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# Anglo-Chinese School (Barker Road) 

## END-OF-YEAR EXAMINATIONS 2018

SECONDARY TWO
EXPRESS

## MATHEMATICS 4048 <br> PAPER ONE

1 hours 15 minutes

## READ THESE INSTRUCTIONS FIRST

Write your index number and name on all the work you hand in.
Write in dark blue or black pen.
You may use an HB pencil for any diagrams or graphs.
Do not use staples, paper clips, glue or correction fluid.
Answer all questions.
If working is needed for any question it must be shown with the answer. Omission of essential working will result in loss of marks.
The use of an approved scientific calculator is expected, where appropriate.
If the degree of accuracy is not specified in the question, and if the answer is not exact, give your answer to three significant figures. Give answers in degrees to one decimal place.
For $\pi$, use either your calculator value or 3.142 , unless the question requires the answer in terms of $\pi$.

At the end of the examinations, fasten your work securely together. The number of marks is given in brackets [] at the end of each question or part question.
The total of the marks for this paper is 60.

## Mathematical Formulae

## Compound Interest

$$
\text { Total amount }=P\left(1+\frac{r}{100}\right)^{n}
$$

## Mensuration

$$
\begin{aligned}
& \text { Curved Surface area of cone }=\pi r l \\
& \text { Surface area of a sphere }=4 \pi r^{2}
\end{aligned}
$$

$$
\text { Volume of a cone }=\frac{1}{3} \pi r^{2} h
$$

$$
\text { Volume of a sphere }=\frac{4}{3} \pi r^{3}
$$

$$
\text { Area of a triangle }=\frac{1}{2} a b \sin C
$$

Arc length $=r \theta$, where $\theta$ is in radians
Sector area $=\frac{1}{2} r^{2} \theta$, where $\theta$ is in radians

## Trigonometry

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\begin{aligned}
& \frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C} \\
& a^{2}=b^{2}+c^{2}-2 b c \cos A
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## Statistics

$$
\begin{aligned}
\text { Mean } & =\frac{\sum f x}{\sum f} \\
\text { Standard deviation } & =\sqrt{\frac{\sum f x^{2}}{\sum f}-\left(\frac{\sum f x}{\sum f}\right)^{2}}
\end{aligned}
$$

For Examiner's Use

1 Estimate correct to 1 significant figure, the value of $\frac{0.049608 \times 599.867}{0.01965}$.

Answer
2 Simplify $(3 x-5)(x-6)-x(3 x-4)$.

Answer
3 Factorise completely
(a) $12 x^{2}-21 x+9$,

Answer (b)
[2]
(b) 15ax-10ay-21bx+14by.

Answer (c)
[2]

4 Petrol costs $x$ cents per litre. Mr Yip intends to take a road trip during the holidays. Find an expression for the number of litres of petrol that can be bought for $y$ dollars.

5 The average capacity of a memory card in a digital camera is 10 GB and each digital photo takes up to 1.3 MB on average. If a salesman claims that the memory card can store more than 7000 photos, is his claim true? Justify your answer with clear working.
$\left(1 \mathrm{~GB}=10^{9} \mathrm{~B}, 1 \mathrm{MB}=10^{6} \mathrm{~B}\right)$

Answer $\qquad$
$\qquad$

6 Given that $2^{n} \times \sqrt{2} \div 2^{-5}=1$, find the value of $n$.

Answer $n=$
$\square$
For Examiner's

7 (a) Express 12600 as a product of its prime factors.

Answer (a)
[1]
(b) Given that $14700=2^{2} \times 3 \times 5^{2} \times 7^{2}$. The greatest number that will divide 12600,14700 and $x$ exactly is 70 . What are the least possible values of $x$.

Answer (b)
[2]

8 Tom, Sam and Matt compete one lap of a circular track in 12, 15 and 18 minutes respectively. They start together. They run in the same direction and maintain the same lap times.
How many more laps will Tom have completed than Matt when all three of them next meet on the starting line together?

9 (a) Solve the inequality $-3 \leq 3 x+3<\frac{4 x+9}{2}$.

Answer (a)
[2]
(b) Represent the solution set in (a) on the number line below.

Answer
[1]

$10 P$ is directly proportional to the square of $r$ and $P=200$ when $r=5$.
(a) Express the $P$ in terms of $r$.

Answer (a)
[1]
(b) When $r$ is increased by $300 \%$, find the percentage increase in $P$.
Answer
(b) \%

11 In the diagram, $A B=8 \mathrm{~cm}, A C=10 \mathrm{~cm}, B C=6 \mathrm{~cm}, B C=C D$ and $A C D$ is a straight line
(a) Explain why $\angle A B C$ is a right angle.

Answer


Answer $\qquad$
$\qquad$
$\qquad$
(b) Without finding any angle, find the area of $\triangle B C D$.
Answer (b)

$$
\mathrm{cm}^{2}
$$

(c) Write down exact value of $\cos \angle B C D$.

## Answer (c)

$\qquad$ [1]

12 A construction company use the following container for sand.


The container is made up of a cylinder on top of a cone. The cylinder has a radius of 3 m and a height of $h \mathrm{~m}$. The cone has a base radius of 3 m and a vertical height of 4 m .

The container is initially empty and is then filled with sand from the top at a constant rate.

After 5 hours, the depth of the sand is 6 m above the vertex of the cone. After 9 hours, the container is full of sand.

Find the value of $h$. Give your answer as correct to two decimal places.
You must show all your working.

> Answer

13 (a) Express $x^{2}+14 x+18$ in the form $(x+a)^{2}-b$.

Answer (a)
(b) Hence, solve $x^{2}+14 x+18=0$. Give your answers correct to 2 decimal places.
$\qquad$
14 Solve $7 a^{2}-28 a=0$.

$$
\text { Answer } a=
$$

15 An area of $2160 \mathrm{~km}^{2}$ is represented on map by an area of $60 \mathrm{~cm}^{2}$. Find
(a) the scale on the map in the form $1: n$,

> Answer (a)
[1]
(b) the length of a road on the map, in cm with an actual distance of 27 km .

$$
\text { Answer (b) } \mathrm{cm}[1]
$$

16 On a particular day, the temperature at the summit of Mount Snowy was $-15^{\circ} \mathrm{C}$ and the temperature at the foot of the mountain was $20^{\circ} \mathrm{C}$.
(a) Find the difference between these two temperature.

Answer (a)
${ }^{\circ} \mathrm{C}$ [1]

The height of Mount Snowy is 2655 m . Shaun thinks that at 1400 m , temperature will be at $0^{\circ} \mathrm{C}$.
(b) Do you agree with him? Explain your answer.

Answer (b) $\qquad$
$\qquad$
(c) Identify one assumption that was made in (b)

Answer (c) $\qquad$

## For <br> Examiner's <br> Use



(a) How high is the kite vertically above the ground assuming that the

## string is taut?

## Answer (a)

(b) The wind becomes stronger and the kite is carried 60 m horizontally further away from point T to point $F$. Noah releases more string, maintaining the height of the kite above the ground.
Calculate the length of the string $G F$.

Answer (b) m
(c) Calculate the angle that the string $G F$ now makes with the ground.

## END OF PAPER



## Anglo-Chinese School (Barker Road)

## END-OF-YEAR EXAMINATIONS 2018 <br> SECONDARY TWO EXPRESS

## MATHEMATICS 4048 PAPER TWO

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1 Marcus invested $\$ 5000$ in a bank at an interest rate of $2.5 \%$ compounded annually.
(a) Find the total amount he had at the end of second year.

At the end of second year, Marcus withdrew all the money in the bank and invested it into another bank which offered simple interest rate of $8 \%$ per annum.
(b) Find the minimum number of years he had to leave the money in the bank in order for it to be more than $\$ 10000$.

2

(a) Using the information shown in the diagrams, write down two equations in $x$ and $y$.
(b) Solve these equations to find the values of $x$ and $y$.

3 The terms $T_{1}, T_{2}, T_{3}, T_{4}, T_{5}$ of a sequence are given as follows:

$$
\begin{aligned}
& T_{1}=1=1 \\
& T_{2}=3=1+2 \\
& T_{3}=6=1+2+3 \\
& T_{4}=10=1+2+3+4 \\
& T_{5}=15=1+2+3+4+5
\end{aligned}
$$

(a) Write down the next two terms, $T_{6}$ and $T_{7}$ in the sequence

$$
\begin{equation*}
1,3,6,10,15, \ldots \ldots \tag{1}
\end{equation*}
$$

(b) The nth term in the sequence is given by $T_{n}=\frac{1}{2} n(n+1)$.

Explain briefly why 200 is not in the sequence.
(c) Use the formula to find $T_{100}$.
(d) Use your answer to part (c) to find $5+10+15+\ldots \ldots+500$.
(e) Hence find the sum of all the whole numbers from 1 to 500 which are not multiples of 5 .

4 (a) In a departmental store, the selling price of a shirt was decreased by $25 \%$ during sale.
(i) If the price of the shirt was $\$ 98.80$ at first, what was its price during the sale?
(ii) During the sale for every 2 shirts that a customer purchase, the customer was entitled to purchase a 'purchase with purchase'(PWP) item.
The item the customer is able to purchase is a limited edition golf umbrella at a PWP price of $\$ 9.20$.
Mr Lim purchased $n$ shirts during the sale and paid $\$ 472.20$ in total including all his entitlements PWP items. Find the value of $n$.
(b) (i) Given that $\xi=\{$ all triangles $\}, A=\{$ isosceles triangles $\}$, $B=$ \{equilateral triangles \} and $C=$ \{right-angled triangles $\}.$ Draw a Venn diagram representing the sets $\xi, A, B$ and $C$.
(ii) A triangle has sides $7 \mathrm{~cm}, 24 \mathrm{~cm}$ and 25 cm . On the same Venn diagram in (b)(i), mark and label the point T to represent this triangle.

5 (a) Solve the equation

$$
\begin{equation*}
\frac{4 x-3}{6}+\frac{x+2}{3}=\frac{5}{2} . \tag{3}
\end{equation*}
$$

(b) (i) Factorise $2 x^{2}-32 y^{2}$.
(ii) Hence simplify

$$
\begin{equation*}
\frac{8 x y+2 x^{2}}{2 x^{2}-32 y^{2}} \tag{2}
\end{equation*}
$$

(c) Make $x$ the subject of the formula.

$$
\begin{equation*}
y=\sqrt{\frac{4 x}{p x-1}} \tag{3}
\end{equation*}
$$

6 Isaac is planning a cycling expedition. He explores two possible routes.
(a) If he travels on route A , which is 120 km long, he expects to cover $x \mathrm{~km}$ per hour. Route B, which is 5 km shorter than route A , has more challenging terrain and he would only be able to cover $(x-2) \mathrm{km}$ per hour.
Write down an expression, in terms of $x$, for the time he expects to take on
(i) route A ,
(ii) route B .
(b) He estimates that route A will take 40 minutes less than route B. Form an equation in $x$ and show that it reduces to $2 x^{2}+11 x-720=0$.
(c) Solve the equation $2 x^{2}+11 x-720=0$, give your answers correct to 3 decimal places.
(d) Calculate the time, in hours and minutes, that he expects to take on route B .

7 In the diagram, $P, Q$ and $R$ represent three islands.
$P Q$ is 72 km . The bearing of $Q$ from $P$ is $336^{\circ} . P R$ is 37 km . The bearing of $R$ from $P$ is $040^{\circ}$. $S$ is due west of $R$.

(a) Calculate
(i) the bearing of $P$ from $Q$,
(ii) the distance $Q R$,
(iii) the distance $R S$.
(b) A helicopter is flying 5 km vertically above Island $S$. A boat is sailing along $P R$. Find the greatest angle of elevation of the top of the helicopter from the boat.

8 Josh and Seth plan to travel from Liverpool to Newcastle. They need to be in Newcastle by 2.00 p.m. and can travel by train or bus. They plan to keep their travelling time and cost to the minimum. Information that Josh and Seth need is in the table below.
(a) Calculate the time taken for the train journey.
(b) Showing all your reasoning and calculations for cost and time, how will you recommend the departure time and mode of transport from Liverpool to Newcastle?

## Part of train timetable

| Liverpool (depart) | 0925 | 1015 | 1105 | 1200 |
| :--- | :---: | :---: | :---: | :---: |
| * Train fare from Liverpool to Newcastle is $\$ 52$ for one person. |  |  |  |  |
| * Train journey from Liverpool to Newcastle is 195 km |  |  |  |  |
| * Average train speed is $60 \mathrm{~km} / \mathrm{h}$ |  |  |  |  |

## Part of bus timetable

| Depart Liverpool | 0755 | 0815 | 0900 |
| :--- | :---: | :---: | :---: |
| via | Middlebrough | Manchester | Leeds |
| Arrive Newcastle | 1245 | 1330 | 1445 |
| Expected average speed of bus on this journey is 35 miles per hour. <br> The bus fare is charged based on the distance travelled: <br> $\$ 0.15$ per kilometre. <br> 1 kilometre is equivalent to 0.62 mile. |  |  |  |

## END OF PAPER

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Marking Scheme
Secondary 2 Express Paper 1
End of Year Exams 2018


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