

### TANJONG KATONG SECONDARY SCHOOL Mid-Year Examination 2017 Secondary 1

| CANDIDATE<br>NAME |              | - |
|-------------------|--------------|---|
| CLASS             | INDEX NUMBER |   |

# MATHEMATICS

Paper 1

4048/01

Monday 15 May 2017

1 hour

Candidates answer on the Question Paper.

### READ THESE INSTRUCTIONS FIRST

Write your name, class and register number on all the work you hand in.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer all questions.

If working is needed for any question it must be shown with the answer.

Omission of essential working will result in loss of marks.

The use of an approved scientific calculator is expected, where appropriate.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For  $\pi$ , use either your calculator value or 3.142, unless the question requires the answer in terms of  $\pi$ .

At the end of the examination, fasten all your work securely together. The number of marks is given in brackets [ ] at the end of each question or part question. The total of the marks for this paper is 40.

| For Examiner's Use |  |  |  |  |  |
|--------------------|--|--|--|--|--|
|                    |  |  |  |  |  |
|                    |  |  |  |  |  |
|                    |  |  |  |  |  |
|                    |  |  |  |  |  |
|                    |  |  |  |  |  |

For

Examiner's

Use

2

For Examiner's Use Answer all the questions

1 Express  $\frac{2}{11}$  as a recurring decimal.

2 Using all the numbers below, complete the following table.

3.3, 
$$\pi$$
,  $\sqrt{5}$ ,  $\sqrt[3]{8}$ ,  $-2.1^2$ 

Answer



Given that x is an integer, when x is rounded off to 1 significant figure, the answer is 40.Write the least possible value of x and the largest possible value of x.

Answer

| For<br>Examiner's<br>Use | 4 | m and $n$ are two prime numbers, both larger than 5.<br>"The sum of $m$ and $n$ will always be a prime number."<br>Do you agree with this statement? Justify your answer. | For<br>Examiner's<br>Use |
|--------------------------|---|---|--------------------------|
|                          |   | Answer  |                          |
|                          |   |   |                          |
|                          |   |   |                          |
|                          |   |   |                          |
|                          |   |   | [2]                      |

5 Mary's household paid \$55.75 for water services in March 2017. The water charges are going to increase by 15% by July 2017. Calculate the amount, correct to the nearest cent, Mary would have to pay in July 2017 if their usage of water remains the same.

Answer \$..... [2]

3

6 (a) Given that the value of m+n=-2, find the value of 4m+4n-3.

For

Examiner's

Use

For Examiner's Use

Answer (a)..... [1]

(b) Given that a=2, b=-1 and c=10, calculate the value of  $\frac{\sqrt{c-3ab}}{b}$ .

Answer (b)..... [2]

For

Examiner's

Use

For **7** (a) A rectangle has an area of 69.8 cm<sup>2</sup> and its length is 5.2 cm. Estimate the breadth of the rectangle.

Answer (a) ...... [1]

(b) Estimate the value of  $\sqrt{82} \times \sqrt[3]{7}$ , without using a calculator. Show your working clearly.

Answer (b) ..... [2]

6

For 8 Examiner's Use Mr Sim bought 60 eggs at q cents per dozen.

(a) Express the total amount of money he paid for the eggs, in terms of q.

Answer (a).....cents [1]

(b) He sold them for r cents each. Show that the profit he made is 5(12r-q) cents.

Answer:

(c) Hence, explain what will happen if 12r - q < 0.

Answer

[1]

4048/Sec1MidYear17

For Examiner's Use

[1]

Examiner's 9 A and B are points on the coordinate plane as shown.



(a) Write down the coordinates of point A.

Answer (a)(.....) [1]

(b) Find the gradient of line AB, given that B(3, 1).

(c) Given that C(k, 1) is a point on the coordinate plane such that the area of triangle *ABC* is 9 units<sup>2</sup>, find the possible values of k.

Answer (c)  $k = \dots$  or ...... [2]

4048/Sec1MidYear17

For Examiner's Use

10 For Use

When written as the product of their prime factors,  $360 = 2^{3} \times 3^{2} \times 5,$  $3024 = 2^{4} \times 3^{3} \times 7.$ 

For Examiner's Use

Find the highest common factor of 360 and 3024. (i)

> Answer (a) (i) ..... [2]

Find the smallest positive integer p such that 360p is a perfect (ii) square.

Answer (a) (ii) ..... [1]

(iii) Find the smallest positive integer q for which 360q is a multiple of 3024.

When the students in a school are arranged into rows of 9, 12 or 20, there (b) will be a student who does not fit into any row. Given that the number of students in the school does not exceed 500, find the greatest possible number of students.

Answer (a)..... [2]

4048/Sec1MidYear17

Examiner's

(a)

For Examiner's Use 11 During each week, a site engineer checks the water level above the ground as required by the environment authority of a country. The table below shows the daily water level recorded for a particular week.

For Examiner's Use

| Day                       | Monday | Tuesday | Wednesday | Thursday | Friday |
|---------------------------|--------|---------|-----------|----------|--------|
| Water<br>level (in<br>mm) | +7.3   | -12.0   | -19.3     | +11.7    | -4.6   |

(a) On which day was the lowest level of water recorded?

Answer (a)..... [1]

(b) What is the largest difference in water level between any two days of the week?

Answer (b)...... [2]

(c) Calculate the average water level.

Answer (c)..... [2]

For

Examiner's

Use

For 12 Examiner's Use (a) Solve the inequality  $\frac{4x-11}{2} \le 3x-3 < 4$ . Represent your answer on the number line given below.

Answer (a) x [4]

(b) Hence, write down

(i) the greatest integer value of x which satisfies  $\frac{4x-11}{2} \le 3x-3 < 4$ .

Answer (b) (i) ..... [1]

(ii) the smallest integer value of x which satisfies  $\frac{4x-11}{2} \le 3x-3 < 4$ .

Answer (b) (ii) ..... [1]

### **End of Paper**



## TANJONG KATONG SECONDARY SCHOOL Mid-Year Examination 2017 Secondary 1

| CANDIDATE<br>NAME |  |  |
|-------------------|--|--|
| CLASS             |  |  |

# MATHEMATICS

# 4048/02

Paper 2

5 May 2017

1 hour 15 minutes

Additional Materials:

Writing Paper Graph Paper

## READ THESE INSTRUCTIONS FIRST

Write your name, class and register number on all the work you hand in. Write in dark blue or black pen. You may use an HB pencil for any diagrams or graphs. Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer all questions.

If working is needed for any question it must be shown with the answer.

Omission of essential working will result in loss of marks.

You are expected to use a scientific calculator to evaluate explicit numerical expressions.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For  $\pi$ , use either your calculator value or 3.142, unless the question requires the answer in terms of  $\pi$ .

At the end of the examination, fasten all your work securely together. The number of marks is given in brackets [ ] at the end of each question or part question. The total of the marks for this paper is 50.

2

1 (a) Write down the following numbers in order of size, starting with the smallest.

|   | 0.564, 0.565, 0.56, 0.563  | [1] |
|---|--|-----|
|   | (b) Expand and simplify $a(a+1)-2(2-a)$ .  | [2] |
|   | (c) (i) Evaluate $\frac{\sqrt[3]{249} + 41}{0.55}$ .   |     |
|   | Write down the first five digits on your calculator display.   | [1] |
|   | (ii) Write down your answer to part (i) correct to 3 significant figures.  | [1] |
| 2 | There are three numbers. The second number is thrice the first number.<br>The third number is three less than four times the first number. |     |
|   | (a) Given that the first number is $2n$ , write down an algebraic expression, in terms of $n$ , for  |     |
|   | (i) the second number,   |     |

|     | (ii) the third number.   | [2] |
|-----|--|-----|
| (b) | If the sum of the three numbers is 77, form an equation in $n$ . | [1] |
| (c) | Solve the equation in part (b) and find the third number.        | [3] |

### 3 Answer the whole of this question on a sheet of graph paper.

The table below shows some values of x and the corresponding values of y.

| x | -3 | 0    | 3  |
|---|----|------|----|
| у | 5  | Free | -3 |

- (a) Using a scale of 2 cm to represent 1 unit on each axis, draw a horizontal x-axis for -3 ≤ x ≤ 3 and a vertical y-axis for -3 ≤ y ≤ 5. [3] On your axes, plot the points given in the table and join them with a straight line.
- (b) Use your graph to find the value of x when y = 3.

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#### [Turn over

[1]

| 4 | (a) | Solve the inequality $15-3x < -x-16$ .<br>Hence, find the smallest prime number, x, such that $15-3x < -x-16$ .   | [3]        |
|---|-----|---|------------|
|   | (b) | It is given that $-3 \le x \le 1$ and $-5 \le y \le 2$ , calculate<br>(i) the smallest possible value of $x - y$ ,<br>(ii) the greatest possible value of $x^2 + y^2$ . | [1]<br>[1] |
|   | (c) | Given that $x = 6$ is the solution to the equation $2kx - 7 = x + 11$ , find the value of k.  | [2]        |
| 5 | (a) | (i) Factorise completely $4x^2 - 4xy - py + px$ .   | [3]        |
|   |     | (ii) Factorise $b^2 + b$ . Explain why if b is a positive integer, then $b^2 + b$ is always even.   | [2]        |
|   | (b) | <ul><li>A stamp collector will suffer a loss of 35% if he sells a particular stamp for \$273.</li><li>(i) Find the price he paid for it.</li></ul>                      | [2]        |
|   |     | (ii) What would the selling price be if he wants to make a profit of 15%?   | [2]        |
| 6 | (a) | Solve the following equations.  |            |
|   |     | (i) $2(x-3)-5x = -3$<br>(ii) $\frac{2}{y+5} = \frac{3}{4y-1}$   | [3]<br>[3] |
|   | (b) | (i) Simplify $\frac{\sqrt{64p^2}}{4} \div \frac{10}{p^2}$ .   | [3]        |

(ii) Express  $\frac{y-2}{3} - \frac{y+3}{2}$  as a single fraction in its simplest form. [3]

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[Turn over

- 7 Jasmine and her family plan to visit the Singapore Zoological Gardens by bus from Yishun. To travel to the zoo by bus, the family needs to take Bus 171 from bus stop X near their house. Then, they will need to alight at bus stop Y to take Bus 927 to the zoo.
  - (a) The distance from bus stop X to bus stop Y is 12 km.
    - (i) If Bus 171 travelled at an average speed of 40 km/h, calculate the time taken to travel from bus stop X to bus stop Y.

The distance from bus stop Y to the zoo is 6 km.

(ii) Find the time taken to travel from bus stop Y to the zoo if Bus 927 travelled at an average speed of 30 km/h. [1] Hence, find the total time taken to travel from bus stop X to the zoo, leaving your answer in minutes. [1] State an assumption that you have made in your calculation. [1]

Table 1 below shows information on Bus 927 from Choa Chu Kang Bus Interchange:

| Period                 | 0630 - 0830     | 0831 - 1659     | 1700 - 1900     | After 1900      |
|------------------------|-----------------|-----------------|-----------------|-----------------|
| Estimated waiting time | 13 – 14 minutes | 13 – 18 minutes | 13 – 18 minutes | 13 – 18 minutes |

(b) The family boards Bus 171 from bus stop X at 0930.

When they reach bus stop Y, Bus 927 has just left.

Using your answer in part (a) and **Table 1**, do you think they will definitely be able to reach the zoo by 1015? Show your working clearly.

#### **End of Paper**

[3]

| 1         | 0.18  |                                      | B1  |
|-----------|---|--------------------------------------|---|
| 2         | Rational Numbers  | $3.3^{\circ}, \sqrt[3]{8}, -2.1^{2}$ | B2 (minus 1 mark for<br>each mistake, up to 2<br>mistakes)    |
|           | Irrational Numbers  | $\pi,\sqrt{5}$                       |   |
| 3         | Least: 35<br>Largest: 44  |                                      | BI<br>BI  |
| 4         | No. If $m = 9$ and $n = 7$ , number.  | m + n = 16.16 is not a prime         | B1 – use of specific eg.<br>B1 – correct<br>conclusion        |
| 5         | $\frac{115}{100} \times 55.75 = 64.11$  |                                      | M1 – calculate 15% or<br>115%<br>A1                           |
| <u>6a</u> | -11   |                                      | Bl  |
| 00        | $\frac{\sqrt{c-3ab}}{b} = \frac{\sqrt{10-3(2)(-1)}}{-1} = -4$                         |                                      | A1  |
| 7a        | 14  |                                      | B1 C.A.O  |
| 7b        | $\sqrt{82} \times \sqrt[3]{7}$ $= \sqrt{81} \times \sqrt[3]{8}$ $= 9 \times 2$ $= 18$ |                                      | M1 estimate 82≈81 or<br>7≈8.<br>A1 (do not accept 17)         |
| 8a        | 5q  |                                      | B1  |
| 8b        | 60r - 5q = 5(12r - q)   |                                      | B1 - 60r - 5q   |
| 8c        | Mr Sim will make a loss   | s if $12r - q < 0$ (or $12r < q$ )   | B1 o.e (accept negative<br>profit, Mr Sim will<br>lose money) |
| 9a        | (0, -2)   |                                      | B1  |
| 9b        | $m = \frac{3}{3}$ $= 1$   |                                      | M1 rise/run or<br>change in y/ change in<br>x (nfww)<br>A1    |
| 9c        | -3 or 9   |                                      | B2  |
| 10ai      | $2^3 \times 3^2 = 72$   |                                      | M1 (any method, 2<br>and 3 seen as common<br>factors)<br>A1   |
| 10<br>aii | 10  |                                      | B1  |
| 10a       | 42  |                                      | B1  |

| iii  |                                     |                                       |
|------|-------------------------------------|---------------------------------------|
| 10b  | LCM = 180                           | M1 – finding LCM                      |
|      | No. of students = $361$             | Al                                    |
| 11a  | Wednesday                           | B1                                    |
| 11b  | 11.7 - (-19.3) = 31                 | M1 – largest minus                    |
|      | 6                                   | smallest value or                     |
|      |                                     | smallest minus largest                |
|      |                                     | A1                                    |
| 11c  | 7.3-12.0-19.3+11.7-4.6              | M1 - calculating                      |
|      | 5                                   | average (sum/5)                       |
|      |                                     | A1                                    |
| 12a  | $4x - 11 \le 3x - 3 \le 4$          | M1 Split                              |
|      | $\frac{1}{2}$                       |                                       |
|      | 4x - 11                             | M1 Solving inequality                 |
|      |                                     | by moving x to one                    |
|      | 2                                   | side (either inequality)              |
|      | $x \ge -2.5$ and $x < 2\frac{1}{3}$ |                                       |
|      | 25 (                                | A1 (if improper, A0)                  |
|      | $-2.5 \le x < 2\frac{1}{3}$         |                                       |
|      | <b>O</b>                            | D1                                    |
|      |                                     | DI                                    |
|      | -25 2 <sup>1</sup> x                |                                       |
|      | $\frac{2.5}{3}$                     |                                       |
| 12bi | 2                                   | √B1                                   |
| 12b  | -2                                  | √B1                                   |
| ii   |                                     | · · · · · · · · · · · · · · · · · · · |

## Secondary One Mathematics Mid-Year Examination 2017 Paper 2 Marking Scheme Deduct maximum of 1 mark overall for no statement/ units Statement to be stated for Question 2(c) / 5(b) (i) & (ii) / 7(a) (i) (ii) and (b)

|          | Solution   | Marks      | Remarks                                |
|----------|--|------------|--|
| 1(a)     | 0.563, 0.564, 0.565, 0.56  | B1         |  |
| 1(b)     | a(a+1)-2(2-a)  |            | Either $a^2 + a$ or                    |
|          | $=a^{2}+a-4+2a$  | B1         | -4+2a seen                             |
|          | $=a^2+3a-4$  | B1         |  |
| 1(c)(i)  | 85.983   | <b>B</b> 1 |  |
| 1(c)(ii) | 86.0   | B1√        |  |
|          |  |            | 5 marks                                |
| 2(a) (i) | 6 <i>n</i> or 3(2 <i>n</i> )   | B1         |  |
| 2(a)(ii) | 8n-3  or  4(2n)-3  | B1         |  |
| 2(b)     | 2n + 6n + (8n - 3) = 77  | B1√        | 2n + (a)(i) + (a)(ii) =<br>77 seen     |
| 2 (c)    | 16n = 80   | M1         | simplifying variable                   |
|          | n=5  | Al         | on one side                            |
|          | Third number $= 37$  | <b>B</b> 1 |  |
|          |  |            | 6 marks                                |
| 3 (a)    | Axes correctly drawn and labeled<br>correct scale used<br>Correct plotting of points | B1<br>B1   | B0 for missing pts or                  |
|          | Joining of points with a line  | B1         | any l pt plotted<br>wrong              |
| 3 (b)    | x = -1.5 or 1.50   | B1         |  |
|          |  |            | 4 marks                                |
| 4(a)     | 15 - 3x < -x - 16  | -          | Grouping of variable                   |
|          | 2x > 31  | M1         | or constant                            |
|          | x > 15.5<br>Smallest prime number = 17   | A1<br>B1√  | A0 for $\frac{31}{2}$                  |
|          |  | 2.1        | Must see                               |
|          |  |            | $x > cons \tan t$                      |
| 4(b)(i)  | -3-2=-5  | B1         |  |
| 4(b)(ii) | $(-3)^2 + (-5)^2 = 34$   | B1         |  |
| 4(c)     | 12k - 7 = 17<br>12k - 24   | M1         | Substituting of value to solve for $h$ |
|          | k = 2  | Al         |  |
|          |  |            | 7 marks                                |

| EL MAN      | . 2 .   |                        |   |
|-------------|---|------------------------|---|
| 5(a)(1)     | $4x^{2} - 4xy - py + px$ $= 4x(x - y) - p(y - x)$   | M1                     | Either $4x(x-y)$ or $p(y-x)$  |
|             | =4x(x-y)+p(x-y)   | Bl                     | p(x-y) seen (SOI)   |
|             | =(4x+p)(x-y)  | A1                     |   |
| 5(a)(ii)    | $b^2 + b = b(b+1)$  | Bl                     |   |
|             | b and $b$ +1 are consecutive integers, thus one of them must<br>be even. The <b>product</b> of an <b>even</b> integer with another<br>integer is always even. / <b>Odd</b> / <b>Even integer multiply</b> by<br><b>another integer</b> will always be even. | B1                     | Product and even seen   |
| 5 (b) (i)   | 273 100   | <b>M</b> 1             | o.e.  |
|             | $Price = \frac{1}{65} \times 100$   | 4.1                    |   |
|             | = \$420   | AI                     |   |
| 5 (b) (ii)  | Selling Price = $\frac{115}{110} \times 420$  | M1 √                   | 115% x (b)(i)   |
|             | 100 - \$483   | Al                     |   |
|             |   |                        | 0 months  |
| 6120        |   | DI                     | 9 marks   |
| 6 (a) (1)   | 2(x-3)-5x=-3  | BI                     | for $2(x-3)$  |
| а.<br>С     | 2x - 6 - 5x = -3  | M1                     | Grouping of variable/   |
| 00.4 s 1    | r = -1  | irana z                | constant 3  |
| an an Suite |   | iller <b>Al</b> en sta | A0 for $-3$   |
| 6 (a)(ii)   | $\frac{2}{y+5} = \frac{3}{4y-1}$ $2(4y-1) = 3(y+5)$ $8y-2 = 3y+15$ $5y = 17$ $y = 3\frac{2}{5}$   | M1<br>M1<br>A1         | Remove denominator<br>Group constant /<br>variable<br>A0 for $\frac{17}{5}$ |
|             | $\frac{\sqrt{64p^{2}}}{4} \div \frac{10}{p^{2}}$ $= \frac{8p}{4} \times \frac{p^{2}}{10}$ $= \frac{p^{3}}{5} / \frac{1}{5} p^{3}$   | B1<br>M1<br>A1         | For 8p<br>x $\frac{p^2}{10}$ seen   |

| 6(b)(ii)   | $\frac{2(y-2)}{3} - \frac{y+3}{2} = \frac{2y-4-3(y+3)}{6}$   | M1 | Express as a single<br>fraction with<br>common<br>denominator<br>For correct expansion  |
|------------|--|----|---|
|            | $=\frac{2y-4-3y-9}{2}$   | B1 | of -3y-9  |
|            | $=\frac{-y-13}{6} \text{ or } \frac{-(y+13)}{6}$   | A1 | ISW   |
|            |  | D. | 12 marks  |
| 7(a)(i)    | Time taken from Bus Stop X to Bus Stop $Y=\frac{12}{40}h$<br>= $\frac{3}{10}h$ or 18 min                         | B1 |   |
| 7 (a) (ii) | Time taken from Bus Stop Y to the zoo = $\frac{1}{5}$ h or 12 min  | B1 |   |
|            | Total time taken from Bus Stop X to the $zoo = 18 \min + 12 \min = 30 \min$                                      | B1 | B0 if answer given in hour  |
|            | Assumption: No waiting time required during transfer of buses  | B1 |   |
| 7(b)       | Max waiting time needed for Bus $927 + Total travel time = 30 + 18 = 48 minutes$                                 | B1 | Indicated the<br>maximum waiting<br>time for Bug 027  |
|            |  | B1 | Calculating total time<br>needed to reach zoo/<br>Award 1 mark if<br>student use minimum<br>waiting time (i.e. 13<br>+ 30 = 43 minutes) |
|            | If they need to be at the zoo by 1015, total time needed should not be more than 45 minutes.<br>No, they cannot. | Bl | Conclusion with<br>working shown  |
|            |  |    | 7 marks   |

B1 45 mins seen

B1 45mins + waiting time > 1015

B1 Conclusion indicating that the time reached will be > 1015

B1 45 mins seen

B1 30 mins + (16, 17, 18) mins or (a) (ii) + 18 mins > 45 mins

B1 Conclusion indicating time taken > 45 mins

B1 45 mins seen

B1 (a)(ii) (28mins or more) + 18 mins > 45 mins seen

B1 B1 Conclusion indicating time taken > 45 mins

B1 45 mins seen

B1 (a)(ii) (26mins or less) + 18 mins < 45 mins seen

B1 B1 Conclusion indicating total time taken < 45 mins - cannot reached