# CHIJ St Nicholas Girls' School 2018 Preliminary Examination Mathematics Paper 1

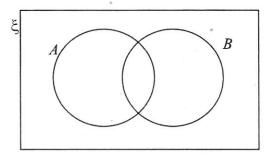
1 (a) Given  $x^9 = 9^0$ , find the value of x.

**(b)** Simplify 
$$\frac{x^2}{3y} \div \frac{x}{9y^2}$$
.

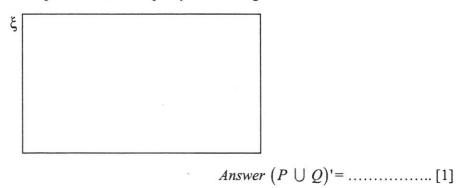
2 Factorise  $2p-2q-p^2+pq$ .

3 Write as a single fraction in its simplest form  $\frac{5x}{(3-x)^2} - \frac{1}{x-3}$ .

4 (a) On the Venn diagram, shade the region which represents  $A' \cap B$ .



(b) Given that P is a subset of Q, simplify  $(P \cup Q)'$ . You may use the space below to help in your investigation.



5 A shuttle bus is due to arrive at the ABC station at a certain time every morning.

The numbers of minutes by which the bus was late on ten successive days are shown below.

(b) Find the mean number of minutes by which the bus was late.

[1]

**6** Given that *p* is a positive integer,

(a) write down expressions for the next two even numbers after 2(p-1).

(b) (i) find, in its simplest form, an expression for the sum of the squares of these three even numbers,

		Answer	[2]
(ii) exp	lain why this sum is a multiple	e of 4.	
Answer			
			[1]

7 (a) Express 40 and 138 as the product of their prime factors.

(b) Hence, find the smallest positive integer k such that 138k is divisible by 40.

Answer smallest positive integer  $k = \dots$ [1]

8 A wooden cube with side 8 cm is cut into two-centimetre cubes.All of the two-centimetre cubes are then arranged to form a cuboid with height greater than 8 cm.

The perimeter of the top of the cuboid is 36 cm.

Find the height of the cuboid.

Answer ..... cm [2]

- 9 A map is drawn to a scale of  $1:40\ 000$ .
  - (a) This scale can be expressed as 1 cm represents n km.Find n.

(b) The distance between a seaport and an airport on the map is 60 cm.

Find the actual distance, in kilometres, between the seaport and the airport.

Answer ...... km [1]

(c) A bus depot has an actual area of  $8 \text{ km}^2$ .

Find the area, in square centimetres, of the bus depot on the map.

*Answer* ..... cm<sup>2</sup> [2]

CHIJ SNGS Preliminary Examinations 2018 - Mathematics 4048/01

10 (a) Fynn deposited \$m into an account that paid a compound interest of 1.85% per annum. He made no other deposits or withdrawals for three years. At the end of three years, he had \$2509.26 in his account.

Find the value of m, giving your answer correct to the nearest dollar.

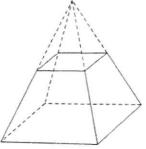
(b) Fynn withdrew all his money from the bank and used 30% of it to buy a watch. Subsequently he sold the watch for a profit of 60%.

Find the selling price of the watch.

Answer \$..... [2]

11 The diagram shows a frustum obtained by removing a small pyramid with height half of that of the original pyramid.

[A frustum is a portion of a pyramid that is left after a smaller pyramid is removed from the top.]



Find the ratio of the volume of the frustum to the volume of the original pyramid.

Answer ...... [2]

12 (a) Express  $3x^2 - 12x$  in the form  $3[(x+a)^2 + b]$ .

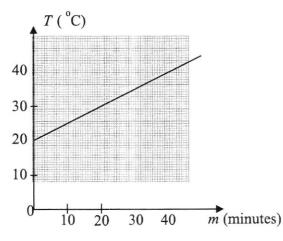
(b) Write down the smallest value of  $3x^2 - 12x$ .

13 Cooking oil is sold in two sizes:

\$4.80 for each 2 kg-bottle \$6.95 for each 3 kg-bottle Which bottle gives the better value? You must show your calculations.

Answer The ..... kg-bottle gives the better value. [2]

14 The graph shows the temperature,  $T^{\circ}C$ , of the water in a hot water tank after the heater is switched on for *m* minutes.



Use the graph to find

(a) the increase in temperature of the heater when it is switched on for 20 minutes,

Answer ..... °C [1]

(b) an equation for T in terms of m.

15 The distance between the points M(k, 7) and N(9, k) is  $\sqrt{20}$ .

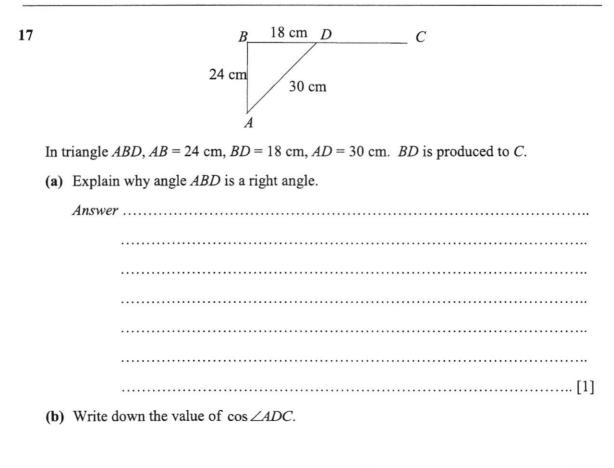
Given that k > 10, find the value of k.

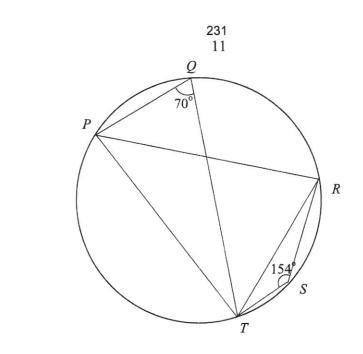
- 230 10
- 16 The table shows some corresponding values of x and y of the equation of a line.

x	-1	0	b	3
y	2	a	0	-18

(a) Find the equation of the line.

(b) Hence find the value of a and of b.





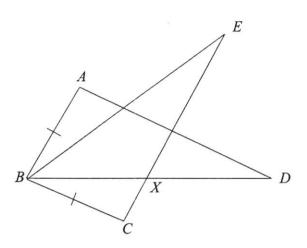
In the diagram, P, Q, R, S and T are points on the circumference of a circle. Angle  $TQP = 70^{\circ}$  and angle  $TSR = 154^{\circ}$ .

(a) Find angle *PTR*.Give a reason for each step of your working.

Answer angle PTR =.....[3]

(b) There is a point A on the same side of PT as point R. Angle  $TAP = 90^{\circ}$ .

Determine if point *A* lies on the circumference of the circle, inside or outside the circle. Justify your answer.



(a) In the diagram, BA = BC, angle ABE = angle CBD and angle BEC = angle BDA.
 Explain why triangles ABD and CBE are congruent.

	Answer	•••••		•••••					
						•••••		•••••	
				•••••				•••••	
								•••••	
									[2]
(h)	Given fu	rther th	nat angl	$e \ ARF =$	angle R	FC what	home of an	adrilatoral	in ADCE 9
	Justify yo		-	CADL	aligie D	EC, what	type of qu	aumaterar	IS ADCE ?
	Justify yo	our ans	wer.						IS ADCE ?
	Justify yo	our ans Quadri	wer.	ABCE is	sa				IS ADCE ?
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20 The table shows the number of people in groups of 1, 2, 3 and 4 people who attended a travel fair exhibition during a two-hour period.

No. of people in each group	1	2	3	4
No. of groups	20	94	85	26

Find

.

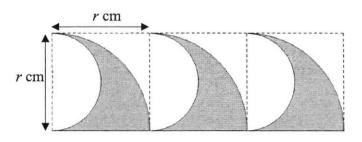
(a) the total number of people who attended the exhibition during the two-hour period,

(b) the median number of people per group,

(c) the percentage of groups with at least 2 people.

Answer .....% [1]





A surfing brand's logo consists of 3 waves. Each wave is made up of a quadrant with a semicircle removed.

(a) Find the perimeter of the logo in terms of r.

The logo is drawn and then cut from a piece of fabric measuring 3r cm by r cm.

(b) Given that the area of the remaining fabric is  $16.4 \text{ cm}^2$ , find the value of r.

**22** A is the point (-4, 11). The position vector of B is  $\begin{pmatrix} 10 \\ 4 \end{pmatrix}$ .

(a) Express  $\overrightarrow{BA}$  as a column vector.

Answer ......[1]

**(b)** Calculate  $|\overrightarrow{AB}|$ .

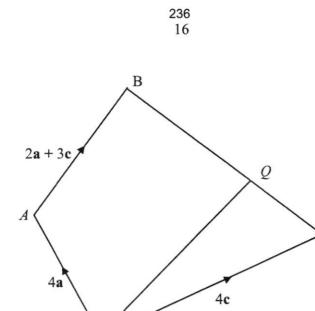
. .

Answer ..... units [1]

$$\overrightarrow{BC} = \begin{pmatrix} 0 \\ 6 \end{pmatrix} \text{ and } D \text{ is the point } (0, d).$$
(c) (i) Find the column vector  $\overrightarrow{OC}$ .

(ii) If  $\overrightarrow{BA}$  is parallel to  $\overrightarrow{CD}$ , find the value of d.

*Answer d* = .....[3]



*OABC* is a quadrilateral.  $\overrightarrow{OA} = 4\mathbf{a}, \quad \overrightarrow{OC} = 4\mathbf{c}, \text{ and } \quad \overrightarrow{AB} = 2\mathbf{a} + 3\mathbf{c}.$ CQ : QB = 2 : 3.

(a) Write each of the following in terms of a and c. Give your answers in their simplest form.

0

(i) 
$$\overrightarrow{BC}$$
,

Answer .....[1]

C

 $\overrightarrow{oQ}$ . (ii)

Answer .....[1]

(b) Use your answer to part (a) (ii) to explain why AB is parallel to OQ.

Answer	
	[1]

## (c) Find

(i) OQ:AB,

Answer .....[1]

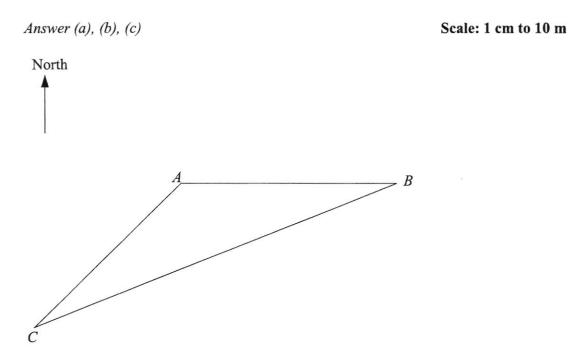
(ii)  $\frac{\text{Area of triangle } OAB}{\text{Area of triangle } OQB}$ ,

Answer .....[1]

(iii)  $\frac{\text{Area of triangle } OQC}{\text{Area of triangle } OBC}$ .

Answer .....[1]

## 24 The diagram below shows a scale drawing of triangle ABC.



(a) Measure the bearing of B from C.

Answer .....[1] Points A, B and C are on the ground and a WiFi router is placed at B. The WiFi router's signal can reach a distance of up to 42 m. (b) Construct the range of the WiFi signal from the WiFi router at B. [1] (c) Stacia is currently at C and starts walking along a path that is equidistant to AC and BC. She stops at a point that is equidistant from A and B. Locate this point by construction and label it S. [3] (i) Hence state if Stacia is able to receive the Wifi signal at S, giving a reason (ii) for your answer. Answer Stacia is ..... to receive the Wifi signal at S, ..... ..... 

[3]

#### CHIJ St. Nicholas Girls' School 2018 Preliminary Examination 2018 Mathematics Paper 2 k + h

1 (a) It is given that 
$$h = \frac{k+h}{3h-k}$$
.

(i)	Find the positive value of h when $k = 2h$ .	[1]
-----	--	-----

(ii) Express k in terms of h. [3]

(b) Solve the equation 
$$\frac{3x}{4} + \frac{1}{x} = 2$$
. [3]

(c) Solve these simultaneous equations

$$x + 4y + 3 = 0,$$
  

$$5x - 2y - 29 = 0.$$
 [2]

(d) Simplify 
$$\frac{2-5x-7x^2}{1-x^2}$$
. [3]

2 (a) The interior angles of a hexagon are

$$(2x+17)^{\circ}$$
,  $(3x-4)^{\circ}$ ,  $(2x+49)^{\circ}$ ,  $(x+40)^{\circ}$ ,  $(x-17)^{\circ}$ ,  $(3x-25)^{\circ}$ .

Find the smallest exterior angle.

(b) The areas of the two similar octagons are  $25 \text{ cm}^2$  and  $576 \text{ cm}^2$ . The length of the sides of the octagons are x cm and 7 cm.

Find the two possible values of *x*. [3]

CHIJ SNGS Preliminary Examinations 2018 - Mathematics 4048/02 [Turn over

3 A group of volunteers pack goodie bags for the residents of a nursing home. The table shows the contents of one of each type of goodie bag.

	Bag Type					
	Р		Q			R
Number of buns	5		3			4
Number of toothbrushes	2		1			2
Number of packets of Milo	2		3			2
Number of packets of coffee	1		2			3
This information can be represented by the	he matrix $A =$	$ \begin{pmatrix} 5 \\ 2 \\ 2 \\ 1 \end{pmatrix} $	3 1 3 2	4` 2 2 3	).	

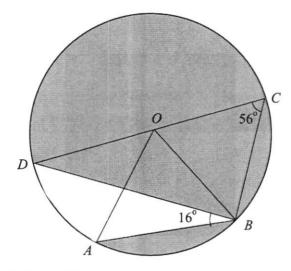
There are 20 bags of type P, 30 bags of type Q and 10 bags of type R.

(a)	(i)	Represent the numbers of the three types of goodie bags in a $3 \times 1$ column matrix <b>B</b> .	n [1]		
	(ii)	Evaluate the matrix $\mathbf{C} = \mathbf{AB}$ .	[2]		
	(iii)	State what the elements of C represent.	[1]		
(b)	A to A pa A pa	un costs \$1. othbrush costs \$1.50. acket of Milo costs \$6.40. acket of coffee costs \$5.60.			
	The elements of the matrix <b>E</b> , where $\mathbf{E} = \mathbf{D}\mathbf{A}$ , represent the costs, in dollars, of each bag of <i>P</i> , of <i>Q</i> and of <i>R</i> respectively.				
	(i)	Write down the matrix <b>D</b> .	[1]		
	(ii)	Evaluate the matrix <b>E</b> .	[1]		
(c)	Eval	uate the matrix $\mathbf{F} = \mathbf{E}\mathbf{B}$ .	[1]		
( <b>d</b> )	State	e what the element(s) of F represent.	[1]		

4 The first four terms in a sequence of numbers are given below.

$T_1 =$	$1^2 + 8 = 9$	
$T_2 =$	$2^2 + 12 = 16$	
$T_3 =$	$3^2 + 16 = 25$	
$T_4 =$	$4^2 + 20 = 36$	
(a)	Find $T_5$ .	[1]
(b)	Find an expression, in terms of $n$ , for the <i>n</i> th term, $T_n$ , of the sequence.	[2]
(c)	$T_p$ and $T_{p+1}$ are consecutive terms in the sequence.	
	Find and simplify an expression, in terms of $p$ , for $T_{p+1} - T_p$ .	[2]
(d)	Explain why two consecutive terms of the sequence cannot have a difference of less than 7.	[1]





The diagram shows a circle *ABCD*, centre *O* and radius 4 cm. *COD* is a diameter of the circle.

Angle  $ABD = 16^{\circ}$  and angle  $BCD = 56^{\circ}$ .

(a) Find the reflex angle DOB. [2]
(b) Find angle AOB. [2]
(c) Find the shaded area. [4]

## 6 Answer the whole of this question on a sheet of graph paper.

A ball was thrown from the top of a building.

The height, h metres, of the ball above ground level t seconds after it was thrown was measured every second.

Some corresponding values of t and h are given in the table below.

t	0	1	2	3	4	5	6	7
h	210	250	250	237	206	155	84	0

Using a scale of 2 cm to represent 1 second, draw a horizontal t-axis for 0 ≤ t ≤ 7.
 Using a scale of 4 cm to represent 100 metres, draw a vertical h-axis for 0 ≤ h ≤ 300.

On your axes, plot the points given in the table and join them with a smooth curve. [3]

- (b) Explain what the *h*-intercept of the curve represents. [1]
- (c) Use your graph to estimate

	(i)	the maximum height of the ball,	[1]
	(ii)	the time taken for the ball to reach its maximum height.	[1]
(d)	(i) (ii)	By drawing a tangent, find the gradient of the curve at (4, 206). Use your answer in (d)(i) to explain what was happening to the ball a	[2] at $t = 4$ .
			[1]

7 (a) A shopkeeper mixed 30 kg of Brand A tea, which he bought at \$32 per kg, with 20 kg of Brand B tea, which he bought at \$35 per kg. He sold all the mixture at \$40 per kg.

Determine whether the shopkeeper made a gain or loss from this transaction. Show your working clearly. [2]

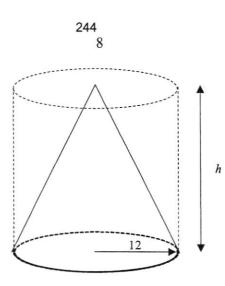
- (b) Mrs Tan bought some packets of coffee for \$800. Each packet of coffee costs x.
  - (i) Write down an expression, in terms of x, for the number of packets of coffee bought. [1]

It was found that 2 packets were damaged and had to be thrown away. Mrs Tan then sold each of the remaining packets of coffee for \$2 more than what she had paid for.

- (ii) Write down an expression, in terms of x, for the total sum received from the sale of the packets of coffee. [1]
- (iii) Given that Mrs Tan made a profit of \$99 from the sale of the packets of coffee, form an equation in x and show that it reduces to

$$2x^2 + 103x - 1600 = 0.$$
 [3]

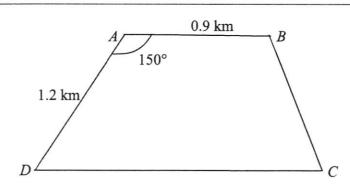
- (iv) Solve the equation  $2x^2 + 103x 1600 = 0$ . [3]
- (v) Find the number of packets of coffee sold. [1]



The diagram shows a solid cone of radius 12 cm and height h cm cut from a solid cylindrical steel block of the same radius and height.

(a)	The	cylinder has a volume of $4320\pi$ cm <sup>3</sup> . Find the value of h.	[2]			
(b)	Find	the total surface area of the cone.	[3]			
(c)	Afte	After the cone is cut from the steel block, the remaining steel is melted down an				
	made	e into a solid sphere.				
	(i)	Find the radius of the sphere.	[3]			

(ii) Find the surface area of the sphere. [1]



The diagram shows four towns A, B, C and D on a piece of horizontal land. *ABCD* is a trapezium.

AB = 0.9 km, AD = 1.2 km and angle  $BAD = 150^{\circ}$ .

- (a) Calculate the distance between Town B and Town D. [2]
- (b) Calculate the value of angle *BDC*. [2]
- (c) A tower is standing at Town B.The greatest angle of elevation of the top of the tower, T, from the path CD is 18°.

Find the height of the tower in metres.

[3]

**10 (a)** A chicken farmer fed 15 new-born chicks with a new variety of grain.

The stem-and-leaf diagram shows the weight gains of the chicks after three weeks.

37	8			
38	1	9		
37 38 39	0	5	6	
40	2	3	7	9
41	8	9		
40 41 42 43	5 9	7		
43	9			

Key 37 8 means 378 grams

(i)	Find the median weight gain.	[1]
(ii)	Find the interquartile range.	[2]

(iii) Calculate

(a)	the mean of the weight gain,	[1]

(b) the standard deviation. [2]

Chicks fed on the standard variety of grain had weight gains after three weeks.

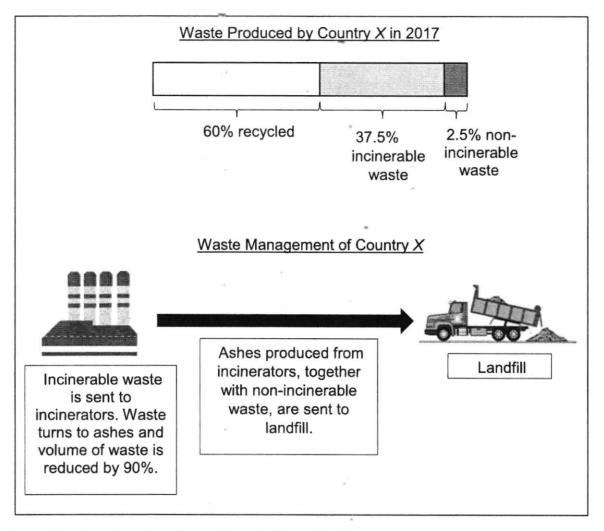
The mean of these weight gains was 392 grams while the standard deviation was 12 grams.

- (c) State briefly how the new variety of grain compares to the standard variety. [2]
- (b) Box A contains 6 red cards, 4 blue cards and 2 green cards. Box B contains 3 red cards and 5 blue cards.

A card is drawn at random from Box A and put into Box B. Next, a card is drawn at random from Box B.

- (i) Draw a tree diagram to show the probabilities of the possible outcomes. [2]
- (ii) Find, as a fraction in its simplest form, the probability that
  - (a) two green cards are drawn, [1]
    (b) neither of the cards is green, [1]
    (c) the two cards are of different colours. [2]

11 Country *X* produced 3 million tonnes of waste in 2017. The infographic below shows more information on the waste produced and the waste management of Country *X*.



Images from: <u>https://www.dreamstime.com/illustration/dumptruck.html</u>, <u>https://www.mewr.gov.sg/topic/landfill</u>

(a) Given that the density of waste is 125 kg/m<sup>3</sup> and 1 tonne = 1000 kg, calculate the volume of waste, in m<sup>3</sup>, that was incinerated in 2017. Give your answer in standard form.

The landfill used by Country X has a total capacity of 42 000 000  $\text{m}^3$ . By the end of 2017, 30% of the landfill has already been used. A news article claims it will take another 32 years before the landfill is completely used.

(b) Is the news article correct? Justify your decision with calculations. [6]
(c) State one assumption you made in your calculations in (b). [1]

1 (a) Given  $x^9 = 9^0$ , find the value of x.

$x^9 = 9^0$		
$x^9 = 1$		
x = 1	A1	

**(b)** Simplify 
$$\frac{x^2}{3y} \div \frac{x}{9y^2}$$
.

(b)  $\frac{x^2}{3y} \div \frac{x}{9y^2}$  $= \frac{x^2}{3y} \times \frac{9y^2}{x}$  $= 3xy \qquad A1$ 

2 Factorise 
$$2p-2q-p^2+pq$$
.

 $2p-2q-p^{2}+pq$ = 2(p-q)-p(p-q) M1 = (p-q)(2-p) A1

3 Write as a single fraction in its simplest form

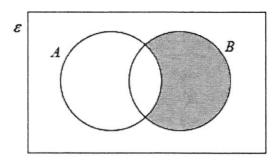
 $\frac{5x}{(3-x)^2} - \frac{1}{x-3}$  $-\frac{5x}{(x-3)^2} - \frac{1}{x-3} \quad \text{B1 for } 3 - x = -(x-3)$  $= \frac{5x - x + 3}{(x-3)^2}$  $= \frac{4x+3}{(x-3)^2} \text{ or } \frac{4x+3}{(3-x)^2} \text{ A1}$ 

$$\frac{5x}{\left(\mathbf{3}-\mathbf{x}\right)^2}-\frac{1}{x-3}.$$

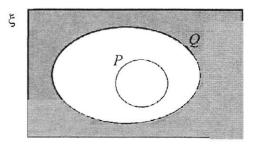
### [Turn over

[1]

4 (a) On the Venn diagram, shade the region which represents  $A' \cap B$ .



(b) Given that P is a subset of Q, simplify (P ∪ Q)'.
 You may use the space below to help in your investigation.



5 A shuttle bus is due to arrive at the ABC station at 09 30 daily.

The numbers of minutes by which the bus was late on ten successive days are shown below.

3 0 -2 -3 8 4 10 5 -4 9

(a) Explain the meaning of the number -2 in the list of numbers of minutes.

Answer

The number '-2' means the bus was early by 2 minutes

- (b) Find the mean number of minutes by which the bus was late.

(a) 
$$\bar{x} = \frac{30}{10} = 3 \min A1$$

- 6 Given that p is a positive integer,
  - (a) write down expressions for the next two even numbers after 2(p-1).

2p and 2p + 2 or 2(p+1) A1

(b) (i) find, in its simplest form, an expression for the sum of the squares of these three even numbers,

 $(2p-2)^{2} + (2p)^{2} + (2p+2)^{2}$ =  $4p^{2} - 8p + 4 + 4p^{2} + 4p^{2} + 8p + 4$  M1 follow thru =  $12p^{2} + 8$  A1

L

(ii) explain why this sum is a multiple of 4.

Answer  $12p^2 + 8 = 4(3p^2 + 2)$ , hence the sum has a factor of 4, this means the sum is a multiple of 4. OR  $4(3p^2 + 2)$  is a multiple of 4. [1]

7 (a) Express 40 and 138 as a product of their prime factors.

 $40 = 2^3 \times 5$  A1  $138 = 2 \times 3 \times 23$  A1

Answer  $40 = \dots$ [2]

(b) Hence, find the smallest positive integer k such that 138k is divisible by 40.

 $\frac{138k}{40} = \frac{2 \times 3 \times 23 \times k}{2^3 \times 5}$  $k = 2^2 \times 5$  $= 20 \qquad A1$ 

Answer smallest positive integer  $k = \dots$ [1]

A wooden cube with side 8 cm is cut into two-centimetre cubes.
 All of the two-centimetre cubes are then arranged to form a cuboid with height greater than 8 cm.

The perimeter of the top of the cuboid is 36 cm.

Find the height of the cuboid.

Total volume =  $8^3 = 512 \text{ cm}^3$ Total number of cubes =  $4^3 = 64 \text{ cubes}$ Breadth of cuboid = 2 cm Length of cuboid = 16 cm Height of cuboid =  $512 \div 2 \div 16$ = 16 cm

B1 for breadth or length

B1 for height

- 9 A map is drawn to a scale of  $1:40\,000$ .
  - (a) This scale can be expressed as 1 cm represents n km.

Find n.

(b) The distance between a seaport and an airport on the map is 60 cm.

Find the actual distance, in kilometres, between the seaport and airport.

 $0.4 \times 60 = 24 \,\mathrm{km} \,\mathrm{A1}$ 

Answer ...... km [1]

(c) A bus depot has an actual area of  $8 \text{ km}^2$ .

Find the area, in square centimetres, of the bus depot on the map.

 $1 \text{ cm}^2$ : 0.16 km<sup>2</sup> B1  $\frac{8}{0.16} = 50 \text{ cm}^2$  A1

Answer  $\dots$  cm<sup>2</sup> [2]

10 (a) Fynn deposited \$m into an account that paid a compound interest of 1.85% per annum. He made no other deposits or withdrawals for three years. At the end of three years, he had \$2509.26 in his account.

Find the value of m, giving your answer correct to the nearest dollar.

 $2509.26 = m \left(1 + \frac{1.85}{100}\right)^3 \quad B1$ m = \$2374.994.. m = \$2375 (nearest dollar) A1

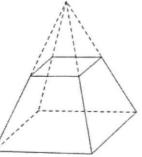
(b) Fynn withdrew all his money from the bank and used 30% of it to buy a watch. Subsequently he sold the watch for a profit of 60%.

Find the selling price of the watch.

$$\begin{array}{cccc} 2509.26 \times 0.3 & \text{M1} \\ = \$752.778 \\ \end{array} \qquad \qquad \begin{array}{c} \frac{160}{100} \times \$752.788 \\ = \$1204.44 \ (2 \text{ d.p.}) & \text{A1} \end{array}$$

11 The diagram shows a frustum obtained by removing a small pyramid with height half of that of the original pyramid.

[A frustum is a portion of a pyramid that is left after a smaller pyramid is removed from the top.]



Find the ratio of the volume of the frustum to the volume of the original pyramid.

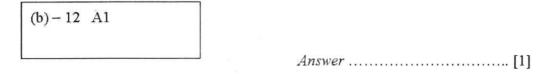
 $V_{top}: V_{original} = \left(\frac{1}{2}\right)^3: 1^3 \text{ B1 for cube}$   $= \frac{1}{8}: 1 = 1: 8$   $V_{fructum}: V_{original} = 1 - \frac{1}{8}: 1$   $= \frac{7}{8}: 1$  = 7: 8 B1

#### [Turn over

**12** (a) Express  $3x^2 - 12x$  in the form  $3[(x+a)^2 + b]$ .

(a) 
$$3x^2 - 12x$$
  
=  $3(x^2 - 4x)$  B1 for factor 3  
=  $3((x-2)^2 - 4)$  A1

(b) Write down the smallest value of  $3x^2 - 12x$ .



13 Cooking oil is sold in two sizes:\$4.80 for each 2 kg bottle

OR

\$6.95 for each 3 kg bottle

Which bottle gives the better value?

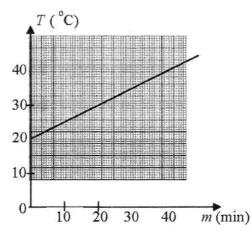
You must show your calculations.

$$\frac{4.80}{2} = 52.40$$
 per kg $\frac{6.95}{3} = $2.32$  per kgThe 3kg bottle gives the better value $\frac{2}{4.80} = 0.416666... \text{ kg per $}$  $\frac{3}{6.95} = 0.431654... \text{ kg per $}$ The 3kg bottle gives the better valueB1 for eitherB1 for answer

Answer The ..... kg-bottle gives the better value. [2]

BP~255

14 The graph shows the temperature,  $T^{\circ}C$ , of the water in a hot water tank after the heater is switched on for *m* minutes.



Use the graph to find

(a) the increase in temperature of the heater when it is switched on for 20 minutes,

Answer ..... °C [1]

(b) an equation for T in terms of m.

(b) 
$$T = 20 + \frac{1}{2}m$$
 A1

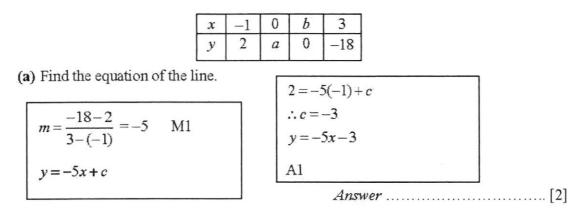
15 The distance between the points M(k,7) and N(9,k) is  $\sqrt{20}$ .

Given that k > 10, find the value of k.

$\sqrt{(k-9)^2 + (7-k)^2} = \sqrt{20}$	B1	
$k^2 - 18k + 81 + 49 - 14k + k^2 = 20$		
$2k^2 - 32k + 110 = 0$		
$k^2 - 16k + 55 = 0$		
(k-5)(k-11) = 0	M1	For factorising
k = 5  or  k = 11	DA1	
(NA)		

[Turn over

16 The table shows some corresponding values of x and y of the equation of a line.

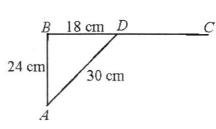


(b) Hence find the values of a and b.

a = -3	A1	
$b = -\frac{3}{5}$	A1	

*Answer*  $a = \dots, b = \dots [2]$ 

17



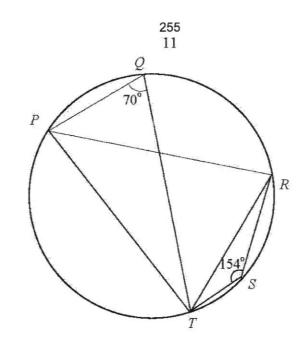
In triangle ABD, AB = 24 cm, BD = 18 cm, AD = 30 cm. BD is produced to C.

(a) Explain why angle ABD is a right angle.

$(AB)^2 + (BD)^2 = 24^2 + 18^2 = 900$	angle $ABD = 90^{\circ}$ by Pythagoras Theorem	A1
$= (30)^2$ = $(AD)^2$	Answer	

(b) Write down  $\cos \angle ADC$ .

$$\cos \angle ADC = -\cos \angle ADB$$
$$= -\frac{18}{30} = -\frac{3}{5} \quad A1$$



In the diagram, P, Q, R, S and T are points on the circumference of a circle. Angle  $TQP = 70^{\circ}$  and angle  $TSR = 154^{\circ}$ .

(a) Find angle PTR.

Give a reason for each step of your working.

 $\angle TPR = 180^{\circ} - \angle TSR$  ( $\angle s$  in opp segment are supp) =180° -154° M1 = 26°

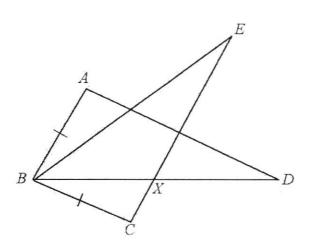
 $\angle PRT = \angle TQP = 70^{\circ}$  ( $\angle s$  in same segment) M1

 $\angle PTR = 180^{\circ} - 70^{\circ} - 26^{\circ} \quad (\angle \text{ sum of } \Delta) \text{ (can don't see this reason)}$ = 84° A1

(b) There is a point A on the same side of PT as point R. Angle  $TAP = 90^{\circ}$ .

Determine if point A lies on the circumference of the circle, inside or outside the circle. Justify your answer.

Answer	Point A liesinside	the circle because
if A lies	on the circumference, $\angle TAP = 70^{\circ}$ ( $\angle s$ in	the same segment), and since
	$\angle TAP = 90^{\circ} > 70^{\circ}$ , A lies inside the circle.	
••••••		



(a) In the diagram, BA = BC, angle ABE = angle CBD and angle BEC = angle BDA.
 Explain why triangles ABD and CBE are congruent.

	Answer			•••••	•••••	<b></b>				
	•••••			•••••	••••••					
										• • • •
	••••••								· · · · · · · · · · · · · · · · · · ·	
				•••••						
										[2]
(b)	Given fu	rther tha	t angle A	BE = ang	gle BEC,	what typ	e of quad	rilateral is	ABCE ?	

Justify your answer.

19(b) ABCE is a trapezium. A1

AB is parallel to CE because alternate angles, as angle ABE and angle BEC, are equal. A1

 $19(a) \angle ABE = \angle CBD \text{ (given)}$   $\angle ABE + \angle EBD = \angle CBD + \angle EBD$   $\therefore \angle ABD = \angle CBE$   $\angle BDA = \angle BEC \text{ (given)}$  BA = BC (given) M1 for any correct two conditions  $\Delta ABD = \triangle CBE \text{ (AAS)} \text{ A1}$ 

20 The table shows the number of people in groups of 1, 2, 3 and 4 people who attended a travel fair exhibition during a two -hour period.

No. of people in each group	1	2	3	4
No. of groups	20	94	85	26

Find

(a) the total number of people who attended the exhibition during the two-hour period,

(a)	$20 + 2 \times 94 + 3 \times 85 + 4 \times 26 = 567$	A1	

(b) the median number of people per group,

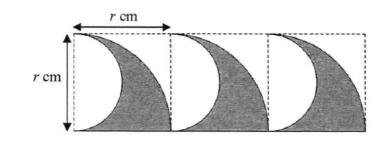
(b)	225 groups in total, 113 <sup>th</sup> group is the middle Median is 2 people per group	Al	
-----	--	----	--

(c) the percentage of groups with at least 2 people,

(c)	Total groups = $20 + 94 + 85 + 26 = 225$ 205 groups with at least 2 people. $\frac{205}{225} \times 100\%$	1 - <sup>2</sup> 10 	
	$=91\frac{1}{9}\%$ or 91.1 % (to 3 s.f.)	Al	

Answer .....%[1]





A surfing brand's logo consists of 3 waves.

Each wave is made up of a quadrant with a semicircle removed. (a) Find the perimeter of the logo in terms of r.

Arc length of quadrant =  $\frac{1}{4}(2 \times \pi \times r)$  B1 =  $\frac{\pi r}{2}$  cm Arc length of semi-circle =  $\frac{1}{2}\left(2\pi r \times \frac{1}{2}r\right)$  B1 no/wrong unit, -1 per paper =  $\frac{\pi r}{2}$  cm

Perimeter = 
$$3\left(\frac{\pi r}{2} + \frac{\pi r}{2} + r\right)$$
  
=  $3(\pi r + r)$  cm B1  
or  $(3\pi r + 3r)$  cm

Answer ...... cm [3]

The logo is drawn and then cut from a piece of fabric measuring 3r cm by r cm.

(b) Given that the area of the remaining fabric is  $16.4 \text{ cm}^2$ , find the value of r.

 $r^{2}\left(1-\frac{\pi}{8}\right) = \frac{16.4}{3} \quad \text{M1}\sqrt{\text{ for atempt to factorise}}$   $r = \sqrt{\frac{16.4}{3}}, \text{ r is positive}$   $r = 3.00 \text{ (to 3 s.f.)} \quad \text{A1 cannot '3'}$   $r = 3.00 \text{ (to 3 s.f.)} \quad \text{A1 cannot '3'}$   $r = 3.00 \text{ (to 3 s.f.)} \quad \text{A1 cannot '3'}$   $r = 3.00 \text{ (to 3 s.f.)} \quad \text{A1 cannot '3'}$ 

Area of logo = 
$$3\left[\frac{1}{4}\pi r^2 - \frac{1}{2}\pi \left(\frac{r}{2}\right)^2\right] = -\frac{3}{8}\pi r^2 \text{ cm}^2 \text{ B1}$$
  
 $3r^2 - \frac{3}{8}\pi r^2 = 16.4 \qquad \text{M1}\sqrt{\text{ for attempting to factorise}}$   
 $r = \sqrt{\frac{16.4}{\left(3 - \frac{3\pi}{8}\right)}}, \text{ where } r > 0 \quad , r = 3.00 \text{ (to } 3 \text{ s.f.) A1}$   
*Answer*  $r = \dots$  [3]

## **22** *A* is the point (-4, 11). The position vector of *B* is $\begin{pmatrix} 10 \\ 4 \end{pmatrix}$ .

.

(a) Express <i>BA</i> as a column vector.		
$ \begin{array}{c}  \\ BA = \begin{pmatrix} -4 \\ 11 \end{pmatrix} - \begin{pmatrix} 10 \\ 4 \end{pmatrix} = \begin{pmatrix} -14 \\ 7 \end{pmatrix} $	Á1	
	Answer	

(b) Calculate $ \overline{AB} $ .		
(b) $ \overline{AB}  =  \overline{BA}  = \sqrt{(-14)^2 + 7^2}$ = $\sqrt{245} = 15.7$ units (3 s.f.)	A1	

$$\overrightarrow{BC} = \begin{pmatrix} 0 \\ 6 \end{pmatrix} \text{ and } D \text{ is the point } (0, d).$$
(c) (i) Find the column vector  $\overrightarrow{OC}$ .  

$$\overrightarrow{OC} - \overrightarrow{OB} = \begin{pmatrix} 0 \\ 6 \end{pmatrix}$$

$$\overrightarrow{OC} = \begin{pmatrix} 0 \\ 6 \end{pmatrix} + \begin{pmatrix} 10 \\ 4 \end{pmatrix}$$

$$= \begin{pmatrix} 10 \\ 10 \end{pmatrix}$$
A1  
A1  
(ii) If  $\overrightarrow{BA}$  is parallel to  $\overrightarrow{CD}$ , find the value of  $d$ .  

$$(iii) \overrightarrow{BA} = h \overrightarrow{CD}$$

$$\begin{pmatrix} -14 \\ 7 \end{pmatrix} = h \left[ \begin{pmatrix} 0 \\ d \end{pmatrix} - \begin{pmatrix} 10 \\ 10 \end{pmatrix} \right]$$

$$= \begin{pmatrix} -10h \\ h(d-10) \end{pmatrix}$$

$$-10h = -14$$

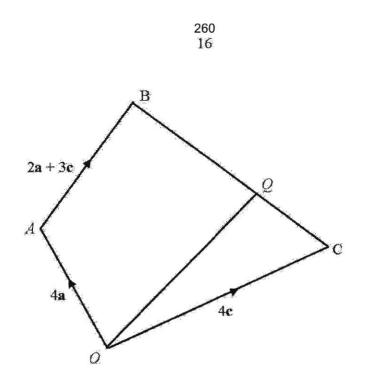
$$h = \frac{7}{5}$$
M1  

$$\overrightarrow{T}_{5}(d-10) = 7$$

$$d-10 = 5, d = 15$$
A1  
Answer  $d = \dots [3]$ 

CHIJ SNGS Preliminary Examinations 2018 - Mathematics 4048/01

[Turn over



OABC is a quadrilateral.

23

 $\overrightarrow{OA} = 4\mathbf{a}, \ \overrightarrow{OC} = 4\mathbf{c}, \ and \ \overrightarrow{AB} = 2\mathbf{a} + 3\mathbf{c}.$  CQ: QB = 2:3.

(a) Write each of the following in terms of a and c. Give your answers in their simplest form.

(i) 
$$\overrightarrow{BC}$$
,

$$B\vec{C} = \vec{B}\vec{A} + \vec{A}\vec{O} + O\vec{C}$$
  
=  $-\vec{A}\vec{B} + (-\vec{O}\vec{A}) + \vec{O}\vec{C}$   
=  $-2\mathbf{a} - 3\mathbf{c} - 4\mathbf{a} + 4\mathbf{c}$   
=  $-6\mathbf{a} + \mathbf{c}$   
[1]

 $\vec{oQ}$ .

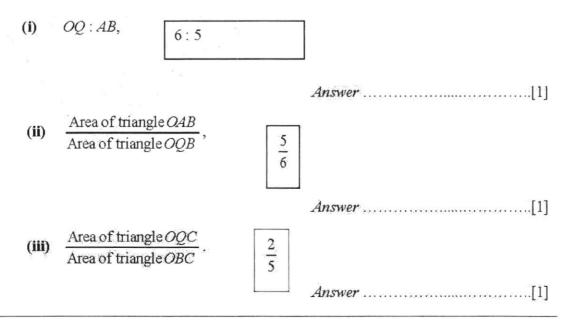
( <b>ii</b> )	$\overline{OQ} = \overline{OC} + \overline{CQ}$
	$=4\mathbf{c}+rac{2}{5}\overrightarrow{CB}$
	$=4\mathbf{c}+\frac{2}{5}(6\mathbf{a}-\mathbf{c})$
	$=\frac{12}{5}\mathbf{a}+\frac{18}{5}\mathbf{c}$ or $\frac{6}{5}(2\mathbf{a}+3\mathbf{c})$ A1

Answer ......[1]

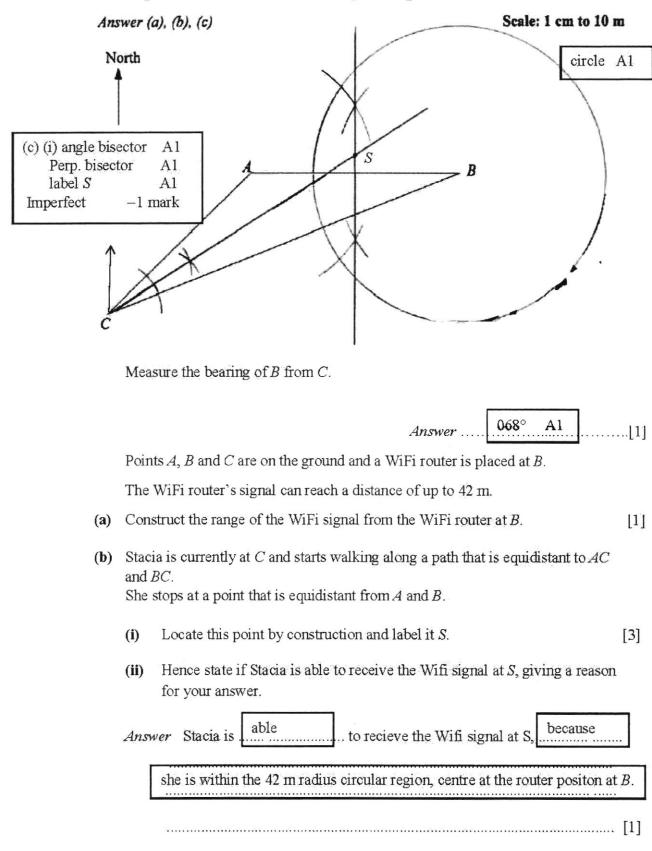
(b) Use your answer to part (a) (ii) to explain why AB is parallel to OQ.

Answer [1] (b)  $\overline{OQ} = \frac{6}{5}(2\mathbf{a} + 3\mathbf{c})$   $\therefore \overline{OQ} = \frac{6}{5}\overline{AB}$ Hence AB is parallel to OQ. A1

(c) Find



24 The diagram below shows a scale drawing of triangle ABC.



CHIJ St. Nicholas Girls' School 2018 Preliminary Examination Mathematics Paper 2 Answers

1 (a) (i) 3 (ii) 
$$k = \frac{h(3h-1)}{(1+h)}$$
 (b)  $x = 2, x = \frac{2}{3}$  (c)  $x = 5, y = -2$  (d)  $\frac{2-7x}{1-x}$ 

1---

2 (a) 19° (b) 1.46,33.6

3 (a) (i) 
$$\begin{pmatrix} 20\\ 30\\ 10 \end{pmatrix}$$
 (ii)  $\begin{pmatrix} 230\\ 90\\ 150\\ 110 \end{pmatrix}$ 

- (iii) The elements of C represent the <u>total numbers</u> of buns, of toothbrushes, of packets of Milo and of packets of coffee respectively, needed to pack <u>all</u> the bags.
- (b) (i)  $(1 \ 1.5 \ 6.4 \ 5.6)$  (ii)  $(26.4 \ 34.9 \ 36.6)$
- (c) (**1941**)
- (d) The element in F represents the <u>total cost</u> in dollars for packing the goodie bags.

4 (a) 49 (b) 
$$n^2 + 4n + 4$$
 (c)  $2p + 5$ 

- (d) As the difference between two consecutive terms is (2p + 5), and p is a positive integer, the smallest difference is 2(1) + 5, which is 7. Hence the difference cannot be less than 7.
- 5 (a)  $248^{\circ}$  (b)  $80^{\circ}$  (c)  $45.3 \text{ cm}^2$
- 6 (b) *h*-intercept represents the height of the building is 210 m.
  - (c) (i) 255 m (ii) 1.5 s
  - (d) (i) -36.8 (ii) The ball is falling at a speed of 36.8 m/s.

(b)(i) 
$$\frac{800}{x}$$
 (ii)  $\$\left(\frac{800}{x}-2\right)(x+2)$  (iv) 12.5, -64 (v) 62

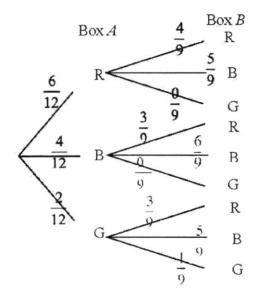
- 8 (a) 30 (b)  $1670 \text{ cm}^2$  (c) (i) 12.9 cm (ii)  $2100 \text{ cm}^2$
- 9 (a) 2.03 km (b) 17.2° (c) 195 m

10 (a) (i) 403 grams (ii) 29 grams (iii)(a) 405.2 grams (b) 17.1 grams (a) (iii) (c) As 392 < 405.3, chicks had more weight gain when fed with the new

variety of grain. As 12 < 17.1, the weight gain from the new variety of grain shows more spread in the results.

10 (b) (i)

(ii) (a) 
$$\frac{1}{54}$$
 (b)  $\frac{5}{6}$  (c)  $\frac{29}{54}$ 



11 (a)  $9 \times 10^6 \text{ m}^3$ 

- (b) No, the news article is incorrect.
   (with working to show it takes less than 32 yrs)
   (1 possible solution is the waste produced per year will take only 19.6 years before the landfill is completely used)
- (c) Possible answers:
  - Amount of incinerated and non-incinerable waste remains the same every year
  - The percentage breakdown of waste remains the same every year.

1 (a)	It is given that $h = \frac{k+h}{3h-k}$ .		
- (4)	(i) Find the positive value of h when $k = 2h$		[1]
	· ·	ε.	[1]
	(ii) Express k in terms of h. $3x = 1$		[3]
<b>(b)</b>	Solve the equation $\frac{3x}{4} + \frac{1}{x} = 2$ .		[3]
(c)	Solve these simultaneous equations		
	$\begin{array}{c} x + 4y + 3 = 0, \\ 5x - 2y - 29 = 0 \end{array}$		[2]
(d)	$\frac{1-x^2}{1-x^2}$		[3]
1(a)	Simplify $\frac{2-5x-7x^2}{1-x^2}$ . (i) $h = \frac{2h+h}{3h-(2h)}$		
	$h = \frac{3h}{h}$	A1	
	h = 3		
	$h = 3$ (ii) $h = \frac{k+h}{3h-k}$		
	$k+h=h(\mathbf{3h}-\mathbf{k})$	M1	No fraction
	$k+h=3h^2-hk$		
	$k+hk = 3h^2 - h$	M1	group like terms
	$k(1+h) = 3h^2 - h$	A1	
	$k = \frac{h(3h-1)}{(1+h)}$ or $\frac{3h^2 - h}{(1+h)}$		
(b)	$\frac{3x}{4} + \frac{1}{x} = 2$		
	$\frac{3\mathbf{x}^2 + 4}{3\mathbf{x}^2 + 4} = 2$		
	4x	M1	single fraction
	$3x^2 - 8x + 4 = 0$ $3x^2 - 8x + 4 = 0$	B1	
	(x-2)(3x-2)=0		
	$x = 2, x - \frac{2}{3}$	A1	
(c)	x + 4y + 3 = 0 (1)		
	5x - 2y - 29 = 0 (2)		
	$(1) \times 5, \ 5x + 20y + 15 = 0 \ \dots \ (3)$ $(3) - (2), \ 22y + 44 = 0$	M1	
	$\therefore y = -2,  x = 5$	Al	
(d)	$\frac{2-5x-7x^2}{1-x^2} = \frac{(2-7x)(1+x)}{(1-x)(1+x)}$	B1, B1	for each factorisation
	$=\frac{2-7x}{1-x}$	Al	
	1-x		

[Turn over

2 (a) The interior angles of a hexagon are

$$(2x+17)^{\circ}$$
,  $(3x-4)^{\circ}$ ,  $(2x+49)^{\circ}$ ,  $(x+40)^{\circ}$ ,  $(x-17)^{\circ}$ ,  $(3x-25)^{\circ}$ .

Find the smallest exterior angle.

(b) The areas of the two similar octagons are  $25 \text{ cm}^2$  and  $576 \text{ cm}^2$ . The length of the sides of the octagons are x cm and 7 cm.

Find the two possible values of x.

(a)	sum of interior angles = $12x + 60$		
	$12x + 60 = (6 - 2) \times 180$	M1✓	
	12x = 720 - 60		
	660		
	$x = \frac{660}{12}$		
	= 55	-	
	smallest exterior angle		
	$= 180^{\circ} - $ largest interior angle		
	$= 180^{\circ} - (3 \times 55 - 4)^{\circ}$	M1√	
	$= 180^{\circ} - 161^{\circ}$		
	- 100	A1	
(b)	* 25		
` ´	$\frac{x}{2} = \sqrt{\frac{25}{576}}$	M1	Either sq rt
	/ 10/0		-
	$\frac{x}{2} = \frac{5}{2}$		
	7 24		
	$x = 1.46 \text{ or } 1\frac{11}{11}$	A1	
	$1.1 \times = 1.40$ of $1{24}$		
	r 576		
	$\frac{x}{z} = \sqrt{\frac{570}{25}}$		
	7 25		
	$\frac{x}{24} = \frac{24}{24}$		
	7 5		
	$x = 33.6 \text{ or } 33\frac{3}{2}$		
	$\frac{x}{7} = \sqrt{\frac{25}{576}}$ $\frac{x}{7} = \frac{5}{24}$ $\therefore x = 1.46 \text{ or } 1\frac{11}{24}$ $\frac{x}{7} = \sqrt{\frac{576}{25}}$ $\frac{x}{7} = \frac{24}{5}$ $\therefore x = 33.6 \text{ or } 33\frac{3}{5}$	Al	

[3]

3 A group of volunteers pack goodie bags for the residents of a nursing home. The table shows the contents of one of each type of goodie bag.

		Bag Type	
	Р	Q	R
Number of buns	5	3	4
Number of toothbrushes	2	1	2
Number of packets of Milo	2	3	2
Number of packets of coffee	1	2	3

This information can be represented by the matrix  $\mathbf{A} = \begin{pmatrix} 5 & 3 & 4 \\ 2 & 1 & 2 \\ 2 & 3 & 2 \\ 1 & 2 & 3 \end{pmatrix}$ .

There are 20 bags of type P, 30 bags of type Q and 10 bags of type R.

(a)	(i)	Represent the numbers of the three types of <b>goodie bags</b> in a 3×1 column matrix <b>B</b> .	n [1]
	( <b>ii</b> )	Evaluate the matrix $\mathbf{C} = \mathbf{A}\mathbf{B}$ .	[2]
	<b>(iii)</b>	State what the elements of C represent.	[1]
(b)	A too A pa A pa	n costs \$1. othbrush costs \$1.50. cket of Milo costs \$6.40. cket of coffee costs \$5.60.	
		elements of the matrix <b>E</b> , where $\mathbf{E} = \mathbf{D}\mathbf{A}$ , represent the costs, in dollars, uch bag of <i>P</i> , of <i>Q</i> and of <i>R</i> respectively.	
	(i)	Write down the matrix <b>D</b> .	[1]
	( <b>ii</b> )	Evaluate the matrix <b>E</b> .	[1]
(c)	Eval	uate the matrix $\mathbf{F} = \mathbf{E}\mathbf{B}$ .	[1]

(d) State what the element(s) of F represent. [1]

BP~270

268

6

Links S.			· · · · · · · · · · · · · · · · · · ·
3(a)	(i) $\mathbf{B} = \begin{pmatrix} 20\\ 30\\ 10 \end{pmatrix}$	B1	
(a)	(ii) $\mathbf{C} = \begin{pmatrix} P & Q & R \\ 5 & 3 & 4 \\ 2 & 1 & 2 \\ 2 & 3 & 2 \\ 1 & 2 & 3 \end{pmatrix} \begin{pmatrix} 20 \\ 30 \\ 10 \end{pmatrix} \begin{pmatrix} P \\ 2 \\ 0 \\ 10 \end{pmatrix}$	M1√	
	$ \begin{bmatrix} 2 & 3 & 2 \\ 1 & 2 & 3 \end{bmatrix} $ (10) $R = \begin{bmatrix} 230 \\ 90 \end{bmatrix} $ buns toothbrush	Al	
	150 Milo 110 coffee		
(a)	(iii)The elements of <b>C</b> represent the <b><u>total numbers</u></b> of buns, of toothbrushes, of packets of Milo and of packets of coffee respectively, needed to pack <u>all</u> the bags.	A1	accept 'no packet'
(b)	(i) $\mathbf{D} = \begin{pmatrix} 1 & 1.5 & 6.4 & 5.6 \end{pmatrix}$	A1	accept 6.40, 5.60
(b)	(ii) $\mathbf{E} = \begin{bmatrix} B & TB & Milo & coffee \\ (1 & 1.50 & 6.40 & 5.60) \end{bmatrix} \begin{bmatrix} P & Q & R \\ 5 & 3 & 4 \\ 2 & 1 & 2 \\ 2 & 3 & 2 \\ 1 & 2 & 3 \end{bmatrix} \begin{bmatrix} TB \\ Milo \\ coffee \end{bmatrix}$ $= \begin{bmatrix} P & Q & R \\ (26.4 & 34.9 & 36.6) \end{bmatrix}$		accept 26.40,
(c)	$\mathbf{F} = \begin{pmatrix} P & Q & R \\ (26.4 & 34.9 & 36.6) \begin{pmatrix} 20 \\ 30 \\ 10 \end{pmatrix} \begin{pmatrix} P \\ Q \\ R \end{pmatrix}$	<u>A1</u>	34.90, 36.60 cannot 1940, cannot (\$1941)
	= (1941)	ΑΪ	3412 119
(d)	The element of <b>F</b> represents the <u>total cost</u> in dollars of <i>all the</i> <u>items</u> needed to pack <u>all the goodie bags</u> altogether. OR	A1	
	The element in F represents the <b>total cost</b> in dollars for packing the goodie bags.		

4 The first four terms in a sequence of numbers are given below.

$$T_{1} = 1^{2} + 8 = 9$$
  

$$T_{2} = 2^{2} + 12 = 16$$
  

$$T_{3} = 3^{2} + 16 = 25$$
  

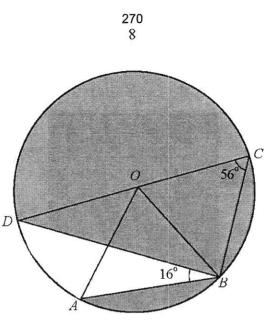
$$T_{4} = 4^{2} + 20 = 36$$
  
(a) Find  $T_{5}$ . [1]

- (b) Find an expression, in terms of n, for the *n*th term,  $T_n$ , of the sequence. [2]
- (c)  $T_p$  and  $T_{p+1}$  are consecutive terms in the sequence.

Find and simplify an expression, in terms of p, for  $T_{p+1} - T$  [2]

(d) Explain why two consecutive terms of the sequence cannot have a difference of less than 7. [1]

4(a)	$T_5 = 5^2 + 24 = 7^2 = 49$	A1	accept just 49
(b)	$T_{\rm h} = (n+2)^2$	A1 +	1 mark for ( <i>n</i> +2),
		A1	1 mark for perfect
	or $T_n = n^2 + 4(n+1)$	5	or 1 mark for $n^2$ or $4(n+1)$
	$= n^2 + 4n + 4$		1 mark for perfect
(c)	$T_{p+1} - T_p = (p+3)^2 - (p+2)^2$	M1	1 mark for $(p+3)^2$ or $(p+2)^2$ .
	$= (p^2 + 6p + 9) - (p^2 + 4p + 4)$		
	= 2p + 5	A1	1 mark for answer
	or	or	
	$T_{p+1} - T_p = (p+1)^2 + 4(p+2) - p^2 - 4p - 4$	M1	1 mark for $(p+1)^2+4(p+2)-p^2-4p-4$
	=2p+5	Al	$(p \cdot x) = (p \cdot 2) p \cdot p + q$
(d)	As the difference between two consecutive		
	terms is $(2p + 5)$ , and p is a positive integer, the		
	smallest difference is		
	2(1) + 5, which is 7. Hence the difference	À 1	
	cannot be less than 7.	A1	



The diagram shows a circle *ABCD*, centre *O* and radius 4 cm. *COD* is a diameter of the circle.

Angle  $ABD = 16^{\circ}$  and angle  $BCD = 56^{\circ}$ .

[2] [2] [4] 1 1 1
[4] 1 1
1
1
1
1
1 mark for either1 sector,
<ol> <li>1 mark for either area of triangle</li> <li>1 mark for either</li> <li>1 segment</li> <li>1 mark for total</li> <li>1 area</li> </ol>
[

5

## 6 Answer the whole of this question on a sheet of graph paper.

A ball was thrown from the top of a building.

The height, h metres, of the ball above ground level t seconds after it was thrown was measured every second.

Some corresponding values of t and h are given in the table below.

t	0	1	2	3	4	5	6	7
h	210	250	250	237	206	155	84	0

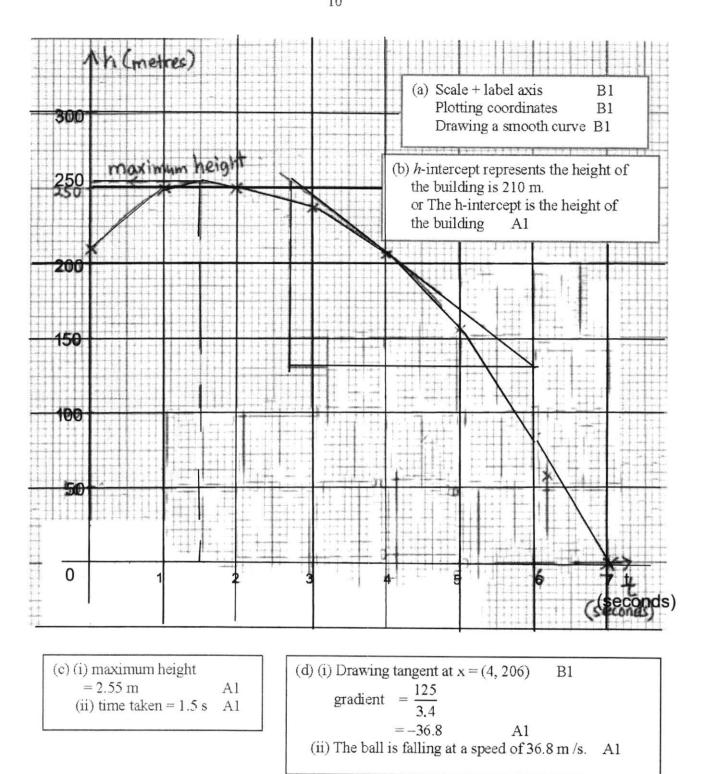
Using a scale of 2 cm to represent 1 second, draw a horizontal t-axis for 0 ≤ t ≤ 7.
 Using a scale of 4 cm to represent 100 metres, draw a vertical h-axis for 0 ≤ h ≤ 300.

On your axes, plot the points given in the table and join them with a smooth curve.

(b) (c)	Explain what the $h$ -intercept of the curve represents. Use your graph to estimate				
(-)	( <b>i</b> )	the maximum height of the ball,	[1]		
	( <b>ii</b> )	the time taken for the ball to reach its maximum height.	[1]		
(d)	( <b>i</b> )	By drawing a tangent, find the gradient of the curve at (4, 206).	[2]		
	( <b>ii</b> )	Use your answer in (d)(i) to explain what was happening to the ball at	t t = 4.		
			[1]		

BP~274

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7	(a)	with He se Dete	opkeeper mixed 30 kg of Brand $A$ tea, which he bo 20 kg of Brand $B$ tea, which he bought at \$35 per h old all the mixture at \$40 per kg. rmine whether the shopkeeper made a gain or loss wyour working clearly.	sg.
		51104	your working crearry.	[2]
	<b>(b)</b>	Mrs	Tan bought some packets of coffee for \$800. Each	packet of coffee costs \$x.
		( <b>i</b> )	Write down an expression, in terms of $x$ , for the n	umber of packets of
			coffee bought.	[1]
			s found that 2 packets were damaged and had to be	
			Tan then sold each of the remaining packets of cof	fee for \$2 more than what
			ad paid for.	. 1
		( <b>ii</b> )	Write down an expression, in terms of $x$ , for the to	
		(***)	sale of the packets of coffee.	[1]
		(iii)	Given that Mrs Tan made a profit of \$99 from the	-
			coffee, form an equation in $x$ and show that it redu	
			$2x^2 + 103x - 1600 = 0$	[3]
		(iv)	Solve the equation $2x^2 + 103x - 1600 = 0$ .	[3]
		(v)	Find the number of packets of coffee sold.	[1]
(a	)	30×32	2+20×35	method for finding
1		-	Alternative method M1	a oct por la of

(a)	$\frac{30 \times 32 + 20 \times 35}{30 + 20}$ \$33.20 per kg \$33.20 < \$40 Gain	Alternative method For 50 kg, cost is \$1660 Selling price is \$2000 \$1660 < \$2000	M1 A1	method for finding cost per kg of mixure Answer of 'gain'
(b)	(i) $\frac{800}{x}$	-	Al	
(ii)	$\left(\frac{800}{x}-2\right)(x+2)$	2)	A1	
(iii)	$\left(\frac{800}{x}-2\right)(x+2)$		M1	
	$\frac{800 + \frac{1600}{x} - 2x}{\frac{1600}{x} - 2x - 103}$		M1	
			B1	
(iv)	$2x^{2} + 103x - 160$ $(2x - 25)(x + 6)$ $\therefore x = 12.5, x = -100$	(4) = 0	M1 DA1, DA1	
(v)	$\frac{800}{12.5} - 2 = 62$		A1	



The diagram shows a solid cone of radius 12 cm and height h cm cut from a solid cylindrical steel block of the same radius and height.

- (a) The cylinder has a volume of  $4320\pi$  cm<sup>3</sup>. Find the value of h.
- (b) Find the total surface area of the cone.
- (c) After the cone is cut from the steel block, the remaining steel is melted down and made into a solid sphere.

12 cm

h cm

(i) Find the radius of the sphere.

	(ii) This are surface aloa of the sphere.		[*]
8(a)	$\pi(12)^2 h = 4320\pi$	B1	
	$h = \frac{4320}{144} = 30$	A1	units overall – 1
(b)	Slant height = $\sqrt{12^2 + 30^2}$	M1√	
	- √1044		
	= 32,31 cm		
	Total surface area		
	$=\pi(12)^{2}+\pi(12)(32.31)$	M1	
	$= 1670 \text{ cm}^2 (3 \text{ s.f})$	Al	
(c)(i)	Volume of remaining steel = $4320\pi - \frac{1}{3}\pi (12^2) 30$ or $\frac{2}{3}\pi (12)^2 (30)$	M1	
	$= 2880\pi \text{ cm}^{3}$ $= 2880\pi \text{ cm}^{3}$ $\frac{4}{3}\pi r^{3} = 2880\pi$ $r^{3} = 2160$ $r = 12.9 \text{ cm} (3 \text{ s.f})$	B1√ A1	
(ii)	Surface area of sphere $= 4\pi (12.92)^2$		
	≈ 2 097.6 = 2100 cm <sup>2</sup> (3 s.f.)	Á1	

( <b>ii</b> )	Find	the	surface	area	of	the	sphere.	
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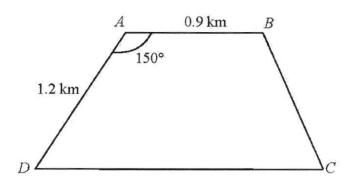
[3] [1]

[2]

[3]



**(b)** 



The diagram shows four towns A, B, C and D on a piece of horizontal land. ABCD is a trapezium.

- AB = 0.9 km, AD = 1.2 km and angle  $BAD = 150^{\circ}$ .
- (a) Calculate the distance between Town B and Town D.

[2] [2]

Calculate the value of angle BDC. A tower is standing at Town B. (c) The greatest angle of elevation of the top of the tower, T from the path CD is 18°. Find the height of the tower in metres. [3]

9(a)	BD <sup>2</sup> = $(0.9)^2$ + $(1.2)^2$ - 2 $(0.9)(1.2)$ cos 150° BD = 2.0299	M1	
	= 2.03  km (3  s.f.)	A1	
(b)	$\frac{\sin \angle ABD}{1.2} = \frac{\sin 150^{\circ}}{2.0299}$ $\sin \angle ABD = \frac{1.2\sin 150^{\circ}}{2.0299}$ $\angle ABD = 17.19^{\circ}$ $= 17.2^{\circ} \text{ (to 1 d.p.)}$ $\angle BDC = \angle ABD \text{ (alt } \angle \text{s, } AB \text{ // DC)}$ $= 17.2^{\circ}$	M1√ A1	accept no mention of angle property
(c)	Let the shortest distance from <i>B</i> to <i>CD</i> be <i>d</i> km. $\sin 17.19^\circ = \frac{d}{2.0299}$ d = 0.5999 km	М1√	
	Let x m be the height of the tower. $\frac{x}{0.5999} = \tan 18^{\circ}$ $x = 0.5999 \tan 18^{\circ}$ $= 0.1949 \text{ km}$	B1√ A1	
	= 195  m ( to  3  s.f.)		

[2]

A chicken farmer fed 15 new-born chicks with a new variety of grain. 10 (a)

The stem-and-leaf diagram shows the weight gains of the chicks after three weeks.

37	8			
<ul> <li>37</li> <li>38</li> <li>39</li> <li>40</li> <li>41</li> <li>42</li> <li>43</li> </ul>	1	9		
39	0	5	6	
40	2	3	7	9
41	2 8 5	9		
42		7		
43	9			

Key: 37 8 means 378 grams

(i)	Find the median weight gain.	[1]
( <b>ii</b> )	Find the interquartile range.	[2]
(iii)	Calculate	
940) (1940).	(a) the mean of the weight gain,	[1]

- (b) the standard deviation.

Chicks fed on the standard variety of grain had weight gains after three weeks. The mean of these weight gains was 392 grams while the standard deviation 12 grams.

(c) State briefly how the new variety of grain compares to the standard variety. [2]

10 (a)	(i) median weight gain = 403 grams	A1	
	(ii) interquartile range = $419 - 390$ = 29 grams	M1 A1	
	(iii)(a) mean weight gain= $\frac{6078}{15}$		
	= 405.2 grams	A1	
	(iii)(b) standard deviation = $\sqrt{\frac{2467210}{15} - \left(\frac{6078}{15}\right)^2}$ = 17.135 538	M1	
	= 17.1  grams ( to 3 s.f.)	Al	
	(iii)(c) 392 < 405.3, chicks had more weight gain when fed with the new variety of grain.	A1	
	12 < 17.1, the weight gain from the new variety of grain shows more spread / more variation / less consistent results.	A1	

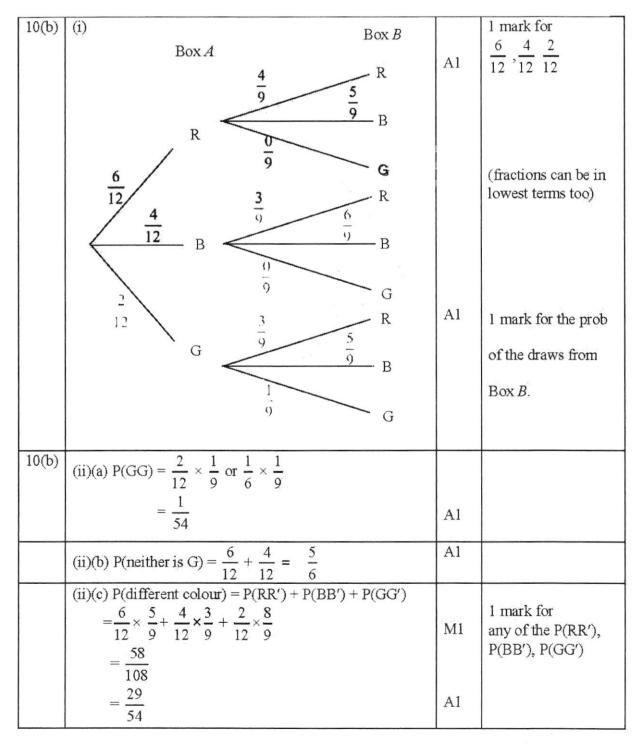
[1]

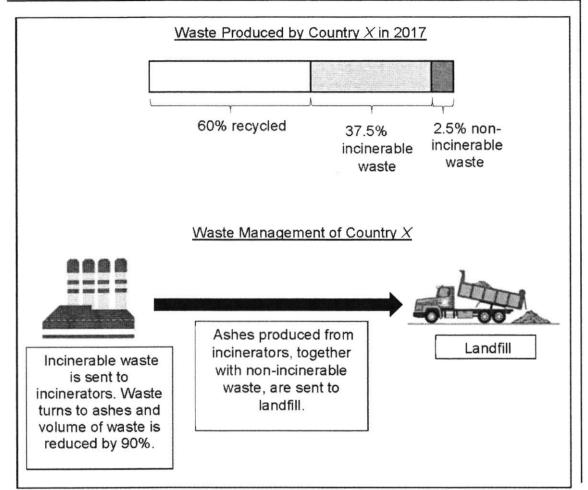
[1]

[2]

(b) Box A contains 6 red cards, 4 blue cards and 2 green cards. Box B contains 3 red cards and 5 blue cards. A card is drawn at random from Box A and put into Box B. Next, a card is drawn at random from Box B.
(b) Draw a trac diagram to show the match bilities of the possible subcomes

- (i) Draw a tree diagram to show the probabilities of the possible outcomes. [2]
- (ii) Find, as a fraction in its simplest form, the probability that
  - (a) two green cards are drawn,
  - (b) neither of the cards is green,
  - (c) the two cards are of different colours.





11 Country X produced 3 million tonnes of waste in 2017. The infographic below shows more information on the waste produced and the waste management of Country X.

Images from: <u>https://www.dreamstime.com/illustration/dumptruck.html</u>, <u>https://www.mewr.gov.sg/topic/landfill</u>

(a) Given that the density of waste is 125 kg/m<sup>3</sup> and 1 tonne = 1000 kg, calculate the volume of waste, in m<sup>3</sup>, that was incinerated in 2017. Give your answer in standard form. [3]

The landfill used by Country X has a total capacity of 42 000 000  $\text{m}^3$ . By the end of 2017, 30% of the landfill has already been used. A news article claims it will take another 32 years before the landfill is completely used.

<b>(b)</b>	Is the news article correct?	
	Justify your decision with calculations.	[6]

(c) State one assumption you made in your calculations in (b). [1]

10	(a) Mass of incinerable waste = $3\ 000\ 000 \times 37.5$ % tonnes	B1	
	= 1125000 tonnes		
	$= 1.125 \times 10^9 \text{ kg}$		
	Volume of incinerable waste = $\frac{1.125 \times 10^9}{125}$ m <sup>3</sup>		
	Volume of incinerable waste = $\frac{125}{125}$	M1√	
	$= 9\ 000\ 000\ \mathrm{m}^3$	A1	
	2.000 000 m	AI	
	3,000,000×1,000×2,5%		
	(b)Volume of non-incinerable waste = $\frac{3000000 \times 1000 \times 2.5\%}{125}$	M1	
	$= 600\ 000\ \mathrm{m}^3$		
	- 600 000 III		
	Values af ashes from incinerated master = 0.000.000 × 100/		
	Volume of ashes from incinerated waste = 9 000 000 $\times$ 10% = 900 000 m <sup>3</sup>	M1√	√ vol of
	= 900 000 III <sup>2</sup>		incin waste
	Total volume of waste to be landfilled = $600\ 000 + 900\ 000$		
	$= 1500\ 000\ \text{m}^3$		√vol of
	- 1500 000 III	M1√	non-incin
			and incin
			waste
	Volume of landfill left = 42 000 000 $\times$ 70%	B1	
	$= 29 \ 400 \ 000 \ \mathrm{m}^3$		
	29 400 000		
	Years left = $\frac{29\ 400\ 000}{1\ 500\ 000}$		
	= 19.6	A1	
	17.0		
	No, the news article is incorrect.	DA1	
	(d) Amount of incinerated and non-incinerable waste remains	A1	
	the same every year.		
1	n e n		
	Or		
	The percentage breakdown of waste remains the same every		
	year.		
	year.		

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Sec 4 Mathematics	Paper 1 - Prelims	2018

Qn No		Marks	Remarks
1	-5.25	B1	o.e. $-5\frac{1}{4}$
			Total : 1 mark
2	$2 \le \frac{f}{7} < 6$	B1	o.e. $14 \le \frac{f}{7} < 42$
			Total : 1 mark
3	5:2 = 22.5: 9	M1	Find the max. amt of red paint needed
	31.5	Al	
			Total : 2 marks
4	$\frac{21y-7}{14} - \frac{4y+10}{14} + \frac{14}{14}$	M1	Combine fraction (All terms with common denominator)
	$-\frac{17y-3}{14}$	A1	
			Total : 2 marks
5 a		B1	
b	116	B1	The by O mode
-	21 22 26 27 28	D1	Total: 2 marks
6	21, 23, 26, 27, 28	B1 B1	26 in Lie Luddle position seen
_		-	Total : 2 marks
7	$\left(\frac{4}{6}\right)^3$	M1	Find Vol ratio
	1.60	Al	Reject 1.6
			Total : 2 marks
8	Basic angle = $46.30$	M1	Find basic angle
	133.7	Al	Accept 2.33 soi
			Total : 2 marks
9 a	A de la de l	B1	
b	132	B1	DM from graph (up to \$220)
10	(20 6 4)	*	Total: 2 marks
10 a	(25 0 5)	B1	· ·
b	(65)	B1	
c	7	√B1	Reject negative
	02		Total : 3 marks
11 a		B1	Accept $2 \times 2 \times 3 \times 3 \times 3 \times 5$
b	54, 60	B1, B1	Total: 3 marks

281 Sec 4 Mathematics Paper 1 - Prelims 2018

Qn	No.	Solutions	Marks	Remarks
12	a	<u>x</u>	B1	
	1.	$\overline{20}$ x+10 $(x)$	N(1	Press trainting
	b	$\left \frac{x+10}{30} = 2\left(\frac{x}{20}\right)\right $	M1	Form equation
		30 \207		0
		x = 5	A1	
		<i>x</i> - 5		Total : 3 marks
13	a	x <sup>4</sup>	B1	
10		$\frac{\pi}{16y^{12}}$		
		109	90	
$\vdash$	b	$2^p \times 2^{-1} \times 3^p = 1$	M1	$2^{p-1} = 2p \div 2$
		$6^p = 4$	Al	
				Total : 3 marks
14	a	32	B1	
	b	Midlehand 3 49	B1	45 and 49
		Multiples of 3		
		39	B1	39, 42 and 51
		145 - 23		
		42		
		11		
		Mattiples of 6	1	
				Total : 3 marks
15		$\frac{3+1.4}{2} = 2.2$	M1	Find the parallel side
		2 0.5(1.4+2.2) 1.2 × 2.5	M1	Area of trapezium $\times$ 2.5
		5.4	A1	
				Total : 3 marks
16	а	$(x-7)^3 - 4(x-7)$		
		$=(x-7)[(x-7)^2-4]$	M1	Factorise $(x - 7)$
		=(x-5)(x-7)(x-9)	MI	Apply diff of 2 sq
			Al	
	b	6	√B1	
				Total : 4 marks
17	8	25%	B1	
	b	78.5	B1	
	с	Students performed better in	B1	
		Maths because higher median/mean marks.		
		median mean marks.		
		Students performed more	B1	
		consistently for Maths because of		
		smaller range.		
		0		Total : 4 marks

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Qn	No.	Solutions	Marks	Remarks
18	a	I disagree because $\frac{360}{55} = 6.545 \neq$	B1	Each ext. angle not a whole number.
		whole number/integer		
		whole number/mileger		
	b	144	M1	each int. angle of decagon
	U	Angle $CAD = 180 - 144 - 60$	M1 M1	each init angle of <i>n</i> -sided polygon
		= 156	IVII	each nit angle of n-stated polygon
		n = 360/24		
		=15	A1	
				Total : 4 marks
19		[10] Lines (B.	B1	Draw <i>PR</i> on bearing $116^{\circ} \pm 1^{\circ}$
		Ity ] Daw or (con)		Construction $\Delta PQR$
		D and stan		
		Cell make and Mart 1	B1	Draw arc 6 cm away from $Q(\pm 1mm)$
		1 to a strange		(
		In Bater		
		Part Part Part	B1	Angle bisector QPR with arc
				0
		A CONTRACTOR	B1	Mark out L.
			× <sup>4</sup>	
				<sup>·</sup> Total : 4 marks
20	a	\$1490.60	B1	cao
	b	% change = $\frac{their(a) - 1250}{1250} \times 100\%$	M1	
		$= 19.3^{1250}$		
		an 1997 a 19	Al	Accept 19.2, 19.3-
	с	4.5%	B1	2. S. S.
	d		B1	Shape
			B1 .	Vertical intercept
		1250	10. <sub>101</sub>	
				m + 1 < 1
1			DI	Total : 6 marks
21	a .	-0.5	B1	0.e
	b	(4, 4)	B1	
	c	2	√B1	
	d	(6, 3)	M1	Find the point the line cuts $2 - 2(x - x)$
		Sub in $(6,3)$ to find y-intercept	M1	y-3=2(x-6)
			A 1	
		y = 2x - 9	Al	0.e.
00		(-4)	D1	Total: 6 marks
22	а	$\begin{pmatrix} -4\\5 \end{pmatrix}$	B1	
	b	$\frac{(5)^2}{(2k)^2 + (-k)^2} = 180$	M1	Use magnitude
	-	$k = \pm 6$	Al	
	c(i)	(-7)	B1	
		( <sub>-1</sub> )		
	c(ii)	(-2, -5)	B1 B1	
				Total : 6 marks

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Sec 4 Mathematics	Paper 1 – Prelims 2018

Qn	No.	Solutions	Marks	Remarks
23	a	$A = \pi a^{2} + 2\pi ab$ $2\pi ab = A - \pi a^{2}$ $b = \frac{A - \pi a^{2}}{2\pi ab}$	M1	Isolate $2\pi ab$
		$b = \frac{1}{2\pi a}$	A1	
	b(i)	$\pi(5)^2 h = \frac{2}{3}\pi r^3$	B1	Equate the 2 volumes
		$r^3 = \frac{75h}{2}$	M1	Isolate $r^3$
		$r = \sqrt[3]{\frac{75h}{2}}$	A1	
	b(ii)	90	B1	
				Total: 6 marks
24	a	Small pipe: $\frac{1}{120}$ Big pipe: $\frac{1}{80}$ 30 mins	B1	Find rate of tank filled in one min. for at least one pipe
	1.(2)		Bl	form equation
	b(i)	$(30 - d)^2 + 27.5^2 = 30^2$ $(30 - d)^2 = 143.75$	M1 M1	form equation
		$(30 - d)^{-} = 143.75$ d = 18.0	A1	Solve equation
	b(ii)	42.0	√B1	60 – their b(i)
				Total: 6 marks