

BEATTY SECONDARY SCHOOL END-OF-YEAR EXAMINATION 2018

Exp

SUBJECT : Mathem	atics	LEVEL : Sec 2E	
PAPER : 4048 / 1		DURATION: 1 hour 15 minutes	
SETTER : Ms Ong	Geok Leng	DATE : 8 Oct 2018	
CLASS :	NAME :	REG NO :	

READ THESE INSTRUCTIONS FIRST

Write your name, class and index number in the spaces on the top of this page. Write in dark blue or black pen. You may use a pencil for any diagrams or graphs. Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer all questions.

The number of marks is given in brackets [] at the end of each question or part question. The total number of marks for this paper is 50.

You are expected to use a scientific calculator to evaluate explicit numerical expressions. If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For π , use either your calculator value or 3.142 or otherwise stated by the question.

For Exam	iner's Use
	50

This paper consists of <u>11</u> printed pages (including this cover page)

Mathematical Formulae

Mensuration

Curved surface area of a cone =
$$\pi rl$$

Surface area of a sphere = $4\pi r^2$

Volume of a cone =
$$\frac{1}{3}\pi r^2 h$$

Volume of a sphere =
$$\frac{4}{3}\pi r^3$$

- 1 Given that y is directly proportional to the cube of (x + 1) and that y = 15 when x = 2.
 - (a) Express y in terms of x.



(b) Find the value of x when y = 120.



Answer $x = \dots$ [2]

(c) Find the value of y when x = 11.

i,

(a) Factorise completely (i) $15y^2 - y - 6$,

2

(ii) 2ac - 6ad + 10bc - 30bd.

(b) Expand and simplify $(2x-1)(2x+1) - 3(2x+3)^2$.

[Turn over

3 (a) Make b the subject of the formula $a = \sqrt{\frac{2b+1}{b}}$.

Answer[3]

(b) Solve the equation $\frac{5}{x-4} = \frac{5x-3}{x^2-2}$.

DANYAL

4

1

Solve the simultaneous equations. 3x - 2y = 8

4x + 3y = 5

Answer x =, y = [3]

Quadrilateral *ABCD* is congruent to quadrilateral *STUV*. *AB* = 7 cm, *BC* = 4 cm, $\angle ABC = 76^{\circ}$, $\angle TUV = 104^{\circ}$ and $\angle VST = 48^{\circ}$.

5



- (a) the length of TU,
- (b) angle ADC.



Answer cm [1]

A triangle ABC has sides AB = 5 cm, BC = 12 cm and AC = 13 cm.



(a) Prove that triangle *ABC* is a right-angled triangle.

(b) Hence, find (i) $\sin \angle BAC$,

(ii) angle ACB.



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15

The stem-and-leaf diagram below represents the scores obtained by 30 boys and girls in a Mathematics test.

 		L	eaf	for	bo	ys	Stem	Le	eaf	for	gir	ls			
						8	4	5	6			51			
					7	2	5	4	6	9					
			8	6	3	2	6	0	2	2	2	5	7	9	
8	6	4	1	1	1	0	7	2	5						
					4	1	8								

Key (Boys): 8|4 means 48 marks

Key (Girls): 4|5 means 45 marks

(a) Write down the modal score for the girls.

Answer marks [1]

(b) Find the median score for the boys.

Answer marks [2]

(c) One more boy took the test later and scored 67 marks. Describe how the inclusion of his score will affect the median score for the boys.

8 The perimeter of a rectangle *ABCD* is 48 cm. Let the length of the rectangle be x cm.



(a) Find an expression, in terms of x, for the width of the rectangle.

1. 1. 1. 1. 1

(b) The area of the rectangle is 135 cm².
(i) Form an equation in terms of x.

[1] Answer

(ii) Solve the equation in (b)(i) and find the length of the rectangle.

A river that is 9.6 km long is 2.4 cm long on a map.

(a) Express the scale of the map in the form 1:n.

(b) A tunnel has a length of 3.8 cm on the map. Calculate its actual length, in km.

Answer km [1]

(c) A plantation has an area of 24 cm^2 on the map. What is its area, in cm², when drawn on another map whose scale is $1 : 80\ 000\ ?$

Answer $\ldots cm^2$ [3]

[Turn over

10 A regular hexagonal spinner with sectors of different number is shown below.



The pointer is spun once, find the probability that the pointer will stop at (a) the number 5,

Answer

[1]

15

ý

(b) a number greater than 2,

(c) a factor of 12,

(d) a prime number.

Answer [1]

11 A cylinder has radius 5 cm and height 6 cm. A hemisphere has radius r cm. The volumes of the cylinder and hemisphere are equal.



Find (a) the value of r,



(b) the total surface area of the hemisphere.

Answer
$$cm^2$$
 [2]



Answer for 2E Math Paper 1

1	(a)	$y = \frac{5}{9}(x+1)^3$
	(b)	r=5
	(c)	$\frac{x-y}{y=960}$
2	(a)(i)	(5y+3)(3y-2)
- 1	(a)(ii)	2(a + 5b)(a - 3d)
	(a)(ll) (b)	$-8x^2 - 36x - 28$
3	(a)	$b = \frac{1}{a^2 - 2}$
3	(b)	$x = \frac{22}{23}$
4		$\begin{array}{c} x = 2 \\ y = -1 \end{array}$
5	(a)	TU = 4 cm
	(b)	132°
6	(a)	$AC^2 = 13^2 = 169$ $AB^2 + BC^2 = 5^2 + 12^2 = 169$ Since $AB^2 + BC^2 = AC^2$, by converse of Pythagoras theorem, triangle ABC is a right-angled triangle. $\angle ABC = 90^\circ$
	(b)(i)	$\sin \angle BAC = \frac{12}{13}$
	(b)(ii)	$\angle ACB = 22.6^{\circ}$
7	(a)	Modal score for the girls = 62 marks
	(b)	Median score for the boys = 70.5 marks
	(c)	Median score will reduce/decrease to 70 marks for the boys.
8	(a)	(24 - x) cm
-	(b)	x = 9 or $x = 15Length of the rectangle is 15 cm.$
9	(a)	1:400000
2	(b)	$3.8 \text{ cm} : 3.8 \times 4 = 15.2 \text{ km}$
	(c)	$384/0.64 = 600 \text{ cm}^2$
10	(a)	the number $5 = \frac{1}{6}$
an a g	(b)	Number greater than $2 = \frac{4}{6} = \frac{2}{3}$
	(c)	A factor of $12 = \frac{5}{6}$
	(d)	A prime number = $\frac{3}{6} = \frac{1}{2}$
11	(a)	$r \approx 6.08 \text{ cm} (\text{to 3 sf})$
	(b)	349 cm^2 (to 3sf)

BEATTY SECONDARY SCHOOL END-OF-YEAR EXAMINATION 2018



SUBJECT : Mathematics

LEVEL : Sec 2 Express

PAPER : 2

SETTER : Ms Irene Ng

DATE : 10 October 2018

DURATION : 1 hour 30 minutes

CLASS :	NAME :	REG NO :
EDO		EPO

READ THESE INSTRUCTIONS FIRST

Write your name, class and index number in the spaces on the top of this page. Write in dark blue or black pen.

You may use a pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer all questions.

If working is needed for any question, it must be shown with the answer.

Omission of essential working will result in loss of marks.

Calculators should be used where appropriate.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to

three significant figures. Give answers in degrees to one decimal place.

For π , use either your calculator value or 3.142, unless the question requires the answer in terms of π .

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question. The total number of marks for this paper is 50.

Mensuration

1

Curved surface area of a cone = $\pi r l$

Surface area of a sphere = $4\pi r^2$

Volume of a cone =
$$\frac{1}{3}\pi r^2 h$$

Volume of a sphere = $\frac{4}{3}\pi r^3$



In the diagram, triangle PQT is similar to triangle SRT. Angle PQT = angle SRT. PQ = 15 cm, PT = 10 cm, QT = 6 cm and ST = 15 cm.

Calculate SR, (a) PR.

(b)

[2]

[1]

[2]

2 (a) Factorise fully
$$18xy + 9y$$
.

(b) Simplify
$$\frac{25-p^2}{2p^2+7p-15}$$
. [3]

(c)	Express as a single fraction in its simplest form	$\frac{5x}{(x+2)^2} -$	$\frac{4x}{x+2}$.	[2]

3 (a) It takes 3 workers 16 weeks to complete a renovation project. How many extra workers are needed if the project is to be completed in 6 weeks?

[2]

14.2

24.24

- (b) y is inversely proportional to x^2 . It is given that y = 28 for a particular value of x. Find the value of y when x is doubled. [2]
- 4 The table shows the heights of 40 students in class 2G.

Heights (cm)	$150 < x \le 160$	$160 < x \le 170$	$170 < x \le 180$	$180 < x \le 190$		
Number of students	8	13	17	2		
DAL EDUCATION EDUCATION						

(a) Find the percentage of students whose heights are less than or equal to 170 cm. [2]

- (b) (i) Calculate an estimate of the mean height. [2]
 - (ii) Explain why the mean in (b)(i) is an estimate. [1]

5	(a)	(i)	Simplify $\frac{16p^2}{4q} \div \frac{8p}{3q}$.	[2]
		(ii)	Expand and simplify $3(a-1)(4a+5)$.	[2]
	(b)	Given t	hat $x^2 + y^2 = 45$ and $xy = 12$, find the value of $(2x - 2y)^2$.	[2]
	(c) D	A cone	has radius 8 cm and volume 320π cm ³ . Find the height of the cone.	[2]

- 6 Mr Yan bought 60 litres of apple juice. He poured the fruit juice equally into x bottles.
 - (a) Write down an expression, in terms of x, for the volume, in litres, of apple juice in each bottle. [1]
 - (b) Mr Yan bought the same amount of orange juice and poured the orange juice into (x 6) bottles.
 Write down an expression, in terms of x, for the volume, in litres, of orange juice in each bottle. [1]
 - (c) It is given that the volume of orange juice in each bottle is 0.5 litres more than the volume of apple juice in each bottle.

Write down an equation in x and show that it reduces to $x^2 - 6x - 720 = 0.$ [3]

[2]

- (d) Solve the equation $x^2 6x 720 = 0$.
 - (e) Hence, find the volume, in litres, of apple juice in one bottle. [1]



The diagram shows a field *ABCD*. *Q* is on *AB* such that *DQ* is perpendicular to *AB*. $DQ = 58 \text{ m}, DB = 71 \text{ m}, \text{ angle } DAQ = 64^\circ, \text{ angle } DBC = 90^\circ \text{ and angle } BCD = 25^\circ.$

Calculate

(a)	QB,	[2]
(b)	AB,	[3]
(c)	the shortest distance from B to DC.	[2]

8 A souvenir was designed in the shape of a solid rectangular pyramid as shown below. AB = 9 cm, BC = 7 cm and VO = 8 cm.



- (a) Find the volume of the souvenir.
- (b) Find the total surface area of the souvenir.
- (c) The souvenir is to be made of wood. The wooden pyramid must not have a mass greater than 119 grams.

Four types of wood are available. The table shows these woods and their densities.

Wood	Pine	Birch	Teak	Maple
Density	0.65	0.71	0.63	0.75
(g/cm^3)				

Which of these woods could be used to make the wooden pyramid? Justify your answers with workings.

[2]

[2]

[4]

1

i.

Answer Key:

On	Answers	
19	22.5 cm	<i>a</i>
1a 1b	10 cm	
221	(2r+1)	
221	5-p	5
Zan	$\frac{1}{2n-3}$	
2b	$\frac{-4x^2-3x}{-4x^2-3x}$	
	$\frac{1}{(x+2)^2}$	\bigcirc
3a	5 workers	\times
3b	7	
4a	52.5%	N
4bi	168.25 cm	N
4bii	It is an estimate as the mid value was used.	
5ai	3p	-3 ¹
	$\overline{2}$	6005
5aii	$12a^2 + 3a = 15$	2860
5b	84	NO
59	h=15 cm	
/6 a	60 By to the sale	
	Mpart	
60	TO COULD ALLONDAN	M .
00	KOGUU HANGIY	
60	$x = 30^{\circ} \text{ or } x = 524^{\circ}$	
De 7	1 Intrest &	
7a 71	41.00MT	
70 5	Q = 0.2 m	
7C ·	n = 04.3 III	
od 9h	206 cm^2	
80	Dine and Teak	
00		\square

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BEATTY SECONDARY SCHOOL END-OF-YEAR EXAMINATION 2018

MARK SCHEME

SUBJECT : Mathematics	LEVEL :	Sec 2E
PAPER : 4048 / 1	DURATION :	1 hour 15 mins
SETTER : Ms Ong Geok Leng	DATE :	8 Oct 2018
CLASS : NAME :	2	REG NO :
El	K	
READ THESE INSTRUCTIONS FIRST Write your name, class and index number in the sp.	it can be the top of this	prare.
You may use a pencil for any diagrams or graphs		-31
Do not use staples, paper clips, highlighters, glue o	r correction fluid.	66000
Answer all questions.	SI OUNS	60
The number of marks is given in brackets P hat the	end opeach question	n or part question.
The total number of marks for this paper is 50.	nac	
You are expected to use a scientific calculator to en	valuate explicit nume	rical expressions.
If the degree of accuracy is not specified in the ou	estion, and if the ans	wer is not exact.
give the answer to three significant figures. Give	answers in degrees	to one decimal

give the answer to three significant figures. Give answers in degrees to one dech place. For π , use either your calculator value or 3.142 or otherwise stated by the question.

For Exam	iner's Use
	50

This paper consists of <u>11</u> printed pages (including this cover page)

1	(a)	$y = k(x+1)^3$
		$15 = k(2+1)^3$ [M1]
		15 = k(27)
		15 5
		$k = \frac{1}{27} = \frac{1}{9}$
		5 ()3 5 ()
		$y = \frac{1}{9}(x+1)^3$ [A1]
	(b)	v = 120
		5 ()3
		$120 = \frac{1}{9}(x+1)^{3}$ [M1]
		$216 = (r+1)^3$
		210 - (x + 1)
		$0 = \mathbf{x} + 1$
and all and the second second		x = 5 [A1]
	(C) BI	x = 11
		$y = \frac{3}{2}(11+1)^3$
		$y = \frac{5}{2}(12)^3$
		y = 960 [BH]
-		
2	(a)(l)	15y - y - 0 - (5y + 2)(2) 2) (22) (2) (2) (2)
		-(2y+p)(2y-2)
	(a)(ii)	2202 - 600 + 1000 - 30bd - 00 - 00
		= 2(ac + 3ad + 5bc + 15bdt) + 52000 + 52000
	$ \langle \rangle ^{2}$	=2[a(a - 3a) + 5b(a - (3a))] [MNIN (2)
	$ \setminus \langle$	=2(a+5b)(c+3d) [A1]
		IN INCOMENT
	Ĭ	Musz Scher Den
		2ac = 6ad + 10bc - 30bd
	DE	=2a(c-3d)+10b(c-3d) [M1]
	EI	=(26+10b)(c-3d)
		=2(a+5b)(c-3d) [A1]
		2
	(b)	$(2x-1)(2x+1) - 3(2x+3)^2$
		$= (4x^{2} + 2x - 2x - 1) - 3(4x^{2} + 6x + 6x + 9)$
		$= 4x^{2} - 1 - 3(4x^{2} + 12x + 9) [M2]$ = 4x^{2} - 1 - 12x^{2} - 26x - 27
		$\frac{-4x - 1 - 12x - 30x - 2}{-9x^2 - 26x - 29}$
		$=-8x^{2}-36x-28$ [A1]
3	(a)	$a = \sqrt{\frac{2b+1}{2}}$
		V b
		$a^2 = \frac{2b+1}{2b+1}$
		b living
		$a^2\mathbf{b} = 2b + 1$
		$a^2b - 2b = 1$
		$b(a^2 - 2) = 1$ [M1]

· "我是一个"你,不是不一个?"他们的话,"你是不



[Turn over

8	(a)	Let the length of the rectangle be <i>x</i> .		
		$Width = (48 - 2x) \div 2$		
		= (24 - x) cm [B1]		
	(b)	x(24-x) = 135 [M1]		
		$24x - x^2 = 135$		
		$x^2 - 24x + 135 = 0$		
		(x-9)(x-15) = 0 [M1]		5 A
		x = 9 (rejected) or $x = 15$		
		Length of the rectangle is 15 cm. [A1]		
9	(a)	Map : Actual		
		2.4 cm : 9.6 km		
		1 cm: 4 km [M1]		
		1 : 400000 [A1]		JAT
		ANY DE		ND P
	(b)	1 cm : 4 km		- Deschillor
		\bigcirc 3.8 cm : 3.8 × 4 = 15.2 km [B1]		
		1		
	(c)	1 cm : 4 km	0	$1 \sqrt{2}$
		1 cm^2 : 16 km ² [M1]	11	IN
		24 cm ⁻ : 384 km ⁻ [M1]		
		1 cm : 0.8 km	11	
		$1 \text{ cm}^2 \cdot 0.64 \text{ km}^2$		21
		$m^2 \cdot 384 \text{ km}^2$		-600s
			2 U	2800
		384/0.64=600 cm ² /[A1]	11/2	MA
	ſ	1 Plan - TOPO	1 nC)((')
	1		, capt	
10	(a)	the number $p = -$	Yrs.	
		- CO. UU 4-12	(5.1)	
	(b) \	Number greater than $2 = 3 = 3$	[B1]	
	V	SS. SDen		1.
	(c)	A factor of 12 de	[B1]	NYAL
	(d)	Landi 3 1		DALMON
	(u)	A prime number = $\frac{3}{2} = \frac{1}{2}$	[B1]	EDUCA
		6 2		
11	(a)	2		
11	(a)	$\frac{2}{\pi}\pi r^3 = \pi (5)^2 (6)$	[M1]	
		3		
		$\frac{2}{r^3} = 150$		
		3	[M1]	
		$r^3 = 225$		
		r = 6.0822		
		$r \approx 6.08 \text{ cm}$ (to 3 sf)	[A1]	
	(b)	Total surface area of the hemisphere		
	999 - 199	$=3\pi r^2$		
		$= 3 \times \pi \times (6.0822)^2$	[M1]	
		$= 349 \text{ cm}^2$ (to 3sf)	[A1]	

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Beatty Secondary School 2E EOY Math P2 2018 Marking scheme

Qn	Solutions	Remarks
1a	SR_ST	
	$\overline{PQ} = \overline{PT}$	
	SR 15	
	$\frac{1}{15} = \frac{1}{10}$	M1
	$SR = \frac{10}{10} \times 15$	
	SR = 22.5 cm	Al
1b	$TR = \frac{3}{2} \times 6$	
	$= \frac{2}{9}$ cm	M1
0	AN TON NOT NA	NUTION
	PR = 10 + 9	Alle
1.1	= 19 cm	4)1
20	18 m + 01	
20	=9v(2r+1)	
2h	25- <i>n</i> ²	
20	$\frac{-1}{2n^2+7n-15}$	
		7/ .
	(5+p)(5-p)	M1 = factorise numerator
	$=\frac{(3+p)(3+p)}{(2p-3)(p+5)}$	MG-factorise denominator
		80-
1	5-p ()) () () ()	A1
	-2pF3	
2c	5x/ 4x (D) 8317 ats24	
	(x4,2)2 (x+2) (1) (Nha	
1	$= \frac{5x}{4x(x+2)}$	
	(x+x)2 (7+2)2 U - 11181,	
	$=\frac{5x-4x(x+2)}{\sqrt{2}}$	
	(x+2)2 11 1Nide	MI
\mathbb{D}	$=\frac{5x-4xx-8x}{2} 2n0^{3}$	NION
	$(x+2)^{2}(5)^{2}$	Der -
	$=\frac{-4x^{-}-5x}{(x+2)^{2}}$	A 1
	$(x+2)^2$	AI .
32	3 workers 16 weeks	
Ja	1 worker 48 weeks	
	8 workers 6 weeks	
		ر _ا
	Answer: $8 - 3 = 5$ workers	A1
3b	an k	
	$2 \aleph = \frac{1}{x^2}$	
	$k = 28x^2$	M1
	$new v = \frac{k}{k}$	
	$(2x)^2$	

	$28x^2$	
	$-\frac{1}{4x^2}$	
	=7	
		Al
4a	8+13	
	$-\frac{1}{40} \times 100\%$	M1
	=52.5%	A1
4bi	mean height	
	$- \frac{(155 \times 8) + (165 \times 13) + (175 \times 17) + (185 \times 2)}{(175 \times 17) + (185 \times 2)}$	
	40	MI
	=168.25 cm	Al
4bii	It is an estimate as the mid value was used. The exact height	
4011	of each student is not known	BI
		Accept any reasonable
	EDUCA	answers.
5ai	$16p^2 8p$	
	$\left \frac{1}{4a} \div \frac{1}{3a}\right $	
	$16n^2$ 3 <i>q</i>	
	$\left =\frac{10p}{4a}\times\frac{5q}{8p}\right $	M1
	3p	5
	$\frac{1}{2}$	
	(\sim)	c00 ³
5aii	3(a-1)((4a+5))	0.6 ^{0~}
	$=3(4a^{2}+5a-4a-5)$	9M1
	$= 3(4a^{2} + a^{-} 5)$	
	-120 + 30 +13	AI
5h	A-1- 10 (0.50 mats	
50	= 2 2 2 + + + +	
	$= x + y^2 - 2xy$ (2) (1) (1)	
	=45 2012	M1
	=21 ide	- WAL
	ndwit	AA TION
	$(2x-2y)^2$ 15/21	DUCALLE
	$= [2(x-y)]^2$	ED
	= 4(21)	
	=84	A1
	1	
50	$\int \frac{1}{2}\pi(8^2)h = 320\pi$	
		MI
	$\frac{31}{2}h = 320$	
	$b = \frac{3}{20 \times 3}$	
	$\left \begin{array}{c} n - \frac{64}{64} \end{array} \right $	
	h = 15 cm	Al
6a	60	
	\overline{x}	B1

6b	60	D1
6c	$\frac{x-6}{60}$ 60 $\frac{5}{60}$	BI
	$\frac{1}{x-6} - \frac{1}{x} = 0.5$	M1
	$\frac{60x-60(x-6)}{60}=0.5$	M1
	x(x-6) 60x-60x+360	
л. А.	$\frac{1}{x^2 - 6x} = 0.5$	
	$360=0.5(x^2-6x) 0.5x^2-3x-360=0$	21 A
	$x^2 - 6x - 720 = 0$	A1
6d	(x-30)(x+24) = 0	M1
	20 0 1 21 - 0	NAL
D	x - 30 = 0 or $x + 24 = 0x = 30$ or $x = -24$	ALTION
6e	$\frac{60}{30} = 2litres$	81
7a	$OB = \sqrt{71^2 - 58^2}$	
	<i>QB</i> = 40.951	
	QB = 41.0 m	
7b	$tan64^\circ = \left(\frac{58}{16}\right)$	x6003
		0°0
	AQ = ran64° Only Only	
	$AQ \neq 28.288$	
•	What what	
	AB = 28.288 + 40.951	M1
	AB = 69.239 (0.50 Deliver)	Al
7c	∠BDC = 180° - 90° 25°	NAL
D	=65° and	CATION
1	boo h	
	$\sin 65^\circ = \frac{1}{71}$	M1
	$h = 71 \times \sin 65^{\circ}$	
	h = 64.347 h = 64.3 m	A1
8a	Volume	
~	$\left \frac{-1}{3} \times (9 \times 7) \times 8 \right $	
	$=168 \text{ cm}^3$	
8b	In triangle VAB, ht = $\sqrt{8^2 + 3.5^2}$]
	$=\sqrt{76.25}$	M1 (any one)
	In triangle VBC, ht = $\sqrt{8^2 + 4.5^2}$	



The A

