Class:

SHUQUN SECONDARY SCHOOL 2017 End-of-Year Examination Secondary 1 Express

MATHEMATICS

Paper 1

05 October 2017

Candidates answer on the Question Paper

1 hour 30 minutes

INSTRUCTIONS TO CANDIDATES

Write your name, class and class index number in the spaces at the top of this page and all the work you hand in.

Write in blue or black pen.

You may use a pencil for any diagrams or graphs.

Do not use staples, paper clips highlighters, glue or correction fluid.

Answer all questions.

If working is needed for any question, it must be shown with the answer. Omission of essential working will result in loss of marks.

You are expected to use a scientific calculator to evaluate explicit numerical expressions.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For π , use either your calculator value or 3.142, unless the question requires the answer in terms of π .

At the end of the examination, fasten all your work securely together. The number of marks is given in brackets [] at the end of each question or part question.

The total number of marks for this paper is 50.

This question paper consists of 12 printed pages.

[Turn over]

Answer all questions.

1. A wooden block has a mass of 165 grams, correct to the nearest gram. Find the least possible mass of the wooden block.

Given that 2k < 20, write down
 (a) the largest integer value of k,

2.

Answer: [1]

Answer: [1]

Answer: g [1]

(b) the largest prime value of k.

4. Here is a recipe for a chocolate dessert.

	Serv	ves 4 people
100	g	Flour
75	g	Plain Chocolate
50	g	Butter
300	ml	Milk
65	g	Sugar
5	ml	Vanilla Essence
2		Eggs

(a) Fiona is making the dessert for 14 people. How many grams of butter does she need?

Answer: _____ g [1]

(b) Michael uses the same recipe with 1.5 litres of milk. For how many people is he making the chocolate dessert?

Answer: ______ people [1]

- 5. Write down the next term for each sequence.
 - (a) 14, 10, 6, 2, _____

Answer: _____ [1]

- **(b)** 1, 4, 9, 16, _____
- Answer: _____ [1]

- The temperature of a city at 09 00 is -6° C. 6. The temperature at 14 00 is 14°C.
 - (a) Calculate the temperature difference of the city between 09 00 and 14 00.

Answer: <u>°C</u> [1]

(b) Assuming that the temperature rises at a steady rate, find the temperature at 11 00.

Answer: -- °C [2]

An athlete runs 10 000 metres in 40 minutes. 7. Calculate his average speed in kilometres per hour.

Answer: _____ km/h [3]

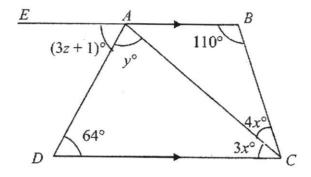
8. (a) Express 360 as a product of its prime factors, giving your answer in index notation.

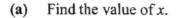
Answer: _____ [2]

(b) Hence, find the smallest positive integer z such that 360z is a cube number.

Answer: $\underline{z} =$ [1]

9. In the figure below, *EAB* is parallel to *DC*. $\angle EAD = (3z+1)^\circ$, $\angle ADC = 64^\circ$, $\angle DAC = y^\circ$, $\angle ACD = 3x^\circ$, $\angle ACB = 4x^\circ$ and $\angle ABC = 110^\circ$.





Answer: x = [1]

(b) Find the value of y.

Answer: y = [1]

(c) Find the value of z.

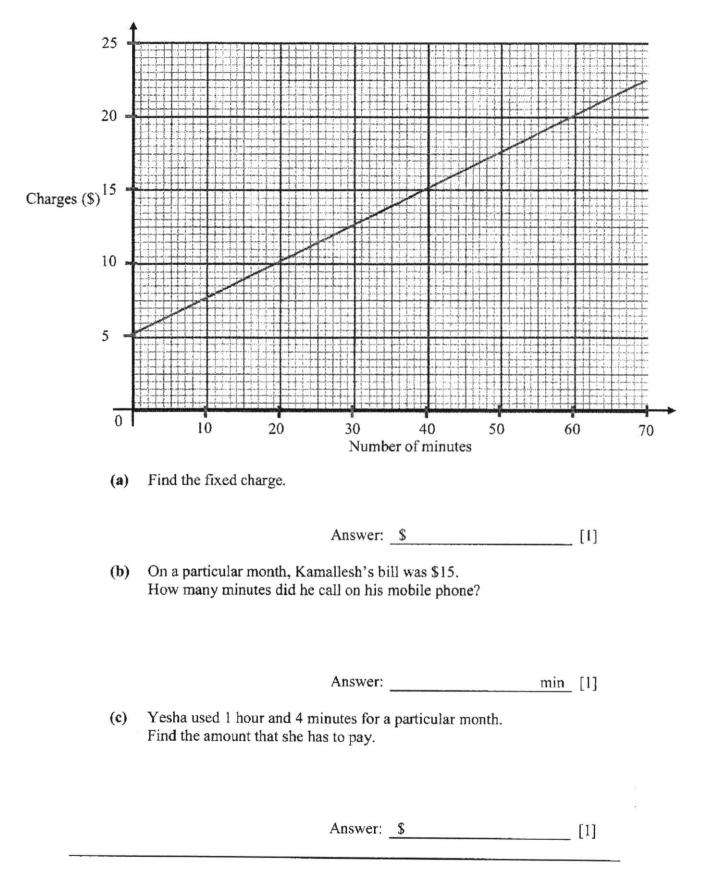
Answer: z = [1]

SQSS 1 EXP EOY P1 2017

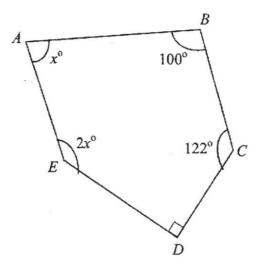
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10. A telephone company charges customers for the number of minutes they called every month.

There is a fixed charge and a charge for each minute of calls made.



11. (a) The diagram shows a pentagon ABCDE. Calculate the value of x.



Answer: x = [3]

(b) Calculate the number of sides of a regular polygon if each of its exterior angle is 30°.

Answer:

Mathematics

sides [1]

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(a) Simplify the ratio 1.6 kg : 400 g. 12.

Answer: _____ [1]

(b) If $p:q = \frac{3}{4}:2$ and $p:r = \frac{1}{3}:\frac{1}{2}$, find q:r.

Answer: _____ [3]

By rounding each number to 1 significant figure, estimate the value of 13. (a)

29.83-3.05×7.8.

Show your working.

Answer: _____ [2]

(b) Estimate the value of $\sqrt{50} \times \sqrt[3]{25}$.

Answer: _____ [2]

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14. (a) Express $\frac{2}{5}$ % as a fraction in the simplest form.

Answer: [1]

(b) Express \$3 as a percentage of 15¢.

Answer: ______% [1]

(c) Chris bought a bicycle in 2016. One year later, he sold it at a loss of 30% at \$581. Calculate the price he paid for the bicycle in 2016.

Answer: \$

[2]

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15. (a) Solve 3(2x-3) = 4x - 1.

Answer: x = [2]

(b) If $n-2y = \frac{3y-n}{m}$, find the value of *n* when y = 5 and m = -3.

Answer: <u>n = [3]</u>

12

1		
A		В
	10 cm	

(a)	Construct the triangle ABC.	[2]
(b)	Measure and write down $\angle ACB$.	
	Answer:	° [1]
(c)	Construct the angle bisector of $\angle ABC$.	[1]
(d)	Construct the perpendicular bisector of AB.	[1]
(e)	The perpendicular bisector of AB meets the angle bisector of point M . Measure and write down the length of BM .	∠ABC at

Answer:	cm	1

End	of	Pa	per
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Class:

SHUQUN SECONDARY SCHOOL 2017 End-of-Year Examination Secondary 1 Express

MATHEMATICS

PAPER 2

06 October 2017

Additional material: Writing paper Graph paper (1 piece)

1 Hour 30 Minutes

READ THESE INSTRUCTIONS FIRST

Write your name, class and index number in the spaces at the top of this page and on all the work you hand in.

Write in blue or black pen.

You may use a pencil for any diagrams or graphs.

Do not use staplers, paper clips, highlighters, glue or correction fluid.

Answer all questions.

If working is needed for any question, it must be shown with the answer. Omission of essential working will result in loss of marks.

Calculators should be used where appropriate.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For π , use either your calculator value or 3.142, unless the question requires the answer in terms of π .

The number of marks is given in brackets [] at the end of each question or part question.

The total number of marks for this paper is 50.

This question paper consists of 6 printed pages.

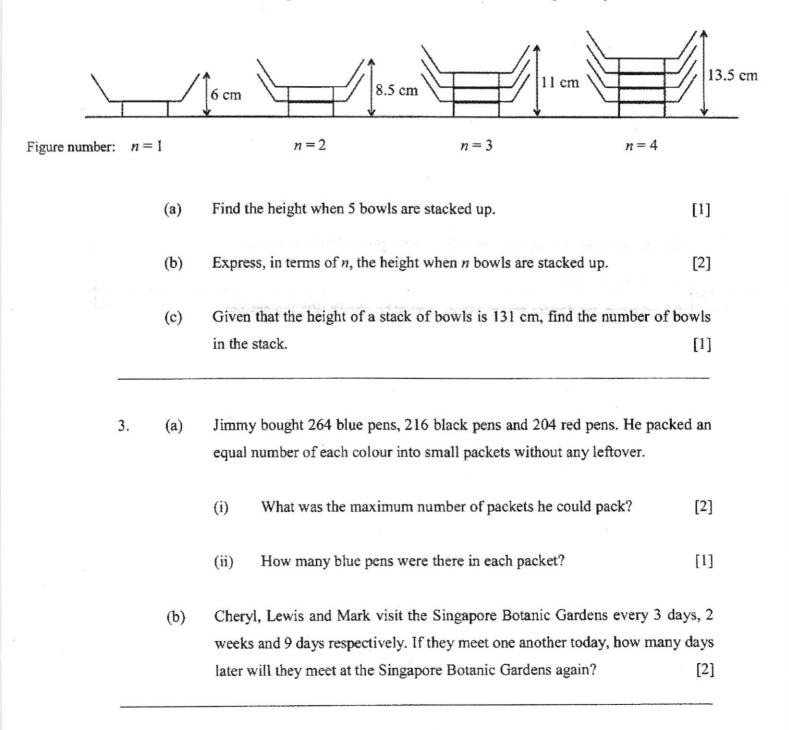
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2 Answer all the questions.

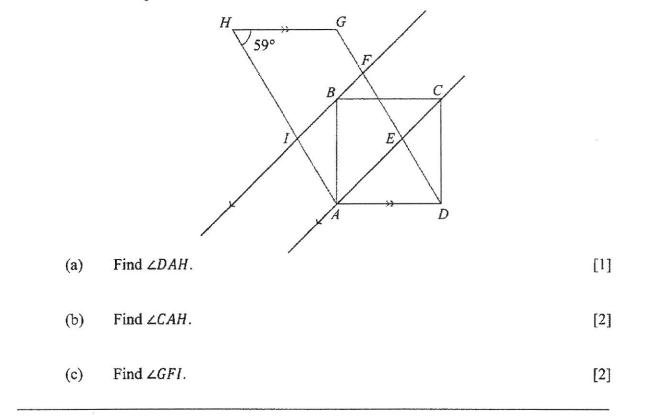
1. (a) Factorise
$$4a + 8aw - 18ax$$
. [1]

(b) Simplify
$$\frac{2x+4}{3} - \frac{1-x}{4}$$
. [3]

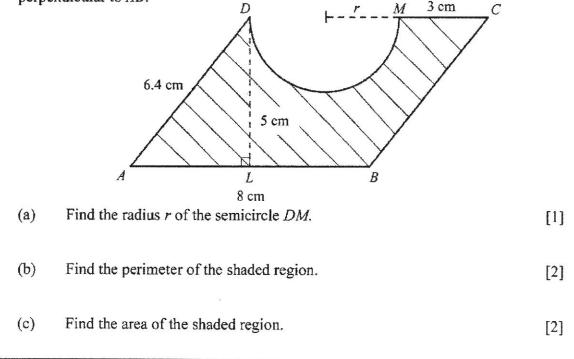
2. Some porcelain bowls are stacked up as shown below. The heights when 1, 2, 3 and 4 bowls are stacked up are 6 cm, 8.5 cm, 11 cm and 13.5 cm respectively.



4. In the diagram below, *ABCD* is a square and *ADGH* is a parallelogram. The lines *CEA* and *FBI* are parallel lines.



5. In the diagram below, ABCD is a parallelogram where a semicircle DM has been cut out from it. It is given that AB = 8 cm, AD = 6.4 cm, CM = 3 cm and DL = 5 cm. DL is perpendicular to AB.



SQSS I Exp EOY 2017 P2

- Chloe drove a distance of 360 km from Point A to Point B at an average speed of u km/h.
 - (a) Write down the expression for the time, in hours, that she took for the journey. [1]
 - (b) She then returned by the same route at an average speed of 2u km/h. Write down the expression for the time, in hours, that she took for the return journey.
 [1]
 - (c) Given that the difference between these two times was 2.5 hours, form an equation in u. Show that the equation can be reduced to 360 = 5u. [2]
 - (d) Hence, solve the equation. [1]
 - (e) Find the time, in hours, Chloe took for the return journey. [1]

7. The volume ratio of water, syrup and ice in an iced lemon tea drink is 7:2:3.

- (a) Calculate the percentage of ice in the iced lemon tea drink. [1]
- (b) Calculate the volume of water in a 600 ml iced lemon tea drink. [1]
- (c) Given that the water costs \$1.80 per litre, the syrup costs \$14.40 per litre and the ice costs \$2.20 per litre, calculate the cost price of each 600 ml iced lemon tea drink.
- (d) If the drink is sold at a profit of \$0.50, find the selling price after applying
 GST of 7%, correcting your answer to the nearest cent. [2]

8. Figure 1 below shows a water trough with a uniform cross section of trapezium shape. It is given that AB = 35 cm, BC = 40 cm, EF = 21 cm and HM = 14 cm.

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- (a) Find the volume of the water trough. [2]
- (b) Figure 2 shows an open cylindrical container of height 30 cm. When all the water from the fully filled water trough is poured into the cylindrical container, the water reaches its brim.
 - (i) Find the radius r of the cylindrical container, leaving your answer to 3 significant figures. [2]
 - (ii) Find the total interior surface area of the open cylindrical container that is in contact with the water, leaving your answer to 3 significant figures. [2]

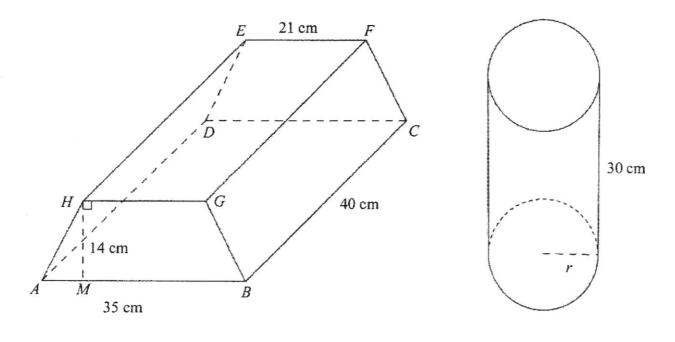


Figure 1

Figure 2

9. Answer the whole of this question on a sheet of graph paper.

The table below shows the corresponding x and y values for the equation: y = -2x + 3.

x	-2	-1	0	1	2
у	7	а	3	b	-1

(e)	Find the coordinates of the point where the two graphs intersect.	[1]
(d)	Draw the line $y = 2$ and state its gradient.	[2]
(c)	From the graph, find the value of x when $y = 6$.	[1]
	Using a scale of 4 cm to represent 1 unit on the x-axis and 2 cm to represent unit on the y-axis, draw the graph of $y = -2x + 3$ for $-2 \le x \le 2$.	nt 1 [3]
(a)	Find the values of a and b .	[2]

End of Paper

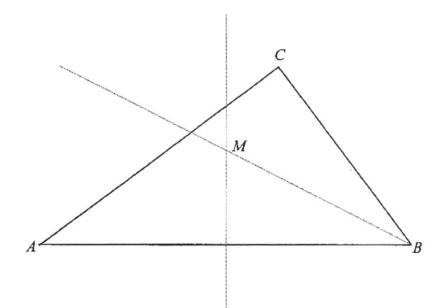
SQSS 1Exp EOY 2017 P2

Qn.	Answer	Marks
1.	164.5g	B1
2.	$-0.8, \frac{4}{5}, 83\%, 0.83, 0.83$	BI
3.	(a) 9	B1
	(b) 7	Bl
4.	(a) 175g	B1
	(b) 20 people	B1
5.	(a) -2	B1
	(b) 25	B1
6.	(a) 20°C	Bl
	(b) 5 h 20°C	$1 h4 \circ C - M1$
	2 h 8°C	$1n4^{\circ}C - M1$
	Temperature at 1100 is 2°C.	Al
7.	$10 \text{ km} \frac{2}{3} \text{h}$	$10 \text{ km or } \frac{2}{3} \text{h seen} - \text{M1}$
	Average speed = $\frac{10km}{\frac{2}{3}h}$	Applying $s = d/t - M1$
	=15 km/h	A1
8.	(a) $360 = 2^3 \times 3^2 \times 5$	Al (M1 – for division method)
	(b) z = 75	B1
9.	(a) $7x = 180 - 110$	
	x = 10 (b) y = 180 - 64 - 3(their 10) = 86	B1 B1
	(c) $3z + 1 = 64$	BI
	<i>z</i> = 21	B1
10.	(a) \$5	Bl
	(b) 40 min	B1
	(c) \$21	

Answer Key to SQSS 1 EXP EOY P1 2017

11.	(a) $(5-2) \times 180 = 540$	M1
	x + 2x + 90 + 122 + 100 = 540	Ml
	3x = 228	
	x = 76	A1
đ	(b) 12 sides	B1
12.	(a) 4:1	B1
12,		
	$p:q=\frac{3}{4}:2$	
	(b) $= 3:8$	M1 (either 3:8 or 2:3 seen – ratio
	= 6:16	in integer)
	$p:r=\frac{1}{3}:\frac{1}{2}$	M1 (p:q:r or equivalent seen)
	= 2:3	
	= 6 : 9	
	q: r = 16:9	A1
13.	30-3×8	M1
15.	(a) $= 6$	Al
	$\sqrt{49} \times \sqrt[3]{27}$	
	(b) $= 7 \times 3$	M1 A1
	= 21	
14.		B1
14.	(a) $\frac{1}{250}$	
	(b) 2000%	B1
	(c) 70% \$581	M1
	100% \$830	A1
15.	(a) $3(2x-3) = 4x - 1$	
	6x - 9 = 4x - 1	M1
	2x = 8 $x = 4$	A1
	$n - 2(5) = \frac{3(5) - n}{-3}$	
	$n-10 = \frac{15-n}{-3}$	M1
	(b) $-3n+30=15-n$	M1
	-2n = -15	A 1
	n = 7.5	Al

16.	(a) as seen below.	B1 - AC = 8 cm
		B1 - BC = 6 cm
		(minus 1 mark if no working arc)
	(b) 90° ±1°	ecf I based on their drawn $\triangle ABC$
	(c) as seen below.	B1 (must see construction arcs & measure 26.5°)
	(d) as seen below.	B1 (must see construction arcs & measure 90° and 5cm)
	(e) BM = $5.6 \text{ cm} \pm 0.1 \text{ cm}$	ecf 1 based on their drawn $\triangle ABC$



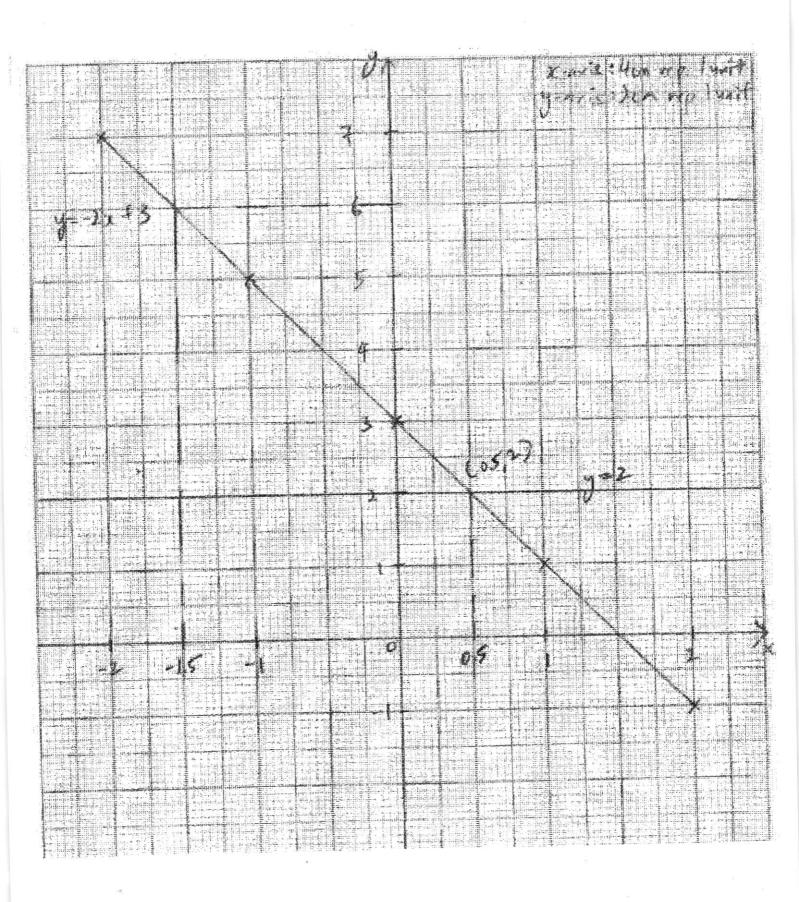
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Question	Answer	Mark	Remarks
l(a)	2a(2+4w-9x)	B1	
	$\frac{2x+4}{3} - \frac{1-x}{4}$ = $\frac{4(2x+4)}{12} - \frac{3(1-x)}{12}$ = $\frac{4(2x+4)-3(1-x)}{12}$	M1	
1(b)	$=\frac{12}{12}$ $=\frac{8x+16-3+3x}{12}$ $=\frac{8x+3x+16-3}{12}$	M1	
	$=\frac{12}{11x+13}$	A1	
2(a)	16 cm	B1	
2(b)	d = 2.5 cm $T_o = 6 - 2.5 = 3.5$ $T_n = 3.5 + 2.5n$	B1 B1	Accept other valid methods
2(c)	3.5 + 2.5n = 131 2.5n = 127.5 n = 51	BI	
3(a)(i)	2 264 216 204 2 132 108 102 3 66 54 51 22 18 17	M1	Award M1 for any correct method used to find HCF
	$HCF = 2 \times 2 \times 3 = 12$	A1	
3(a)(ii)	No. of blue pens = 22	B1	
3(b)	$2 \text{ weeks} = 14 \text{ days}$ $\begin{array}{r rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	M1	Award M1 for any correct method used to find LCM
	$LCM = 2 \times 3 \times 3 \times 7 = 126$	A1	
4(a)	$\angle DAH = 180^\circ - 59^\circ = 121^\circ$ (int. $\angle s, HG//AD$)	B1	
4(b)	$\angle CAD = \angle CAB = 45^{\circ}$ (Line CA is an angle bisector) $\angle CAH = \angle DAH - \angle CAD = 121^{\circ} - 45^{\circ} = 76^{\circ}$	M1 Al	Accept other correct methods
4(c)	$\angle AEG = 180^{\circ} - 76^{\circ} = 104^{\circ}$ (int. $\angle s, HA//GE$) $\angle GFI = \angle AEG = 104^{\circ}$ (corr.	MI Al	Accept other correct methods

2017 SQSS 1Exp Maths EOY Paper 2 Answer Scheme

	$\angle s, IF //AE)$		
5(a)	Diameter = $8 - 3 = 5$ cm r = 2.5 cm	B1	
5(b)	Perimeter of shaded region = $6.4 + 8 + 6.4 + 3 + \frac{1}{2}(2\pi \times 2.5)$	M1	
	= 31.65398 = 31.7 cm (to 3 s.f.)	Al	
5(c)	Area of the shaded region = Area of parallelogram – area of semicircle = $8 \times 5 - \frac{1}{2}\pi (2.5)^2$	M1	
	= 30.18252 = 30.2 cm ² (to 3 s.f.)	A1	
6(a)	Time taken = $\frac{360}{u}$ hours	B1	
6(b)	Time taken = $\frac{360}{2u}$ hours	B1	
6(c)	$\frac{\frac{360}{u} - \frac{360}{2u}}{\frac{2u}{2u} - \frac{360}{2u}} = 2.5$ $\frac{\frac{720}{2u} - \frac{360}{2u}}{\frac{2u}{2u}} = \frac{5u}{2u}$ $720 - 360 = 5u$	M 1	
•(•)	360 = 5u (shown)	A1	
6(d)	5u = 360 $u = 72 km/h$	B1	
6(e)	Time taken = $\frac{360}{2(72)}$ = 2.5 hours	Bl	
7(a)	Percentage of ice = $\frac{3}{12} \times 100\% = 25\%$	B 1	
7(b)	Volume of water = $\frac{7}{12} \times 600 = 350 \text{ ml}$	B1	
	Volume of syrup $=\frac{2}{12} \times 600 = 100$ ml Volume of ice $=\frac{3}{12} \times 600 = 150$ ml	15	
7(c)	Cost price = $\frac{350}{1000} \times 1.80 + \frac{100}{1000} \times 14.40 + \frac{150}{1000} \times 2.20$	M1	
	= \$0.63 + \$1.44 + \$0.33 $= 2.40	Al	
7(d)	Selling price before GST = $$2.40 + 0.50 = $$2.90$ Selling price after GST = $1.07 \times 2.90	M1	
	= $\$3.103$ = $\$3.10$ (to the nearest cent)	A1	

8(a)	Volume of water trough		
	= area of trapezium cross section \times		
	length of trough		
	$=\left[\frac{1}{2}(35+21) \times 14\right] \times 40$	M1	
	$= 15680 \text{ cm}^3$	Al	
8(b)(i)	Volume of water trough = volume of		
	cylindrical container = 15680 cm^3		
	$\pi r^2(30) = 15.680 \text{ cm}^3$	MI	
	$r^2 = \frac{15680}{20-1}$		
	$r^2 = \frac{1}{30\pi}$		
	$r = \frac{15680}{15680}$		
	$7 = 30\pi$		
	= 12.898448		
	= 12.9 cm (to 3 s.f.)	A1	
8(b)(ii)	Total interior surface area		
	$=\pi r^2+2\pi rh$		
	$=\pi(12.9)^2+2\pi(12.9)(30)$	Ml	
	= 2954.3851		
	$= 2950 \text{ cm}^2$ (to 3 s.f.)	A1	
9(a)	<i>a</i> = 5	B1	
	b = 1	B1	
9(b)			P2 for all 5 correct
		P2	points plotted.
			(Award 1 mark for 3
	Refer to attached graph		correct points
	rener to utilization gruph		plotted)
		C1	C1 for straight line
			accurately drawn
9(c)	x = -1.5	B1	
9(d)	Refer to attached graph	B1	
	(Line $y = 2$)		
	Gradient = 0	B1	
9(0)	Coordinates of point of intersection:	DI	
9(e)	(0.5, 2)	B1	



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