Name : $\qquad$
$\qquad$
Class : $\qquad$

# Clementi Town Secondary School <br> Mid-Year Examination 2017 Secondary 2 Express 

## MATHEMATICS

Paper 1



## Candidates answer on the Question Paper.

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## READ THESE INSTRUCTIONS FIRST

Do not open the booklet until you are told to do so.
Write your name, register number and class on all the work you hand in.
Write in dark blue or black pen.
You may use a nHB pencil for any diagrams or graphs.
Do not use staples, paper clips, highlighters, glue or correction fluid.
Answer all questions.
If working is needed for any question it must be shown with the answer.
Omission of essential working will result in loss of marks.
If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answe $r$ to three significant figures. Give answers in degrees to one decimal place.

## CALCULATORS ARE NOT ALLOWED TO BE USED IN THIS PAPER.

The number of marks is given in brackets [ ] at the end of each question or part question. The total numb er of marks for this paper is 50 .


1. (a) Expand and simplify $(3 x-2 y)^{2}$.

Answer (a)
(b) Using your answer to part (a), find the value of $28^{2}$.

Answer (b)
2. Factorise the following completely
(a) $x^{2}+2 x-35$,

Answer (a)
(11)
(b) $9 x^{2}-25$,
Anwer (o) ............................ |1]
(c) $24 x y-81 x^{2} y$.
Answer (c) ................................ |||
3. Simplify the following
(a) $\frac{45 x^{2} y^{3}}{27 p q} \times \frac{3 p^{2} q^{3}}{9 x y^{2} z}$,
(b) $\frac{7 r^{3} s}{3 y^{2} z^{3}} \div \frac{14 r^{2} s^{3}}{6 y z^{3}}$.
4. The curve $y=8+2 x-x^{2}$ cuts the $y$-axis at $A$ and the $x$-axis at $B$ as shown in the diagram.

(a) Find the coordinates of $A$.

$$
\text { Answer (a) } A(\ldots \ldots \ldots . \ldots \ldots \ldots . . . . . . . . .
$$

(b) Find the coordinates of $B$.

$$
\text { Answer (b) } B(\ldots \ldots \ldots \ldots, \ldots \ldots \ldots) \quad \text { [1] }
$$

(c) Write down the equation of the line of symmetry.

Answer (c)
(d) Given that the point $C(2, p)$ lies on the curve, find the value of $p$.

Answer (d) $p=$
5. In a two-digit number, the tens digit is 5 more than the ones digit.

The number is 58 greater than the product of the digits.
Find the number.
6. Given that 3 is one of the roots of the equation $3 x^{2}+a x-30=0$, find
(a) the value of $a$,

$$
\text { Answer (a) } a=
$$

[2]
(b) the value of the other root of the equation $3 x^{2}+a x-30=0$.
7. Given that $x+y=-1$ and $x y=-12$, find the value of
(a) $(x+1)(y+1)$,

> Answer (a) ............................... |2]
(b) $x^{2}+y^{2}$.
8. (a) Giventhat $\frac{x}{b}+\frac{y}{a}=1$, express $y$ in terms of $x, a$ and $b$.

$$
\text { Answer (a) } y=
$$

(b) Giventhat $D=b^{2}-4 a c$, express $b$ in terms of $D, a$ and $c$.
9. Solve the following equations.
(a) $\frac{3}{x+7}=\frac{6}{x}$

Answer (a) $x=$
(b) $(2 x+1)(x-3)=9$.
10. Expand and simplify
(a) $(3 x+y)(2 x+5 y)$,
(b) $(3 x+2)^{2}-(2 x-2)^{2}$.
11. Simplify
(a) $\frac{x-5}{x^{2}-7 x+10}$.

Answer (a)
[2]
(b) $\frac{12 x^{2}+8 x y}{6 x y+4 y^{2}}$Answer (b)[3]
12. The price $(p)$, in cents, of paper is directly propotional to the mass $(m)$ of the paper, in grams. The papercost 50 cents when the mass is 200 g . Find
(a) an equation connecting $p$ and $m$,

> Answer (a) ............................... [2]
(b) the mass of paper, in grams, which cost 200 cents,

Answer (b) $\qquad$ g
[2]
(c) the cost of paper, in cents, with a mass of 300 g .

Answer (c) $\qquad$
$\qquad$
Class : $\qquad$

# Clementi Town Secondary School <br> Mid-Year Examination 2017 <br> Secondary 2 Express 

## MATHEMATICS

## Paper 2

Additional Materials provided: Writing Papers and Graph Paper

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## READ THESE INSTRUCTIONS FIRST

Do not open the booklet until you are told to do so.
Write your name, register number and class on all the work you hand in.
Write in dark blue or black pen on both sides of the paper.
You may use a $n \mathrm{HB}$ pencil for any diagrams or graphs.
Do not use staples, paper clips, glue or correction fluid.
Answer all questions.
If working is needed for any question it must be shown with the answer.
Omission of essential working will result in loss of marks.
The use of an approved scientific calculator is expected, where appropriate.
If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures.
Give answers ind egrees to one decimal place.
For $\pi$, use either your calculator value or 3.142 , unless the question requires the answer in terms of $\pi$.

At the end of the examination, fasten all your work securely together.
The number of marks is given in brackets [ ] at the end of each question or part question. The total numb er of marks for this paper is 50 .

## Answer all questions.

1. Expand and simplify the following expressions.
(a) $(2 m+1)(2 m-1)$
(b) $n+(3-n)^{2}$
2. If $(a+b)^{2}=121$ and $a^{2}+b^{2}=73$, find the value of $a b$.
3. 24 men can finish a job in 7 days.

Assuming that the men work at the same rate, how many more or less men will be needed if the same job has to be completed in 6 days?
4. Solve the equation $\sqrt{\frac{x+1}{2}}=\frac{1}{3}$.

Leave your answer as a fraction in its simplest form.
5. Simplify $\frac{x^{2}-x-6}{x^{2}-49} \div \frac{x-3}{x+7}$.
6. Express each of the following as a single fraction in its simplest form.
(a) $\frac{n+5}{2 m+n}-\frac{3}{4 m+2 n}$
(b) $\frac{1}{x-1}+2$
7. Given that 2 cm on a map represents 5 km on actual ground, find
(a) the scale of the map in the form $1: r$,
(b) the length of a fence on the map if its actual length is 3.8 km ,
(c) the actual area of a lake, in $\mathrm{km}^{2}$, if its area on the map is $3 \mathrm{~cm}^{2}$.
8. Simplify the algebraic fractions
(a) $\frac{3 x+6}{x^{2}-4}$,
(b) $\frac{x^{2}-2 x+1}{x^{2}-8 x+7}$.
9. A villa has two square gardens, a rose garden and a tulip garden, of different dimensions. The rose garden has length $x \mathrm{~m}$, while that of the tulip garden is 2 m longer.
(a) Write down, in terms of $x$, an expression for the area of the tulip garden.
(b) The total area of the two gardens is $130 \mathrm{~m}^{2}$.

Write down an equation in terms of $x$ to represent the information and show that it reduces to $x^{2}+2 x-63=0$.
(c) Solve the equation $x^{2}+2 x-63=0$.
(d) Find the perimeter of the rose garden.
(e) Find the cost of fencing the rose garden if the cost of fencing is $\$ 50$ per metre.
10. Answer the whole of this question on a sbeet of graph paper.

The variables $x$ and $y$ are connected by the equation $y=(x-1)(x-3)$.
Some corresponding values of $x$ and $y$ are given in the following table.

| $x$ | 0 | 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | 3 | 0 | -1 | 0 | $h$ |

(a) Calculate the value of $h$.
(b) Using a scale of 2 cm to represent 1 unit on both axes, draw the graph of $y=(x-1)(x-3)$ for $0 \leq x \leq 4$.
(c) Use your graph to find
(i) the values of $x$ when $y=2$,
(ii) the minimum value of $y$.
(d) State the equation of the line of symmetry.
11. The table below shows the rental details of three soccer fields $A, B$ and $C$.

| Held | Cost (S) | Daration (h) | Rematks |
| :---: | :---: | :---: | :--- |
| $A$ | $k$ | 2 | Fixed rate |
| $B$ | 95 | 1.5 | Weekend rate |
|  | 180 | 1.5 | Weekday rate (1-for-1) |
| C | 65 | 1 | Fixed rate |

(a) The rental cost of field $A$ is fixed at $\$ k$ for every 2 -hour slot.

If 8 boys share the cost of renting one slot of field $A$, each boy will have to pay $\$ 12.50$.
Find the cost of renting field $A$ for 2 hours.
(b) As the cost is too high for the boys, they decided to get more boys to join in their soccer game to share the rental cost of field $A$.
How many more boys should join in if all of them were to pay $\$ 5$ each?
(c) Which field, $B$ or $C$, would be a better deal for weekend rental of 3 hours?

You must show all your working clearly.

## END OF PAPER

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| la | $9 x^{2}-12 x y+4 y^{2}$ |
| :--- | :--- |
| b | 784 |
| 2a | $(x+7)(x-5)$ |
| b | $(3 x-5)(3 x+5)$ |
| c | $3 x y(8-27 x)$ |
| 3a | $\frac{5 x y p q^{2}}{9 z}$ |
| b | $\frac{r}{s^{2} y z^{2}}$ |
| 4a | $A(0,8)$ |
| b | $B(4,0)$ |
| c | $x=1$ |
| d | $P=8$ |
| 5 | The number is 94 or 72 |
| 6a | $\mathrm{a}=1$ |
| b | $x=\frac{-10}{3}=-3 \frac{1}{3}$ |
| 7a | -12 |
| b | $x^{2}+y^{2}=25$ |
| 8a | $y=a b-x a$ |
| $b$ | $b= \pm \sqrt{D+4 a c}$ |
| ba | $x=-14$ |
| (b) | $x=4 \quad x=-1.5$ |
| 10a | $6 x^{2}+17 x y+5 y^{2}$ |
| b | $5 x^{2}+20 x$ |
| 11a | $\frac{1}{(x-2)}$ |
| 9b | $\frac{2 x}{y}$ |
| 12a | $k=0.25$ |
| b | $p=0.25 m$ |
|  | $200=0.25 m$ <br> $m=800$ <br> c |
|  | $P=75$ |

Clementi Town Secondary School
Mid-Year Examination 2017
Secondary 2 Express
Math Paper 2
Answers

| Question | Answers |
| :---: | :---: |
| $1 \mathbf{1}$ | $4 m^{2}-1$ |
| 1b | $9-5 n+n^{2}$ |
| 2 | $a b=24$ |
| 3 | 4 more men |
| 4 | $x=-\frac{7}{9}$ |
| 5 | $\frac{x+2}{x-7}$ |
| 6a | $\frac{2 n+7}{2(2 m+n)}$ |
| 6 b | $\frac{2 x-1}{x-1}$ |
| 7 a | 1:250000 |
| 7 b | 1.52 cm |
| 7 c | $3 \mathrm{~cm}^{2}: 18.75 \mathrm{~km}^{2}$ |
| 8a | $\frac{3}{x-2}$ |
| 8b | $\frac{x-1}{x-7}$ |
| 93 | $(x+2)^{2} \mathrm{~m}^{2}$ |
| 9 c | $x=7$ or -9 |
| 9 d | 28 m |
| 9 e | \$1400 |
| 10 | On graph paper |
| 11. ${ }^{\text {a }}$ | \$100 |
| 11 b | 12 more boys |
| 11 c | Field $B$ is a better deal as it offers a cheaper rental rate. |

