1
	5x - 1 = 0 or $x + 4 = 0$	1411
	$x = \frac{1}{5} or x = -4$	A1
(c)	40.8	B1
9(a)	AB	B1
	$=\sqrt{7^2-5^2}$	
	= 4.90 m	
(b)	$\sin 20^\circ = \frac{8}{CD}$	M1
D	CD = 23.4 m	Al
(c)	$\tan 20^\circ = \frac{8}{BD}$	11
	<i>BD</i> = 21.979 m	
	ED=21.979 - 5 =17.0 m	
(d)	$\tan \angle BDA = \frac{4.8989}{21.979}$	
10(1)	$\angle BDA = 12.6^{\circ}$	a6005
10(1)	50x+10x=8000	B1
(ii)	x+y=500(1)	ecf if from
<	50x+10y=8000(2)	incorrect equation
	From (1), June (0) which	
	v = 2003 + 1+(3) Sub(3)into(2) Deliver'	M1 ecf
	50x+19(500-x)+8000	NYAL ON
U V	50x + 5000 + 20x = 8000	M1 ecf
. K	40x = 3000	
	<i>x</i> = 75	
	Sub $x = 75$ into (1)	
	y = 425	Al
(iii)	2300	B1
	$\frac{1}{75 \times 2 + 425} = \4	

11(a)	$l^2 = 15^2 + 3^2$	
	$l^2 = 234$	
	$l = \sqrt{234}$	M1 for slant
	=15.297	height
	=15.3	
	Surface area	
	$=\pi(3)(15,297)+[\pi(13)^2-\pi(3)^2]+2\pi(13)^2$	M1 for big circle
	$= 543.891\pi$	-small circle
	1710 cm^2	A1
	=1/10 cm	JAN
	DANYDA	ANYDON
	P ¹ UCALO	A DOAL
(b)	Volume	
	$=\frac{1}{\pi}\pi(3)^{2}(15)+\frac{2}{\pi}\pi(13)^{3}$	M1 for sub values
	3 () () 3 ()	
	$=1509\frac{2}{2}\pi$	
	-4742.7 cm^3	M1 for volume
	Density of ormament	G00'3'
		60° M1 for density
	= 3500 Only Only	WIT for density
	4/42.y	
5	Since density of ornament is less than density of liquid C, the	A 1
	ornament floats. Thus, the manufacturer will choose liquid C.	AI
12(a)	136m 19 inely	B1
(b)	Correct points OC	C2
(a)(i)	Smooth cutye	B1
(c)(1)	r = 6.25, (argent from 6.05 to 6.45)	B1
1117	· · · · · · · · · · · · · · · · · · ·	

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